

LINDOGlobal

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1 Introduction

GAMS/LINDOGlobal finds guaranteed globally optimal solutions to general nonlinear problems with continuous and/or discrete variables. GAMS/LINDOGlobal supports most mathematical functions, including functions that are nonsmooth, such as $\text{abs}(x)$ and or even discontinuous, such as $\text{floor}(x)$. Nonlinear solvers employing methods like successive linear programming (SLP) or generalized reduced gradient (GRG) return a local optimal solution to an NLP problem. However, many practical nonlinear models are non-convex and have more than one local optimal solution. In some applications, the user may want to find a global optimal solution.

The LINDO global optimization procedure(GOP) employs branch-and-cut methods to break an NLP model down into a list of subproblems. Each subproblem is analyzed and either a) is shown to not have a feasible or optimal solution, or b) an optimal solution to the subproblem is found, e.g., because the subproblem is shown to be convex, or c) the subproblem is further split into two or more subproblems which are then placed on the list. Given appropriate tolerances, after a finite, though possibly large number of steps a solution provably global optimal to tolerances is returned. Traditional nonlinear solvers can get stuck at suboptimal, local solutions. This is no longer the case when using the global solver.

GAMS/LINDOGlobal can automatically linearize a number of nonlinear relationships, such as $\text{max}(x,y)$, through the addition of constraints and integer variables, so the transformed linearized model is mathematically equivalent to the original nonlinear model. Keep in mind, however, that each of these strategies will require additional computation time. Thus, formulating models, so they are convex and contain a single extremum, is desirable. In order to decrease required computing power and time it is also possible to disable the global solver and use GAMS/LINDOGlobal like a regular nonlinear solver.

GAMS/LINDOGlobal has a multistart feature that restarts the standard (non-global) nonlinear solver from a number of intelligently generated points. This allows the solver to find a number of locally optimal points and report the best one found. This alternative can be used when global optimization is costly. A user adjustable parameter controls the maximum number of multistarts to be performed.

LINDOGlobal automatically detects problem type and uses an appropriate solver, e.g., if you submit an LP model to LINDOGlobal, it will be solved as an LP at LP speed, regardless of what you said in the "solve using" statement. With the NLP parameter *NLP_QUADCHK* turned on, LINDOGlobal can detect hidden quadratic expressions and automatically recognize convex QCPs, as well as second-order cones (SOCP), like in Value-at-Risk models, allowing dramatically faster solution times via the barrier solver. When such models have integer variables, LINDOGlobal would use the barrier solver to solve all subproblems leading to significantly improved solution times when compared to the case with the standard NLP solver.

1.1 Licensing and software requirements

In order to use GAMS/LINDOGlobal, users need a GAMS/LINDOGlobal license. Additionally a GAMS/CONOPT license is required for solving nonlinear subproblems. The GAMS/LINDOGlobal license places upper limits on model size of 3,000 variables and 2,000 constraints. The GAMS/LINDOGlobal license does not include the Barrier solver option. LINDOGlobal would be able to use the barrier solver when the user has a separate license for the GAMS/MOSEK barrier solver.

1.2 Running GAMS/LINDOGlobal

GAMS/LINDOGlobal is capable of solving models of the following types: LP, MIP, RMIP, NLP, DNLP, QCP, MIQCP, RMINLP and MINLP. If GAMS/LINDOGlobal is not specified as the default solver for these models, it can be invoked by issuing the following command before the solve statement:

```
option xxx=lindoglobal;
```

where xxx is one of: LP, MIP, RMIP, NLP, DNLP, QCP, MIQCP, RMINLP, or MINLP.

You can also find global optima to math programs with equilibrium or complementarity constraints, type MPEC, by using the GAMS/NLPEC translator in conjunction with LINDOGlobal. You use NLPEC to translate complementarities into standard mathematical statements, e.g. $h^*y = 0$, and then use LINDOGlobal as the DNLP(Discontinuous Nonlinear) solver to solve the translated model. The following little GAMS model illustrates:

```
$TITLE simple mpec example
variable f, x1, x2, y1, y2; positive
variable y1; y2.lo = -1; y2.up = 1;

equations cost, g, h1, h2;

cost.. f =E= x1 + x2;
g..   sqr(x1) + sqr(x2) =L= 1;
h1..  x1 =G= y1 - y2 + 1;
h2..  x2 + y2 =N= 0;

* declare h and y complementary
model example / cost, g, h1.y1, h2.y2 /;

option mpec= nlpec;
option dnlp=lindoglobal;
solve example using mpec min f;
```

2 Supported nonlinear functions

GAMS/LINDOGlobal supports most nonlinear functions in global mode, including +, -, *, /, floor, modulo, sign, min, max, sqr, exp, power, ln, log, sqrt, abs, cos, sin, tan, cosh, sinh, tanh, arccos, arcsin, arctan and logic expressions AND, OR, NOT, and IF. Be aware that using highly nonconvex functions may lead to long solve times.

3 GAMS/LINDOGlobal output

The log output below is obtained for the NLP model mhw4d.gms from the GAMS model library using LINDO's global solver.

```
LINDOGLOBAL          8Apr10 23.4.0 WIN 17007.17023 VS8 x86/MS Windows
```

```
LINDOGLOBAL Driver
Lindo Systems Inc, www.lindo.com
```

```
Lindo API version 6.0.1.406 built on Mar 17 2010 22:51:09
Barrier Solver Version 5.0.0.127, Nonlinear Solver Version 3.14T
Platform Windows x86
```

```
Number of constraints:      3   le:      0, ge:      0, eq:      3, rn:      0 (ne:0)
Number of variables  :      5   lb:      0, ub:      0, fr:      5, bx:      0 (fx:0)
Number of nonzeros  :      8   density=0.0053(%)
```

```
Nonlinear variables  :      5
Nonlinear constraints:      4
Nonlinear nonzeros  :      5+5
```

Starting global optimization ...

```
Number of nonlinear functions/operators:  3
EP_MULTIPLY EP_POWER EP_SQR
```

Starting GOP presolve ...

```
Pre-check unboundedness
Computing reduced bound...
Searching for an initial solution...
```

Initial objective value: 0.029311

Starting reformulation ...

