

Models and Their Roles Or

"A Model is a Model is a Model*

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Aachen, July 2012

* Freely adapted from the poetry of Gertrude Stein, 1874-1946, American writer





Agenda

What is GAMS
What is a GAMS model
Roles of a Model
Market Demands and Challenges



Agenda

What is GAMS
What is a GAMS model
Roles of a Model
Market Demands and Challenges

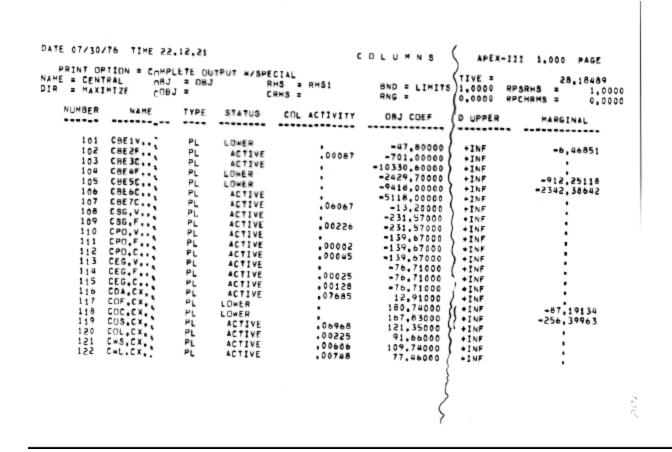


Matrix Generator

```
CUMPPB
  IF (X(248), LT'0,5, AND, X(248), GT., 00) Y(248) 12(2
Y(2491'X(249)
                                                                        CUMPIS
  IF (X(249), LT_0,5, AND, X(249), GT., OO) Y(249) 17(249, 1) +(1+X(249))
Y(250) X(250)
                                                                        COMNEI
  IF (x(250),LT,0,5,AND,x(250),GT,,00) Y(250)'Z(250,1)*(1+x(250))
Y(251)1X(251)
                                                                        CUMDNE
  1F (X(251), LT 0,5, AND, X(251), GT., 00) Y(251) (2(251,1)
Y(252)1X(252)
                                                                        CUMTED
  IF (X(252), LT 0, 5, AND, X(252), GT., 00) Y(252) (252, 1)
Y(253) 1X(253)
                                                                        CUMTER
  IF (X(253),LT 0.5,AND,X(253),GT..00) Y(253) 7(253,1) +(1+X(253))
                                                                        COMPOU
  IF (X(254), LT 0.5, AND, X(254), GT., OO) Y(254) Z(254, 1) +(1+X(254))
Y(255) 1Y(266) +Y(267)
                                                                        CUMPIV
Y (256) 1X (256)
                                                                        CCMLCT
  IF (X(256), LT 0,5,4ND, X(256), GT, 00) Y(256) (Z(256,1) *(1+X(256))
Y(257) 1X(257)
                                                                        CUMLEG
  IF (X(257), LT 0.5, AND, X(257), GT, .00) Y(257) Z(257, 1) *C1+X(257))
Y(258) 1X(258)
                                                                        CLMDLS
  IF (X(258),LT,0,5,AND,X(258),GT,.00) Y(258) Z(258,1) +(1+X(258))
Y(259) 1x(259)
                                                                        CU 6-
  IF (X(259), LT 0,5, AND, X(259), GT, .00) Y(259) Z(259, 1) *(1+X(259))
Y(260) 1X(260)
  IF (x(260).LT_0.5.AND.x(260).GT..OD) Y(250) Z(260.1)*(1+X(260))
Y(261) Y(63)
                                                                        EXPORT
A(595) x(595)
                                                                        NETDII
  IF (x(262), LT 0,5, AND, x(262), GT,, 00) ((262) 2(262, 1) *(1+x(262))
Y(263) X(263)
                                                                        NETDFI
  IF (X(263),LT,0,5,AVD,X(263),GT,,00) ((263) Z(263,1)*(1*X(263))
A (594) x (594)
                                                                        MHKRMT
  IF (x(264),LT_0,5,AND,x(264),GT,,00) Y(264) Z(264,1) = (1+x(264))
Y (265) 1 X (265)
                                                                        METTRN
  IF (X(265), LT_C, 5, AND, K(265), GT, .00) Y(265) Z(265, 1)*(1-X(265))
                                                                        OFFCUR
  IF (x(266),LT'C,5,AND,x(266),GT,,00) Y(266) Z(266,1)=(1-x(266))
                                                                        OFFEAR
```



MPS Output





Algebraic Modeling Languages

What's that?