Model	Input	Operation	Atomic	Convex
Number of variables :	5	6	20	20
Number of constraints:	3	4	18	46
integer variables :	0	0	0	0
nonlinear variables :	5	5	9	0

Starting global search ...

```
Initial upper bound on objective: +2.931083e-002
Initial lower bound on objective: -3.167052e+022
```

#ITERS	TIME(s)	LOWER BOUND	UPPER BOUND	BOXES
1	0	-3.167052e+022	+2.931083e-002	1
41	0	+2.630106e-002	+2.931083e-002	35 (*I)

Terminating global search ...

```

Global optimum found
Objective value      :      0.0293108307216
Best Bound          :      0.0283736126217
Factors (ok, stb)   :                      892 (100.00, 99.78)
Simplex iterations  :                      4060
Barrier iterations  :                      0
Nonlinear iterations :                      627
Box iterations      :                      41
Total number of boxes :                    35
Max. Depth          :                      8
Total time (sec.)   :                      0

```

After determining the different kinds of nonlinear operators LINDOGlobal tries to linearize these within the presolving. When a feasible starting point is found the optimization starts and the log provides information about the progress. At the end it is reported if an optimum could be found and then the results as well as the used resources are summarized.

4 Summary of LINDOGlobal Options

LINDOGlobal offers a diverse range of user-adjustable parameters to control the behavior of its solvers. While the default values of these parameters work best for most purposes, there may be cases the users prefer to work with different settings for a subset of the available parameters. This section gives a list of available LINDOGlobal parameters, categorized by type, along with their brief descriptions. A more detailed description is given in the section that follows.

4.1 LINDOGlobal Options File

In order to set LINDOGlobal options, you need to set up an option file *lindoglobal.opt* in your GAMS project directory. You must indicate in the model that you want to use the option file by inserting before the solve statement, the line:

```
<modelname>.optfile = 1;
```

where

```
<modelname>
```

is the name of the model referenced in the model statement. The option file is in plain text format containing a single LINDOGlobal option per line. Each option identifier is followed by its target value with space or tab characters separating them. The lines starting with * character are treated as comments.

A sample option file *lindoglobal.opt* looks like below

```
* Use(1) or Disable(0) global optimization for NLP/MINLP models
```

```

USEGOP          0

* Enable Multistart NLP solver
NLP_SOLVER      9

* Allow a maximum of 3 multistart attempts
MAXLOCALSEARCH  3

* Set an overall time limit of 200 secs.
SOLVER_TIMLMT   200

```

4.2 General Options

DECOMPOSITION_TYPE	decomposition to be performed on a linear or mixed integer model
SOLVER_IUSOL	flag for computing basic solution for infeasible model
SOLVER_TIMLMT	time limit in seconds for continuous solver
SOLVER_FEASTOL	feasibility tolerance
SOLVER_RESTART	starting basis flag
SOLVER_OPTTOL	dual feasibility tolerance

4.3 LP Options

SPLEX_SCALE	scaling flag
SPLEX_ITRLMT	simplex iteration limit
SPLEX_PPRICING	pricing option for primal simplex method
SPLEX_REFACTORQ	number of simplex iterations between two consecutive basis re-factorizations
PROB_TO_SOLVE	controls whether the explicit primal or dual form of the given LP problem will be solved
SPLEX_DPRICING	pricing option for dual simplex method
SPLEX_DUAL_PHASE	controls the dual simplex strategy
LP_PRELEVEL	controls the amount and type of LP pre-solving
SOLVER_CUTOFFVAL	solver will exit if optimal solution is worse than this
SOLVER_USECUTOFFVAL	flag for using cutoff value

4.4 MIP Options

MIP_TIMLIM	time limit in seconds for integer solver
MIP_AOPTTIMLIM	time in seconds beyond which the relative optimality tolerance will be applied
MIP_LSOLTIMLIM	time limit until finding a new integer solution
MIP_PRELEVEL	controls the amount and type of MIP pre-solving at root node
MIP_NODESELRULE	specifies the node selection rule
MIP_INTTOL	absolute integer feasibility tolerance
MIP_RELINTTOL	relative integer feasibility tolerance
MIP_RELOPTTOL	MIP relative optimality tolerance
MIP_PEROPTTOL	MIP relative optimality tolerance in effect after MIP_AOPTTIMLIM seconds
MIP_MAXCUTPASS.TOP	number passes to generate cuts on the root node

MIP_MAXCUTPASS_TREE	number passes to generate cuts on the child nodes
MIP_ADDCUTPER	percentage of constraint cuts that can be added
MIP_ADDCUTPER_TREE	percentage of constraint cuts that can be added at child nodes
MIP_MAXNONIMP_CUTPASS	number of passes allowed in cut-generation that does not improve current relaxation
MIP_CUTLEVEL_TOP	combination of cut types to try at the root node when solving a MIP
MIP_CUTLEVEL_TREE	combination of cut types to try at child nodes in the B&B tree when solving a MIP
MIP_CUTTIMLIM	time to be spent in cut generation
MIP_CUTDEPTH	threshold value for the depth of nodes in the B&B tree
MIP_CUTFREQ	frequency of invoking cut generation at child nodes
MIP_HEULEVEL	specifies heuristic used to find integer solution
MIP_CUTOFFOBJ	defines limit for branch & bound
MIP_USECUTOFFOBJ	flag for using branch and bound limit
MIP_STRONGBRANCHLEVEL	depth from the root in which strong branching is used
MIP_TREEREORDERLEVEL	tree reordering level
MIP_BRANCHDIR	first branching direction
MIP_TOPOPT	optimization method to use when there is no previous basis
MIP_REOPT	optimization method to use when doing reoptimization
MIP_SOLVERTYPE	optimization method to use when solving mixed-integer models
MIP_KEEPIINMEM	flag for keepin LP bases in memory
MIP_BRANCHRULE	rule for choosing the variable to branch
MIP_REDCOSTFIX_CUTOFF	cutoff value as a percentage of the reduced costs
MIP_ADDCUTOBJTOL	required objective improvement to continue generating cuts
MIP_HEUMINTIMLIM	minimum time in seconds to be spent in finding heuristic solutions
MIP_BRANCH_PRIO	controls how variable selection priorities are set and used
MIP_SCALING_BOUND	maximum difference between bounds of an integer variable for enabling scaling
MIP_PSEUDOCOST_WEIGT	weight in pseudocost computations for variable selection
MIP_LBIGM	Big-M value used in linearizing nonlinear expressions
MIP_DELTA	near-zero value used in linearizing nonlinear expressions
MIP_DUAL_SOLUTION	flag for computing dual solution of LP relaxation
MIP_BRANCH_LIMIT	limit on the total number of branches to be created during branch and bound
MIP_ITRLIM	iteration limit for branch and bound
MIP_AGGCUTLIM_TOP	max number of constraints involved in derivation of aggregation cut at root node
MIP_AGGCUTLIM_TREE	max number of constraints involved in derivation of aggregation cut at tree nodes
MIP_ANODES_SWITCH_DF	threshold on active nodes for switching to depth-first search
MIP_ABSOPTTOL	MIP absolute optimality tolerance
MIP_MINABSOBJSTEP	value to update cutoff value each time a mixed integer solution is found
MIP_PSEUDOCOST_RULE	specifies the rule in pseudocost computations for variable selection
MIP_USE_ENUM_HEU	frequency of enumeration heuristic
MIP_PRELEVEL_TREE	amount and type of MIP pre-solving at tree nodes
MIP_REDCOSTFIX_CUTOFF_TREE	cutoff value as a percentage of the reduced costs at tree nodes
MIP_USE_INT_ZERO_TOL	controls if all MIP calculations would be based on absolute integer feasibility tolerance
MIP_USE_CUTS_HEU	controls if cut generation is enabled during MIP heuristics
MIP_BIGM_FOR_INTTOL	threshold for which coefficient of a binary variable would be considered as big-M
MIP_STRONGBRANCHDONUM	minimum number of variables to try the strong branching on
MIP_MAKECUT_INACTIVE_COUNT	threshold for times a cut could remain active after successive reoptimization
MIP_PRE_ELIM_FILL	controls fill-in introduced by eliminations during pre-solve

4.5 NLP Options

NLP_SOLVE_AS_LP	flag indicating if the nonlinear model will be solved as an LP
NLP_SOLVER	type of nonlinear solver
NLP_SUBSOLVER	type of nonlinear subsolver
NLP_PSTEP_FINITEDIFF	value of the step length in computing the derivatives using finite differences
NLP_DERIV_DIFFTYPE	flag indicating the technique used in computing derivatives with finite differences
NLP_FEASTOL	feasibility tolerance for nonlinear constraints
NLP_REDTOL	tolerance for the gradients of nonlinear functions
NLP_USE_CRASH	flag for using simple crash routines for initial solution
NLP_USE_STEEPEdge	flag for using steepest edge directions for updating solution
NLP_USE_SLP	flag for using sequential linear programming step directions for updating solution
NLP_USE_SELCONVAL	flag for using selective constraint evaluations for solving NLP
NLP_PRELEVEL	controls the amount and type of NLP pre-solving
NLP_ITRLMT	nonlinear iteration limit
NLP_LINEARZ	extent to which the solver will attempt to linearize nonlinear models
NLP_STARTPOINT	flag for using initial starting solution for NLP
NLP_QUADCHK	flag for checking if NLP is quadratic
NLP_AUTODERIV	defining type of computing derivatives
NLP_MAXLOCALSEARCH	maximum number of local searches
NLP_USE_LINDO_CRASH	flag for using advanced crash routines for initial solution
NLP_STALL_ITRLMT	iteration limit before a sequence of non-improving NLP iterations is declared as stalling
NLP_AUTOHESS	flag for using Second Order Automatic Differentiation for solving NLP

4.6 Global Options

OPTTOL	optimality tolerance
FLTOL	floating-point tolerance
BOXTOL	minimal width of variable intervals
WIDTOL	maximal width of variable intervals
DELTATOL	delta tolerance in GOP convexification
BNDLIM	max magnitude of variable bounds used in GOP convexification
TIMLIM	time limit in seconds for GOP branch-and-bound
OPTCHKMD	criterion used to certify the global optimality
BRANCHMD	direction to branch first when branching on a variable
MAXWIDMD	maximum width flag for the global solution
PRELEVEL	amount and type of GOP presolving
POSTLEVEL	amount and type of GOP postsolving
BBSRCHMD	node selection rule in GOP branch-and-bound
DECOMPPTMD	decomposition point selection rule in GOP branch-and-bound
ALGREFORMMD	algebraic reformulation rule for a GOP
RELBRNDMD	reliable rounding in the GOP branch-and-bound
USEBNDLIM	max magnitude of variable bounds flag for GOP convexification
BRANCH_LIMIT	limit on the total number of branches to be created in GOP tree
CORELEVEL	strategy of GOP branch-and-bound
OPT_MODE	mode for GOP optimization
HEU_MODE	heuristic used in global solver
SUBOUT_MODE	substituting out fixed variables

LSOLBRANLIM branch limit until finding a new nonlinear solution
 USEGOP use global optimization

4.7 Link Options

CHECKRANGE calculate feasible range for variables
 WRITEMPI write MPI file of processed model

5 Detailed Descriptions of LINDOGlobal Options

DECOMPOSITION_TYPE (*integer*)

This refers to the type of decomposition to be performed on a linear or mixed integer model.

(*default = 1*)

- 0 Solver decides which type of decomposition to use
- 1 Solver does not perform any decompositions and uses the original model
- 2 Attempt total decomposition
- 3 Decomposed model will have dual angular structure
- 4 Decomposed model will have block angular structure
- 5 Decomposed model will have both dual and block angular structure

SPLEX_SCALE (*integer*)

This is the scaling flag. Scaling multiplies the rows and columns of the model by appropriate factors in an attempt to avoid numerical difficulties by reducing the range of coefficient values.