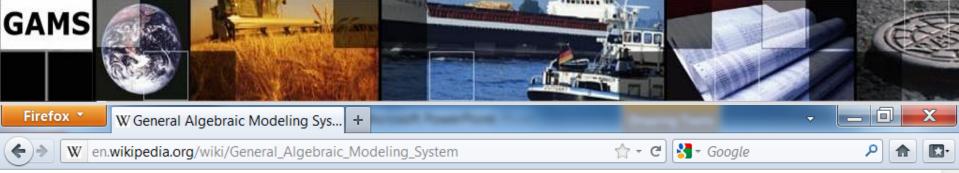
http://en.wikipedia.org/wiki/Algebraic_modeling_language

- High-level computer programming languages for the formulation of complex mathematical optimization problems
- Notation similar to algebraic notation: Concise and readable definition of problems in the domain of optimization
- Do not solve problems directly, but ready-for-use links to state-ofthe-art algorithms
- → Simplified model building
- → Efficient solution process
- → Increased productivity











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General Algebraic Modeling System

From Wikipedia, the free encyclopedia

Article Talk

The General Algebraic Modeling System (GAMS) is a high-level modeling system for mathematical optimization. GAMS is designed for modeling and solving linear, nonlinear, and mixed-integer optimization problems. The system is tailored for complex, large-scale modeling applications and allows the user to build large maintainable models that can be adapted to new situations. The system is available for use on various computer platforms. Models are portable from one platform to another.

GAMS was the first algebraic modeling language (AML) and is formally similar to commonly used fourth-generation programming languages. [citation needed] GAMS contains an integrated development environment (IDE) and is connected to a group of third-party optimization solvers. Among these solvers are BARON, COIN solvers, CONOPT, CPLEX, DICOPT, GUROBI, MOSEK, SNOPT, and XPRESS.

GAMS facilitates the users to implement a sort of hybrid algorithms combining different solvers in a seamless way. Models are described in concise algebraic statements which are easy to read, both for humans and machines. GAMS is among the most popular input formats for the

NEOS Server for Optimization ©. Although initially designed for applications related to economics and management science, it has a large community of users from various backgrounds of engineering and science.

GAMS

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Developer(s)	GAMS Development Corporation 습
Stable release	23.7.3 / August 23, 2011
Development status	Active
Platform	Cross-platform
Туре	Algebraic Modeling Language (AML)

License Proprietary

Website GAMS USA 🚱

GAMS Germany 🚱



2 Timeline 3 Background



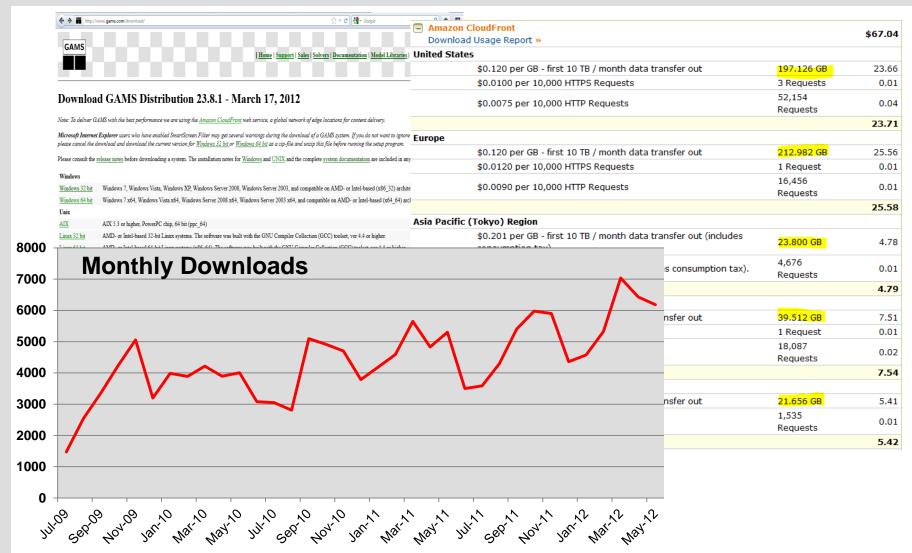
General Algebraic Modeling System

- Roots: World Bank, 1976
- Went commercial in 1987
- GAMS Development Corporation (Washington, Houston)
- GAMS Software GmbH (Cologne, Braunschweig)
- Broad academic & commercial user community and network