(*default = 1*)

- 0 Scaling is suppressed
- 1 Scaling is performed

SPLEX_ITRLMT (*integer*)

This is a limit on the number of iterations the solver will perform before terminating. If this value is a nonnegative integer, then it will be used as an upper bound on the number of iterations the solver will perform. If this value is -1, then no iteration limit will be used. The solution may be infeasible.

(*default = GAMS IterLim*)

SPLEX_PPRICING (*integer*)

This is the pricing option to be used by the primal simplex method.

(*default = -1*)

- 1 Solver decides the primal pricing method
- 0 Partial pricing
- 1 Devex

SPLEX_REFACFRQ (*integer*)

This is a positive integer scalar referring to the simplex iterations between two consecutive basis re-factorizations. For numerically unstable models, setting this parameter to smaller values may help.

(*default = 100*)

PROB_TO_SOLVE (*integer*)

This flag controls whether the explicit primal or dual form of the given LP problem will be solved.

(default = 0)

- 0 Solver decides
- 1 Explicit primal form
- 2 Explicit dual form

SPLEX_DPRICING (*integer*)

This is the pricing option to be used by the dual simplex method.

(default = -1)

- 1 Solver decides the dual pricing method
- 0 Partial pricing
- 1 Steepest edge

SPLEX_DUAL_PHASE (*integer*)

This controls the dual simplex strategy, single-phase versus two-phase.

(default = 0)

- 0 Solver decides
- 1 Single-phase
- 2 Two-phase

LP_PRELEVEL (*integer*)

This controls the amount and type of LP pre-solving to be used.

(default = 126)

- +2 Simple pre-solving
- +4 Probing
- +8 Coefficient reduction
- +16 Elimination
- +32 Dual reductions
- +64 Use dual information
- +512 Maximum pass

SOLVER_IUSOL (*integer*)

This is a flag that, when set to 1, will force the solver to compute a basic solution to an infeasible model that minimizes the sum of infeasibilities and a basic feasible solution to an unbounded problem from which an extreme direction originates. When set to the default of 0, the solver will return with an appropriate status flag as soon as infeasibility or unboundedness is detected. If infeasibility or unboundedness is declared with presolver's determination, no solution will be computed.

(default = 0)

- 0 Return appropriate status if infeasibility is encountered
- 1 Force the solver to compute a basic solution to an infeasible model

SOLVER_TIMLMT (*integer*)

This is a time limit in seconds for the LP solver. The default value of -1 imposes no time limit.

(default = GAMS ResLim)

SOLVER_CUTOFFVAL (*real*)

If the optimal objective value of the LP being solved is shown to be worse than this (e.g., if the dual simplex method is being used), then the solver will exit without finding a feasible solution. This is a way of saving computer time if there is no sufficiently attractive solution. [SOLVER_USECUTOFFVAL](#) needs to be set to 1 to activate this value.

(default = 0)

SOLVER_FEASTOL (*real*)

This is the feasibility tolerance. A constraint is considered violated if the artificial, slack, or surplus variable associated with the constraint violates its lower or upper bounds by the feasibility tolerance.

(default = 1e-7)

SOLVER_RESTART (*integer*)

This is the starting basis flag. 1 means LINDO API will perform warm starts using any basis currently in memory. 0 means LINDO API will perform cold starts discarding any basis in memory and starting from scratch.

(default = 0)

- 0 Perform cold start
- 1 Perform warm start

SOLVER_OPTTOL (*real*)

This is the optimality tolerance. It is also referred to as the dual feasibility tolerance. A dual slack (reduced cost) is considered violated if it violates its lower bound by the optimality tolerance.

(default = 1e-7)

SOLVER_USECUTOFFVAL (*integer*)

This is a flag for the parameter [SOLVER_CUTOFFVAL](#)

(default = 0)

- 0 Do not use cutoff value
- 1 Use cutoff value

NLP SOLVE_AS_LP (*integer*)

This is a flag indicating if the nonlinear model will be solved as an LP. 1 means that an LP using first order approximations of the nonlinear terms in the model will be used when optimizing the model with the `LSoptimize()` function.

(default = 0)

- 0 NLP will not be solved as LP
- 1 NLP will be solved as LP

NLP_SOLVER (*integer*)

This value determines the type of nonlinear solver.

(default = 7)

- 4 Solver decides
- 7 Uses CONOPTs reduced gradient solver
- 9 Uses CONOPT with multistart feature enabled

NLP_SUBSOLVER (*integer*)

This controls the type of linear solver to be used for solving linear subproblems when solving nonlinear models.

(default = 1)

- 1 Primal simplex method
- 2 Dual simplex method
- 3 Barrier solver with or without crossover

NLP_PSTEP_FINITEDIFF (*real*)

This controls the value of the step length in computing the derivatives using finite differences.
(*default = 5e-7*)

NLP_DERIV_DIFFTYPE (*integer*)

This is a flag indicating the technique used in computing derivatives with Finite Differences.
(*default = 0*)

- 0 The solver decides
- 1 Use forward differencing method
- 2 Use backward differencing method
- 3 Use center differencing method

NLP_FEASTOL (*real*)

This is the feasibility tolerance for nonlinear constraints. A constraint is considered violated if the artificial, slack, or surplus variable associated with the constraint violates its lower or upper bounds by the feasibility tolerance.

(*default = 1e-6*)

NLP_REDGTOL (*real*)

This is the tolerance for the gradients of nonlinear functions. The (projected) gradient of a function is considered to be the zero-vector if its norm is below this tolerance.

(*default = 1e-7*)

NLP_USE_CRASH (*integer*)

This is a flag indicating if an initial solution will be computed using simple crash routines.

(*default = 0*)

- 0 Do not use simple crash routines
- 1 Use simple crash routines

NLP_USE_STEEPEdge (*integer*)

This is a flag indicating if steepest edge directions should be used in updating the solution.

(*default = 0*)

- 0 Do not use steepest edge directions
- 1 Use steepest edge directions

NLP_USE_SLP (*integer*)

This is a flag indicating if sequential linear programming step directions should be used in updating the solution.

(*default = 1*)

- 0 Do not use sequential linear programming step directions
- 1 Use sequential linear programming step directions

NLP_USE_SELCONeVAL (*integer*)

This is a flag indicating if selective constraint evaluations will be performed in solving a nonlinear model.

(*default = 1*)

- 0 Do not use selective constraint evaluations
- 1 Use selective constraint evaluations

NLP_PRELEVEL (*integer*)

This controls the amount and type of NLP pre-solving.

(default = 126)

- +2 Simple pre-solving
- +4 Probing
- +8 Coefficient reduction
- +16 Elimination
- +32 Dual reductions
- +64 Use dual information
- +512 Maximum pass

NLP_ITRLMT (*integer*)

This controls the iteration limit on the number of nonlinear iterations performed.

(default = GAMS IterLim)

NLP_LINEARZ (*integer*)

This determines the extent to which the solver will attempt to linearize nonlinear models.

(default = 0)

- 0 Solver decides
- 1 No linearization occurs
- 2 Linearize ABS MAX and MIN functions
- 3 Same as option 2 plus IF AND OR NOT and all logical operators are linearized

NLP_STARTPOINT (*integer*)

This is a flag indicating if the nonlinear solver should accept initial starting solutions.

(default = 1)

- 0 Do not use initial starting solution for NLP
- 1 Use initial starting solution for NLP

NLP_QUADCHK (*integer*)

This is a flag indicating if the nonlinear model should be examined to check if it is a quadratic model.

(default = 0)

- 0 Do not check if NLP is quadratic
- 1 Check if NLP is quadratic

NLP_AUTODERIV (*integer*)

This is a flag to indicate if automatic differentiation is the method of choice for computing derivatives and select the type of differentiation.

(default = 0)

- 0 Finite Differences approach will be used
- 1 Forward type of Automatic Differentiation will be used
- 2 Backward type of Automatic Differentiation will be used

NLP_MAXLOCALSEARCH (*integer*)

This controls the maximum number of local searches (multistarts) when solving a NLP using the multistart solver.

(default = 5)

NLP_USE_LINDO_CRASH (*integer*)

This is a flag indicating if an initial solution will be computed using advanced crash routines.

(default = 1)

- 0 Do not use advanced crash routines
- 1 Use advanced crash routines

NLP_STALL_ITRLMT (*integer*)

This specifies the iteration limit before a sequence of non-improving NLP iterations is declared as stalling, thus causing the solver to terminate.

(default = 100)

NLP_AUTOHESS (*integer*)

This is a flag to indicate if Second Order Automatic Differentiation will be performed in solving a nonlinear model. The second order derivatives provide an exact/precise Hessian matrix to the SQP algorithm, which may lead to less iterations and better solutions, but may also be quite expensive in computing time for some cases.

(default = 0)

- 0 Do not use Second Order Automatic Differentiation
- 1 Use Second Order Automatic Differentiation

MIP_TIMLIM (*integer*)

This is the time limit in seconds for branch-and-bound. The default value is -1, which means no time limit is imposed. However, the value of [SOLVER_TIMLMT](#) will be applied to each continuous subproblem solve. If the value of this parameter is greater than 0, then the value of [SOLVER_TIMLMT](#) will be disregarded. If this time limit is reached and a feasible integer solution was found, it will be installed as the incumbent (best known) solution.

(default = GAMS ResLim)

MIP_AOPTTIMLIM (*integer*)

This is the time in seconds beyond which the relative optimality tolerance, [MIP_PEROPTTOL](#) will be applied.

(default = 100)

MIP_LSOLTIMLIM (*integer*)

(default = -1)

MIP_PRELEVEL (*integer*)

This controls the amount and type of MIP pre-solving at root node.

(default = 510)

- +2 Simple pre-solving
- +4 Probing
- +8 Coefficient reduction
- +16 Elimination
- +32 Dual reductions
- +64 Use dual information

- +128 Binary row presolving
- +256 Row aggregation
- +512 Maximum pass

MIP_NODESELRULE (integer)

This specifies the node selection rule for choosing between all active nodes in the branch-and-bound tree when solving integer programs. Possible selections are: 0: Solver decides (default). 1: Depth first search. 2: Choose node with worst bound. 3: Choose node with best bound. 4: Start with best bound. If no improvement in the gap between best bound and best integer solution is obtained for some time, switch to: if (number of active nodes > 10000) Best estimate node selection (5). else Worst bound node selection (2). 5: Choose the node with the best estimate, where the new objective estimate is obtained using pseudo costs. 6: Same as (4), but start with the best estimate.

(default = 0)

- 0 Solver decides
- 1 Depth first search
- 2 Choose node with worst bound
- 3 Choose node with best bound
- 4 Start with best bound
- 5 Choose the node with the best estimate
- 6 Same as 4 but start with the best estimate

MIP_INTTOL (real)

An integer variable is considered integer feasible if the absolute difference from the nearest integer is smaller than this.

(default = 1e-6)

MIP_RELINTTOL (real)

An integer variable is considered integer feasible if the difference between its value and the nearest integer value divided by the value of the nearest integer is less than this.

(default = 8e-6)

MIP_RELOPTTOL (real)

This is the MIP relative optimality tolerance. Solutions must beat the incumbent by at least this relative amount to become the new, best solution.

(default = 1e-5)

MIP_PEROPTTOL (real)

This is the MIP relative optimality tolerance that will be in effect after T seconds following the start. The value T should be specified using the [MIP_AOPTTIMLIM](#) parameter.

(default = 1e-5)

MIP_MAXCUTPASS_TOP (integer)

This controls the number passes to generate cuts on the root node. Each of these passes will be followed by a reoptimization and a new batch of cuts will be generated at the new solution.