Monthly System Downloads



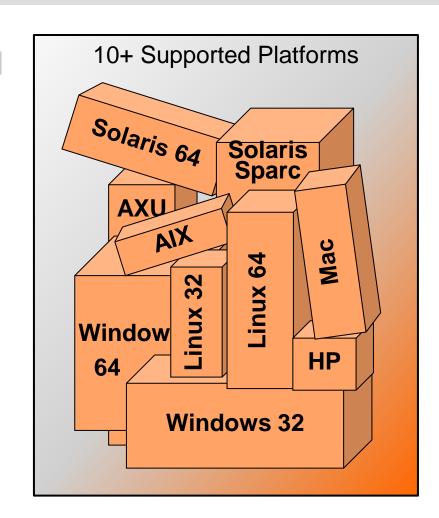


- Balanced mix of declarative and procedural elements
- Platform independence
- Hassle-free switch of solution methods
- Open architecture and interfaces to other systems

- Declarative: Model Algebra
- Procedural: Programming Flow Control Features
 - Loop, For, While, Repeat
 - If, else, else...
 - Macros
 - Access to external programs/libraries
 - •

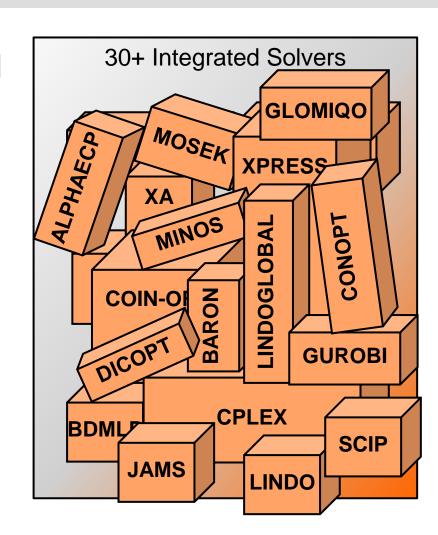


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- ASCII
- Gams Data eXchange (Binary)
 - MS Excel, MS Access
 - Databases
 - Matlab, R,
- API's
- Component Libraries
- .NET Integration (Alpha)



Independence of

- Model and data
- Model and solution methods (solver)
- Model and operating system
- Model and user interface

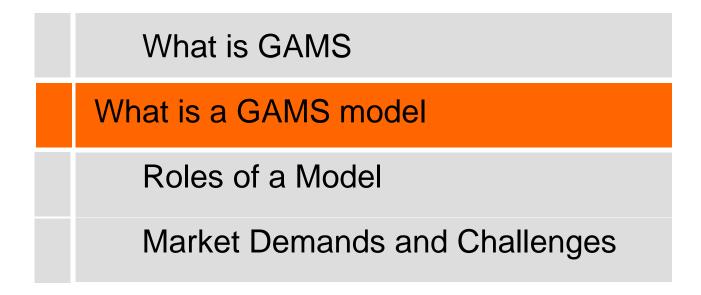


→ Models benefit from

- Advancing hardware
- Enhanced / new solver technology
- Improved / upcoming interfaces to other systems