(default = 200)

MIP_MAXCUTPASS_TREE (integer)

This controls the number passes to generate cuts on the child nodes. Each of these passes will be followed by a reoptimization and a new batch of cuts will be generated at the new solution.

(default = 2)

MIP_ADDCUTPER (*real*)

This determines how many constraint cuts can be added as a percentage of the number of original rows in an integer programming model.

(*default = 0.75*)

MIP_ADDCUTPER_TREE (*real*)

This determines how many constraint cuts can be added at child nodes as a percentage of the number of original rows in an integer programming model.

(*default = 0.5*)

MIP_MAXNONIMP_CUTPASS (*integer*)

This controls the maximum number of passes allowed in cut-generation that does not improve the current relaxation.

(*default = 3*)

MIP_CUTLEVEL_TOP (*integer*)

This controls the combination of cut types to try at the root node when solving a MIP. Bit settings are used to enable the various cut types.

(*default = 6142*)

- +2 GUB cover
- +4 Flow cover
- +8 Lifting
- +16 Plant location
- +32 Disaggregation
- +64 Knapsack cover
- +128 Lattice
- +256 Gomory
- +512 Coefficient reduction
- +1024 GCD
- +2048 Obj integrality
- +4096 Basis Cuts
- +8192 Cardinality Cuts
- +16384 Disjunk Cuts

MIP_CUTLEVEL_TREE (*integer*)

This controls the combination of cut types to try at child nodes in the B&B tree when solving a MIP.

(*default = 4094*)

- +2 GUB cover
- +4 Flow cover
- +8 Lifting
- +16 Plant location
- +32 Disaggregation
- +64 Knapsack cover
- +128 Lattice
- +256 Gomory
- +512 Coefficient reduction

+1024 GCD
+2048 Obj integrality
+4096 Basis Cuts
+8192 Cardinality Cuts
+16384 Disjunk Cuts

MIP_CUTTILMIM (integer)

This controls the total time to be spent in cut generation throughout the solution of a MIP. The default value is -1, indicating that no time limits will be imposed when generating cuts.

(default = -1)

MIP_CUTDEPTH (integer)

This controls a threshold value for the depth of nodes in the B&B tree, so cut generation will be less likely at those nodes deeper than this threshold.

(default = 8)

MIP_CUTFREQ (integer)

This controls the frequency of invoking cut generation at child nodes. The default value is 10, indicating that the MIP solver will try to generate cuts at every 10 nodes.

(default = 10)

MIP_HEULEVEL (integer)

This specifies the heuristic used to find the integer solution. Possible values are: 0: No heuristic is used. 1: A simple heuristic is used. Typically, this will find integer solutions only on problems with a certain structure. However, it tends to be fast. 2: This is an advanced heuristic that tries to find a "good" integer solution fast. In general, a value of 2 seems to not increase the total solution time and will find an integer solution fast on many problems. A higher value may find an integer solution faster, or an integer solution where none would have been found with a lower level. Try level 3 or 4 on "difficult" problems where 2 does not help. Higher values cause more time to be spent in the heuristic. The value may be set arbitrarily high. However, >20 is probably not worthwhile. [MIP_HEUMINTILMIM](#) controls the time to be spent in searching heuristic solutions.

(default = 3)

MIP_CUTOFFOBJ (real)

If this is specified, then any part of the branch-and-bound tree that has a bound worse than this value will not be considered. This can be used to reduce the running time if a good bound is known.

(default = 1e30)

MIP_USECUTOFFOBJ (integer)

This is a flag for the parameter [MIP_CUTOFFOBJ](#). If you do not want to lose the value of the parameter [MIP_CUTOFFOBJ](#), this provides an alternative to disabling the cutoff objective.

(default = 1)

- 0 Do not use current cutoff value
- 1 Use current cutoff value

MIP_STRONGBRANCHLEVEL (integer)

This specifies the depth from the root in which strong branching is used. The default value of 10 means that strong branching is used on a level of 1 to 10 measured from the root. Strong branching finds the real bound for branching on a given variable, which, in most cases, requires a solution of a linear program and may therefore also be quite expensive in computing time. However, if used on nodes close to the root node of the tree, it also gives a much better bound for that part of the tree and can therefore reduce the size of the branch-and-bound tree.

(default = 10)

MIP_TREEREORDERLEVEL (*integer*)

This specifies the tree reordering level.

(default = 10)

MIP_BRANCHDIR (*integer*)

This specifies the direction to branch first when branching on a variable.

(default = 0)

- 0 Solver decides
- 1 Always branch up first
- 2 Always branch down first

MIP_TOPOPT (*integer*)

This specifies which optimization method to use when there is no previous basis.

(default = 0)

- 0 Solver decides
- 1 Use primal method
- 2 Use dual simplex
- 3 Use barrier solver

MIP_REOPT (*integer*)

This specifies which optimization method to use when doing reoptimization from a given basis.

(default = 0)

- 0 Solver decides
- 1 Use primal method
- 2 Use dual simplex
- 3 Use barrier solver

MIP_SOLVERTYPE (*integer*)

This specifies the optimization method to use when solving mixed-integer models.

(default = 0)

- 0 Solver decides
- 1 Use B&B only
- 2 Use Enumeration and Knapsack solver only

MIP_KEEPIINMEM (*integer*)

If this is set to 1, the integer pre-solver will try to keep LP bases in memory. This typically gives faster solution times, but uses more memory. Setting this parameter to 0 causes the pre-solver to erase bases from memory.

(default = 1)

- 0 Do not keep LP bases in memory
- 1 Keep LP bases in memory

MIP_BRANCHRULE (*integer*)

This specifies the rule for choosing the variable to branch on at the selected node.

(default = 0)

- 0 Solver decides

- 1 Basis rounding with pseudo reduced costs
- 2 Maximum infeasibility
- 3 Pseudo reduced costs only

MIP_REDCOSTFIX_CUTOFF (*real*)

This specifies the cutoff value as a percentage of the reduced costs to be used in fixing variables when using the reduced cost fixing heuristic.

(default = 0.9)

MIP_ADDCUTOBJTOL (*real*)

This specifies the minimum required improvement in the objective function for the cut generation phase to continue generating cuts.

(default = 1.5625e-5)

MIP_HEUMINTIMLIM (*integer*)

This specifies the minimum time in seconds to be spent in finding heuristic solutions to the MIP model. [MIP_HEULEVEL](#) controls the heuristic used to find the integer solution.

(default = 0)

MIP_BRANCH_PRIO (*integer*)

This controls how variable selection priorities are set and used.

(default = 0)

- 0 If the user has specified priorities then use them Otherwise let LINDO API decide
- 1 If user has specified priorities then use them Overwrite users choices if necessary
- 2 If user has specified priorities then use them Otherwise do not use any priorities
- 3 Let LINDO API set the priorities and ignore any user specified priorities
- 4 Binaries always have higher priority over general integers

MIP_SCALING_BOUND (*integer*)

This controls the maximum difference between the upper and lower bounds of an integer variable that will enable the scaling in the simplex solver when solving a subproblem in the branch-andbound tree.

(default = 10000)

MIP_PSEUDOCOST_WEIGHT (*real*)

This specifies the weight in pseudocost computations for variable selection.

(default = 1.5625e-05)

MIP_LBIGM (*real*)

This refers to the Big-M value used in linearizing nonlinear expressions.

(default = 10000)

MIP_DELTA (*real*)

This refers to a near-zero value used in linearizing nonlinear expressions.

(default = 1e-6)

MIP_DUAL_SOLUTION (*integer*)

This flag controls whether the dual solution to the LP relaxation that yielded the optimal MIP solution will be computed or not.

(default = 0)

- 0 Do not calculate dual solution for LP relaxation

1 Calculate dual solution for LP relaxation

MIP_BRANCH_LIMIT (*integer*)

This is the limit on the total number of branches to be created during branch-and-bound. The default value is -1, which means no limit is imposed. If the branch limit is reached and a feasible integer solution was found, it will be installed as the incumbent (best known) solution.

(default = -1)

MIP_ITRLIM (*integer*)

This is the iteration limit for branch-and-bound. The default value is .1, which means no iteration limit is imposed. If the iteration limit is reached and a feasible integer solution was found, it will be installed as the incumbent (best known) solution.

(default = -1)

MIP_AGGCUTLIM_TOP (*integer*)

This specifies an upper limit on the number of constraints to be involved in the derivation of an aggregation cut at the root node. The default is .1, which means that the solver will decide.

(default = -1)

MIP_AGGCUTLIM_TREE (*integer*)

This specifies an upper limit on the number of constraints to be involved in the derivation of an aggregation cut at the tree nodes. The default is .1, which means that the solver will decide.

(default = -1)

MIP_ANODES_SWITCH_DF (*integer*)

This specifies the threshold on active nodes for switching to depth-first search rule.

(default = 50000)

MIP_ABSOPTTOL (*real*)

This is the MIP absolute optimality tolerance. Solutions must beat the incumbent by at least this absolute amount to become the new, best solution.

(default = 0)

MIP_MINABSOBJSTEP (*real*)

This specifies the value to update the cutoff value each time a mixed integer solution is found.

(default = 0)

MIP_PSEUDOCOST_RULE (*integer*)

This specifies the rule in pseudocost computations for variable selection.

(default = 0)

MIP_USE_ENUM_HEU (*integer*)

This specifies the frequency of enumeration heuristic.

(default = 4)

MIP_PRELEVEL_TREE (*integer*)

This controls the amount and type of MIP pre-solving at tree nodes.

(default = 174)

- +2 Simple pre-solving
- +4 Probing
- +8 Coefficient reduction
- +16 Elimination

- +32 Dual reductions
- +64 Use dual information
- +128 Binary row presolving
- +256 Row aggregation
- +512 Maximum pass

MIP_REDCOSTFIX_CUTOFF_TREE (*real*)

This specifies the cutoff value as a percentage of the reduced costs to be used in fixing variables when using the reduced cost fixing heuristic at tree nodes.

(default = 0.9)

MIP_USE_INT_ZERO_TOL (*integer*)

This flag controls if all MIP calculations would be based on the integrality tolerance specified by [MIP_INTTOL](#).

(default = 0)

- 0 Do not base MIP calculations on MIP_INTTOL
- 1 Base MIP calculations on MIP_INTTOL

MIP_USE_CUTS_HEU (*integer*)

This flag controls if cut generation is enabled during MIP heuristics. The default is -1 (i.e. the solver decides).

(default = -1)

- 1 Solver decides
- 0 Do not use cut heuristic
- 1 Use cut heuristic

MIP_BIGM_FOR_INTTOL (*real*)

This value specifies the threshold for which the coefficient of a binary variable would be considered as big-M (when applicable).

(default = 1e8)

MIP_STRONGBRANCHDONUM (*integer*)

This value specifies the minimum number of variables, among all the candidates, to try the strong branching on.

(default = 3)

MIP_MAKECUT_INACTIVE_COUNT (*integer*)

This value specifies the threshold for the times a cut could remain active after successive reoptimization during branch-and-bound. If the count is larger than the specified level the solver will inactive the cut.

(default = 10)

MIP_PRE_ELIM_FILL (*integer*)

This is a nonnegative value that controls the fill-in introduced by the eliminations during pre-solve. Smaller values could help when the total nonzeros in the presolved model is significantly more than the original model.

(default = 100)

OPTTOL (*real*)

This value is the GOP optimality tolerance. Solutions must beat the incumbent by at least this amount to become the new best solution.

(default = 1e-6)

FLTTOL (*real*)

This value is the GOP floating-point tolerance. It specifies the maximum rounding errors in the floating-point computation.

(default = 1e-10)

BOXTOL (*real*)

This value specifies the minimal width of variable intervals in a box allowed to branch.

(default = 1e-6)

WIDTOL (*real*)

This value specifies the maximal width of variable intervals for a box to be considered as an incumbent box containing an incumbent solution. It is used when [MAXWIDMD](#) is set at 1.