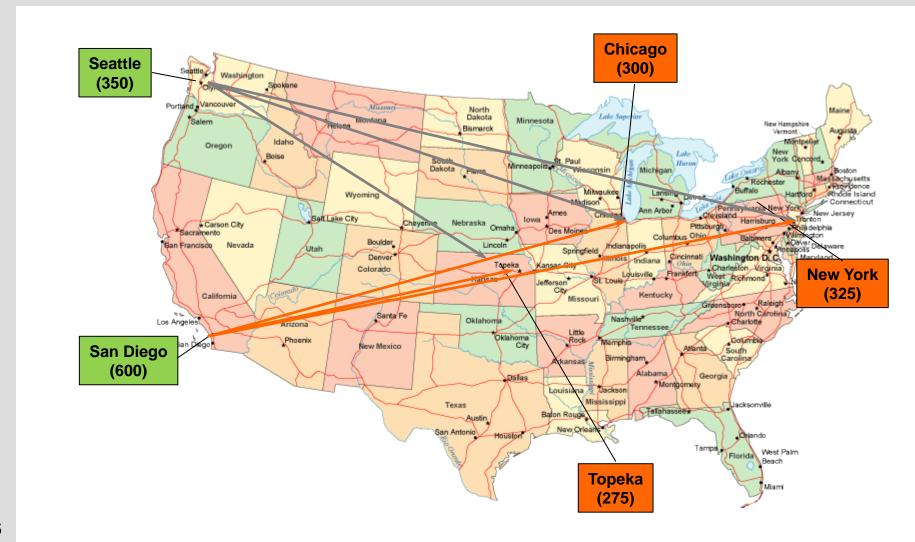


Agenda





A Simple Example: Transportation Model





A Simple Example: Algebra

Minimize Transportation cost

subject to Demand satisfaction at markets

Supply constraints



A Simple Example: Declarative Model

```
C:\Users\Franz\Documents\gamsdir\projdir\trnsport.gms
                                                                                  - O X
data.inc trnsport.gms trnsport.lst
   Sets
              canning plants
             markets;
   Parameters a(i) capacity of plant i in cases
              b(i) demand at market j in cases
              d(i,i) distance in thousands of miles
                      freight in dollars per case per thousand miles
              c(i,j) transport cost in thousands of dollars per case ;
   Variables
             x(i,j) shipment quantities in cases
                     total transportation costs in thousands of dollars ;
   Positive Variable x :
                   define objective function
  Equations cost
              supply(i) observe supply limit at plant i
              demand(j) satisfy demand at market j ;
          z = e = sum((i,j), c(i,j)*x(i,j));
   cost ..
   supply(i) .. sum(j, x(i,j)) = l = a(i);
   demand(j) .. sum(i, x(i,j)) = g = b(j);
   Model transport /all/;
       1: 3 Modified
                        Insert
```



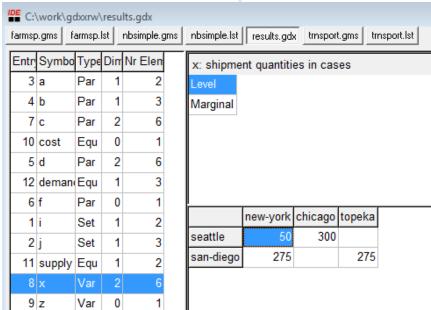
A Simple Example: Model Data

```
C:\Users\Franz\Documents\gamsdir\projdir\data.inc
                                                                                  _ <u>-</u>
data.inc trnsport.gms trnsport.lst
   sets i / seattle, san-diego /,
        j / new-york, chicago, topeka / ;
   Parameters
       a(i)/
               seattle
                            350
               san-diego 600 /,
      b(j)/ new-vork 325
                chicago
                           300
                topeka 275 /;
   Table d(i,j) distance in thousands of miles
                       new-york
                                      chicago
                                                topeka
         seattle
                          2.5
                                        1.7
                                                     1.8
         san-diego
                          2.5
                                                    1.4 :
                                       1.8
   Scalar f freight in dollars per case per thousand miles /90/;
      11: 44
                       Insert
```



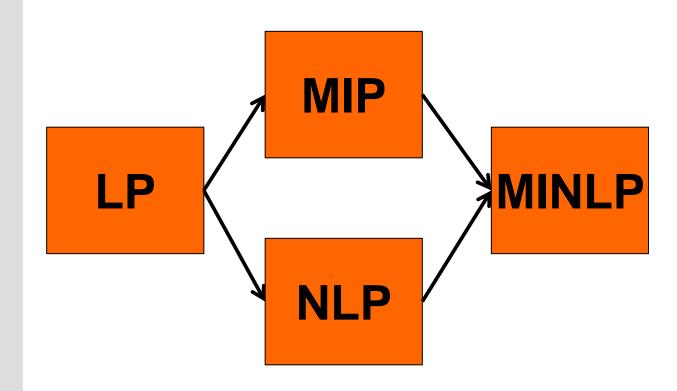
A Simple Example: Results

Compilation Equation Listing SOLVE transport Usin **** REPORT SUMMARY : NONOPT 0 INFEASIBLE Column Listing SOLVE transport Usin 0 UNBOUNDED Model Statistics SOLVE transport Using GAMS Rev 238 WEX-WEI 23.8.1 x86 64/MS Windows 03/29/12 13:28:06 Page 6 Solution Report SOLVE transport Usin A Transportation Problem (TRNSPORT, SEQ=1) Execution Execution 68 VARIABLE z.L 153.675 total transportation costs in thousands of dollars 68 VARIABLE x.L shipment quantities in cases new-york chicago topeka seattle 50.000 300.000 san-diego 275.000 275.000





A Simple Example: Modifications





A Simple Example: Minimum Shipment

- Extension: Minimum Shipment
 - Ship at least 100 units or don't ship
- Continuous variable x(i,j)
- Binary variable ship(i,j)
- Coupling constraints:
 - if $ship = 1 \rightarrow x \ge 100$: $x \ge 100 * ship$
 - If ship = $0 \rightarrow x = 0$: $x \le \text{bigM} * \text{ship}$

A Simple Example: Min/Max Shipments

```
model m2 min shipments / all /;
solve m2 using mip minimizing z;
rep1(i,j,'mip') = x.l(i,j);
rep2('mip') = z.l;

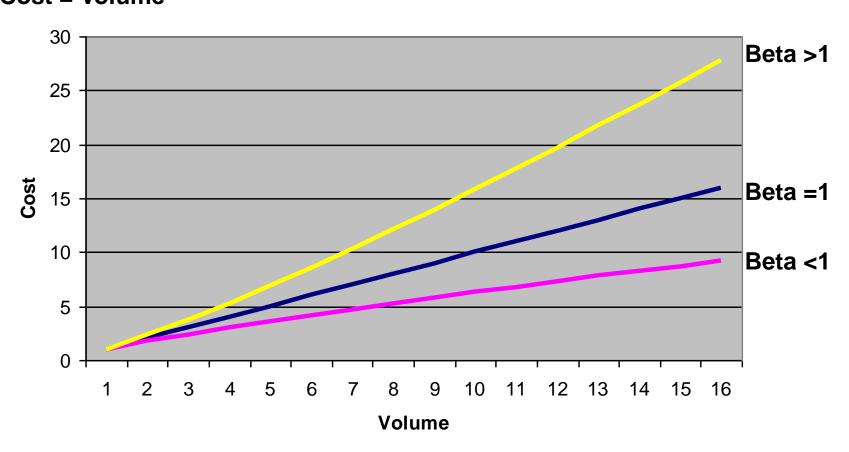
option mip=coincbc
solve m2 using mip minimizing z;
rep1(i,j,'mip-coincbc') = x.l(i,j);
rep2('mip-coincbc') = z.l;
display rep1, rep2;
```

```
100 PARAMETER rep1 Shipments between plants and markets
                           1p
                                      mip mip-coinc~
seattle .new-york
                       50.000
                                              300.000
seattle .chicago
                      300.000
                                  300.000
                                  325.000
                                              325.000
san-diego.new-york
                      275.000
san-diego.topeka
                      275.000
                                  275.000
                                              275.000
       100 PARAMETER rep2 Objective value
           153.675,
                       mip
                                  153.675.
                                              mip-coincbc 153.675
```



A Simple Example: Economy of Scales









* nonlinear cost



equation nlcost nonlinear cost function;







A Simple Example: Nonlinear Costs (NLP)

```
scalar beta;
nlcost.. z = e = sum((i,j), c(i,j)*x(i,j)**beta);
model m3 / transport -cost +nlcost /;
beta = 1.5;
solve m3 using nlp minimizing z;
repl(i,j,'nlp-convex') = x.l(i,j);
rep2('nlp-convex')
                       = z.1;
beta = 0.6:
solve m3 using nlp minimizing z;
repl(i,j,'nlp-concave') = x.l(i,j);
rep2('nlp-concave')
                        = z.1:
option nlp=baron;
solve m3 using nlp minimizing z;
rep1(i,j,'nlp-baron') = x.l(i,j);
rep2('nlp-baron')
                       = z.1:
display rep1, rep2;
```

```
127 PARAMETER rep1 Shipments between plants and markets
                           lp nlp-convex nlp-conca~
                                                       nlp-baron
seattle .new-york
                       50.000
                                  142.384
                      300.000
                                  130.930
seattle .chicago
                                              300.000
                                                          300.000
seattle .topeka
                                  76.686
                      275.000
                                  182.616
                                              325.000
                                                          325.000
san-diego.new-vork
                                  169.070
san-diego.chicago
san-diego.topeka
                      275.000
                                  198.314
                                              275.000
                                                          275.000
        127 PARAMETER rep2 Objective value
            153.675.
                        nlp-convex 1983.555,
lp
                                                 nlp-concave
                                                              15.585
nlp-baron
             15.585
```



A Simple Example: MIP and Nonlinear

```
* min/max and nonlinear objective
model m4 / m3 +minship +maxship/;
option minlp=baron;
solve m4 using minlp minimizing z;
repl(i,j,'minlp-bar') = x.l(i,j);
rep2('minlp-bar')
                      = z.1:
option minlp=lindoglobal;
solve m4 using minlp minimizing z;
repl(i,j,'minlp-lin') = x.l(i,j);
rep2('minlp-lin') = z.1;
display rep1,rep2;
```

```
142 PARAMETER rep1 Shipments between plants and markets
                                       mip mip-coinc~ nlp-convex nlp-conca~
seattle .new-york
                        50.000
                                                           142.384
seattle .chicago
                       300.000
                                   300.000
                                               300.000
                                                           130.930
                                                                       300.000
seattle .topeka
                                                            76.686
san-diego.new-york
                       275.000
                                   325.000
                                               325.000
                                                           182.616
                                                                       325.000
san-diego.chicago
                                                           169.070
san-diego.topeka
                       275.000
                                   275.000
                                               275.000
                                                           198.314
                                                                       275.000
                     nlp-baron
                                 minlp-bar
                                             minlp-lin
seattle .chicago
                       300.000
                                   300.000
                                               300.000
                       325.000
                                   325.000
                                               325.000
san-diego.new-vork
san-diego.topeka
                       275.000
                                   275.000
                                               275.000
        142 PARAMETER rep2 Objective value
             153.675,
                                     153.675,
                                                  mip-coincbc 153.675
nlp-convex 1983.555,
                         nlp-concave
                                                  nlp-baron
                                                                15.585
minlp-bar
              15.585,
                         minlp-lin
                                       15.585
```



Agenda

What is GAMS
What is a GAMS model
Roles of a Model
Market Demands and Challenges



What is a Model?