(default = 1e-4)

DELTATOL (*real*)

This value is the delta tolerance in the GOP convexification. It is a measure of how closely the additional constraints added as part of convexification should be satisfied.

(default = 1e-7)

BNDLIM (*real*)

This value specifies the maximum magnitude of variable bounds used in the GOP convexification. Any lower bound smaller than the negative of this value will be treated as the negative of this value. Any upper bound greater than this value will be treated as this value. This helps the global solver focus on more productive domains.

(default = 1e10)

TIMLIM (*integer*)

This is the time limit in seconds for GOP branch-and-bound.

(default = GAMS ResLim)

OPTCHKMD (*integer*)

This specifies the criterion used to certify the global optimality. When this value is 0, the absolute deviation of objective lower and upper bounds should be smaller than [OPTTOL](#) at the global optimum. When its value is 1, the relative deviation of objective lower and upper bounds should be smaller than [OPTTOL](#) at the global optimum.

(default = 1)

BRANCHMD (*integer*)

This specifies the direction to branch first when branching on a variable. The branch variable is selected as the one that holds the largest magnitude in the measure.

(default = 5)

- 0 Absolute width
- 1 Locally relative width
- 2 Globally relative width
- 3 Globally relative distance from the convex minimum to the bounds
- 4 Absolute violation between the function and its convex envelope at the convex minimum
- 5 Relative violation between the function and its convex envelope at the convex minimum

MAXWIDMD (*integer*)

This is the maximum width flag for the global solution. The GOP branch-and-bound may continue contracting a box with an incumbent solution until its maximum width is smaller than [WIDTOL](#).

(default = 0)

- 0 The maximum width criterion is suppressed
- 1 The maximum width criterion is performed

PRELEVEL (integer)

This controls the amount and type of GOP pre-solving. The default value is: $30 = 2+4+8+16$ meaning to do all of the below options.

(default = 30)

- +2 Initial local optimization
- +4 Initial linear constraint propagation
- +8 Recursive linear constraint propagation
- +16 Recursive nonlinear constraint propagation

POSTLEVEL (integer)

This controls the amount and type of GOP post-solving. The default value is: $6 = 2+4$ meaning to do both of the below options.

(default = 6)

- +2 Apply LSgetBestBound
- +4 Reoptimize variable bounds

BBSRCHMD (integer)

This specifies the node selection rule for choosing between all active nodes in the GOP branch-and-bound tree when solving global optimization programs.

(default = 1)

- 0 Depth first search
- 1 Choose node with worst bound

DECOMPPTMD (integer)

This specifies the decomposition point selection rule. In the branch step of GOP branch-and-bound, a branch point M is selected to decompose the selected variable interval $[Lb, Ub]$ into two subintervals, $[Lb, M]$ and $[M, Ub]$.

(default = 1)

- 0 Mid-point
- 1 Local minimum or convex minimum

ALGREFORMMD (integer)

This controls the algebraic reformulation rule for a GOP. The algebraic reformulation and analysis is very crucial in building a tight convex envelope to enclose the nonlinear/nonconvex functions. A lower degree of overestimation on convex envelopes helps increase the convergence rate to the global optimum.

(default = 18)

- +2 Rearrange and collect terms
- +4 Expand all parentheses
- +8 Retain nonlinear functions
- +16 Selectively expand parentheses

RELBRNDMD (integer)

This controls the reliable rounding rule in the GOP branch-and-bound. The global solver applies many suboptimizations to estimate the lower and upper bounds on the global optimum. A rounding error or numerical instability could unintentionally cut off a good solution. A variety of reliable approaches are available to improve the precision.

(default = 0)

- +2 Use smaller optimality or feasibility tolerances and appropriate presolving options
- +4 Apply interval arithmetic to reverify the solution feasibility

USEBNDLIM (*integer*)

This value is a flag for the parameter [BNDLIM](#).

(*default = 2*)

- 0 Do not use the bound limit on the variables
- 1 Use the bound limit right at the beginning of global optimization
- 2 Use the bound limit after the initial local optimization if selected

BRANCH_LIMIT (*integer*)

This is the limit on the total number of branches to be created during branch-and-bound in GOP tree. The default value is -1, which means no limit is imposed. If the branch limit is reached and a feasible solution was found, it will be installed as the incumbent (best known) solution.

(*default = -1*)

CORELEVEL (*integer*)

This controls the strategy of GOP branch-and-bound procedure.

(*default = 14*)

- +2 LP convex relaxation
- +4 NLP solving
- +8 Box Branching

OPT_MODE (*integer*)

This specifies the mode for GOP optimization.

(*default = 1*)

HEU_MODE (*integer*)

This specifies the heuristic used in the global solver to find good solution. Typically, if a heuristic is used this will put more efforts in searching for good solutions, and less in bound tightening.

(*default = 0*)

- 0 No heuristic is used
- 1 A simple heuristic is used

SUBOUT_MODE (*integer*)

This is a flag indicating whether fixed variables are substituted out of the instruction list used in the global solver.

(*default = 1*)

- 0 Do not substitute out fixed variables
- 1 Substitute out fixed variables

LSOLBRANLIM (*integer*)

This value controls the branch limit until finding a new nonlinear solution since the last nonlinear solution is found. The default value is -1, which means no branch limit is imposed.

(*default = -1*)

CHECKRANGE (*string*)

If this option is set, Lindo calculates the feasible range (determined by an upper and lower bound) for every variable in each equation while all other variables are fixed to their level. If set, the value of this option defines the name of the GDX file where the results are written to. For every combination of equation- and variable block there will be one symbol in the format *EquBlock_VarBlock(equ_Ind_1, ..., equ_Ind_M, var_Ind_1, ..., var_Ind_N, directions)*.

(default = *range.gdx*)

USEGOP (*integer*)

This value determines whether the global optimization will be used.

(default = 1)

0 Do not use global optimization

1 Use global optimization

WRITEMPI (*string*)

If this option is set, Lindo write an MPI file of processed model. If set, the value of this option defines the name of the MPI file.