- List of equations
 - Mathematical Programming (MP) model
- Collection of several intertwined (MP) models
 - Data preparation and calibration
 - "Solution" module
 - Reporting module
- → Categorization of models by answering: Who is the user of a model?



Academic Researcher

- Most of model source is algebra
- Declarative modeling
- Performance of the solver is important
- Set of (benchmark) problem instances
- Taste (Syntax, development environment, solver,...)
- Data in most cases less important
- No maintenance issues



Consultants

- Model is tool for problem analysis
- Only a small fraction of model source is (equation) algebra
- User: Domain & modeling expert (not necessary the same person)
- Living model (changes with the problem), lifecycle: at least 10 years
- Technology change (platform, solver, ...)



End-User (Black Box Models)

- Innocent user
- Bulletproof optimization application
- No failures (e.g. no infeasible models)
- Model embedded in larger systems
- Optimization
 - takes longer than one is willing to wait
 - will eventually fail
- Application
 - Real time
 - Always needs a solution



Communication Vehicle

- Defining scope of a (part of a) project/model
- IT, analysts, managers, model builders have different views
- Misunderstandings common with verbal descriptions
- Use a model to define the scope
- Requirements for such a model
 - Rapid prototyping
 - Standard I/O interface (Excel)



Analytic Framework

- Optimization models do not allow for any type of vagueness
 - Input data requirements
 - Objectives and constraints
 - Results
- Misunderstandings result in failure of the model
 - Compilation/execution errors
 - Infeasible/unbounded MP models
- Model as a contract



Model as a Contract

- Good models do not rely on contract (input data)
- Input Module (handles bad data)
 - Simple error checks
 - Analyzing and reporting complex data problems
- Good models (modeling systems) provide access to results via independent result analyzers for non model experts
- Analytic framework helps to define a result metric
 - e.g. violations of soft constraints



Cost Saver

- Most convincing and obvious reason for using an optimization model
- Science of better (INFORMS)
- Often exaggerated/difficult to estimate
- More reasons:
 - Institutionalize personal knowledge
 - Scientific foundation (economic models)
 - Get "fair" results (usually fails)



Model Roles over Time

Communication Vehicle

Analytic Framework

Cost Saver Lifecycle:

+15 Years

Time



CAPRI

The CAPRI (Common Agricultural Policy Regional Impact) **Modelling System**

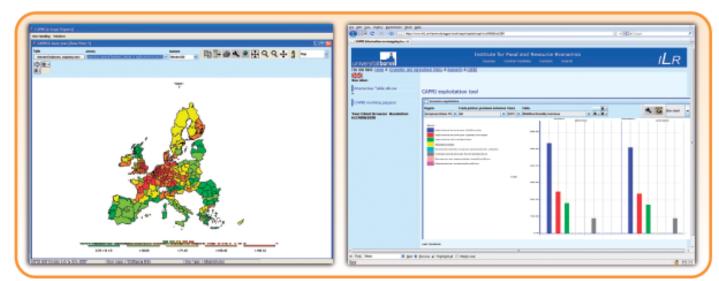
CAPRI is a global agricultural sector model powered by GAMS with focus on 27 countries of the European Union and Norway

- Global multi-commodity model for agricultural products in 18 trade blocks
- About 250 regions or even up to six farm types for each region
- Evaluates regional and aggregate impacts of trade policies on production, income, markets, trade and environment
- · Used by research institutions and EU Commission services

More information and an online exploitation tool at:

http://www.ilr1.uni-bonn.de/agpo/rsrch/capri/capri_e.htm Universitätbonn







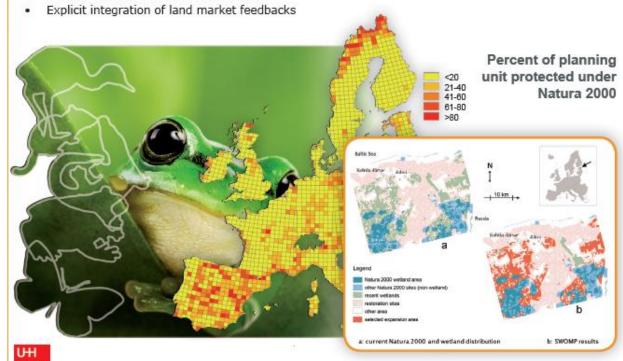
HABITAT

HABITAT – a reserve selection tool for European wetland biodiversity conservation

Developed at the University of Hamburg, the HABITAT model was explicitly designed for the special requirements for conservation planning on the European continent with its fragmented habitats and high human population density. It is based on principles of systematic conservation planning and economic theory. This central component of the systematic conservation planning philosophy aims at efficiency of resource use. The objective is to find a set of conservation sites that achieves a conservation target at minimum cost.

- A set-covering problem formulated as a mixed integer program to find the cost-efficient allocation of nature reserves
- · Integration of representation and persistence principles in the "conservation target" approach
- · Endogenous calculation of reserve sizes

Universität Hamburg



For further information about this application please contact Kerstin Jantke <kerstin.jantke@zmaw.de>,

Uwe Schneider <uwe.schneider@zmaw.de >, or visit: http://fnu.zmaw.de/

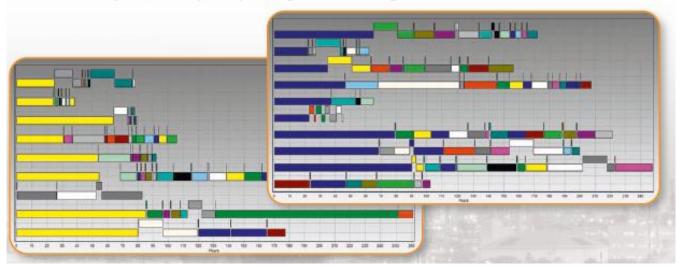


Scheduling and Planning at BASF

Scheduling and Planning at BASF

Close cooperation between logistics, information services and the scientific computing group of BASF, Prof. Dr. C. A. Floudas (Princeton University), Dr. A. V. Eremeev and Dr. P. A. Borisovski (Omsk Branch of Sobolev Institute of Mathematics SB RAS), SAP AG, and Mathesis GmbH led to a number of successfully deployed applications based on exact and hybrid optimization techniques. One of the results is a novel modeling approach of batch and continuous plants:

- · State-task network formulation resulting in mixed-integer linear program
- · Unit-specific, event-specific continuous-time formulations
- Hybrid methods and decomposition schemes to handle large instances
- Tight lower bounds derived from auxiliary models
- Implementation in GAMS with parallel GAMS/CPLEX
- · New interfacing technology and integration approaches to connect to SAP-APO
- . Used on a daily basis to improve planning and scheduling



Cutting Stock Optimization at GSE

Cutting Stock Optimization at GSE

GSE-TRIM is a fully integrated module of the ERP-System GSE-PPS for Cutting Stock Optimization. Close cooperation of our in-house specialists with scientists in the area of discrete optimization has led to a number of successfully deployed applications used by the paper industry. Exact and hybrid optimization techniques coded in GAMS and Fortran have been implemented in our software package GSE-TRIM.



Our clients in various Mid-European paper industry companies benefit from:

- Exact waste minimization in roll production
- Non-standard objective functions
- Considering detailed operational restrictions
- Multi-stage format production

Based on a daily basis GSE-TRIM improves our clients key indicators and has been proven very stable over 7 years.



DemandTec

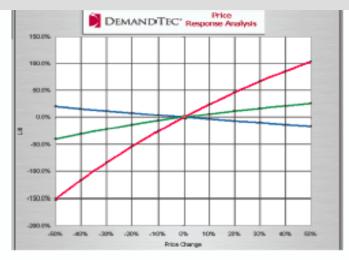
DemandTec Leverages GAMS to Drive Innovation in Retail and CPG Industries

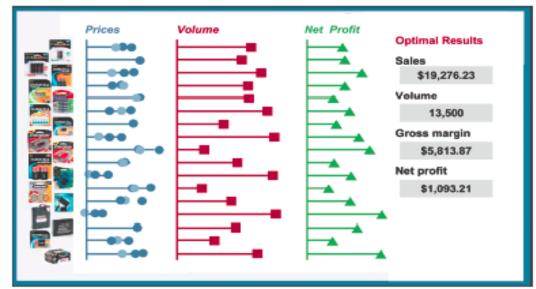
DemandTec uses sophisticated econometric and optimization models to help retailers and manufacturers make merchandising and marketing decisions based on a quantified understanding of consumer demand. DemandTec's applications are used to:

 Model price elasticity, cross-price elasticity, and other merchandising causals to predict and influence demand

given different merchandising conditions and strategies.

- Optimize prices and promotions to maximize sales, volume, or profit, while operating within the constraints of competitive pricing and other business rules.
- Accurately forecast the impact of merchandising strategies and tactics, taking into account cannibalization, halo effects, seasonality, trend, and other factors.







Agenda

What is GAMS
What is a GAMS model
Roles of a Model
Market Demands and Challenges



Market Demands

- Minimize risks for (new) clients / management
- Provide cutting edge technology
- Protect user investments



Minimize Risks

- Support rapid prototyping
- Increase productivity
- Deliver (expected) results
- Do not lock users into a certain environment



Provide cutting edge technology

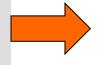
- Industry: Reliable, high performance system for developing and deploying optimization applications
- Academia (research tool):
 - New modeling paradigms (e.g. SDP, bilevel, SP,...)
 - Emerging solution technology (e.g. MPEC)
 - New computing environments



Bridging the Gap

GAMS serves both worlds (synergy):

- Large user base in industry and academia
- Dissemination of research ideas
- Challenging/relevant problems from industry



30% of revenue invested in research and product development



Protect User Investments

- Life time of a model: 15+ years:
 - New maintainer, platform, solver, user interface
 - Protection of investment in a model
- Blessing for the user (mostly) curse for developers
 - Old concepts in new situations
 - Example: GAMS listing file
 - Language additions have to be supported in the future
 - GAMS is conservative when it comes to syntax additions
- Danger of becoming a barrier for innovation



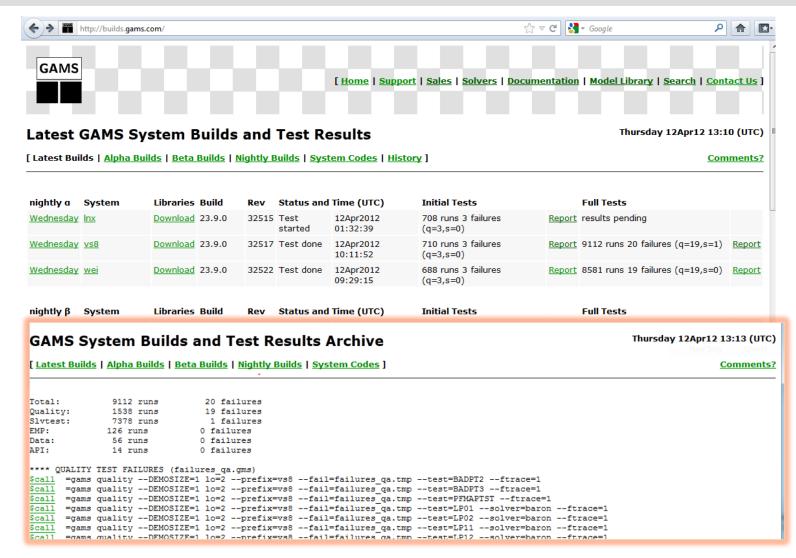
Quality Assurance at GAMS

Quality Test Models Library

- Include tests to verify proper behavior of the system
- More than 550 quality test models (included in the distribution), each containing numerous pass/fail tests
- Continuous quality improvement using automated and reproducible tests (> 20.000 solves for each platform)
- Automatic generated test summaries with different levels of information



Quality Assurance at GAMS



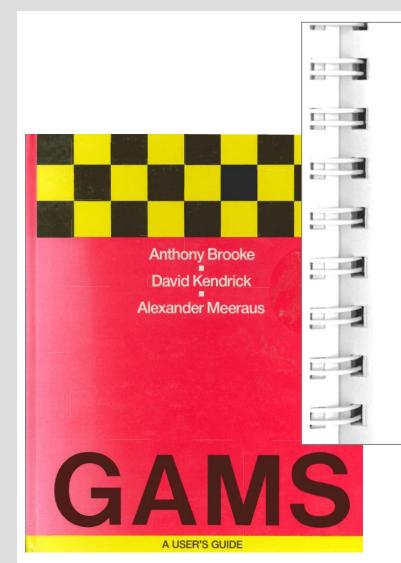


Client Model Testing

- Requires changes to the model of the clients to allow automated pass/failure tests
- Includes:
 - Ability to solve (= no bugs)
 - Returns the same solution back
 - Similar or better performance
- Gives clients assurance that their application will also work with new GAMS releases
- Improves communication between development team and clients (specific wishes)



Then ...



In Table 17.1 we list sizes and attributes of representative models that are "large" in the sense that they are near the limit of what is practical on a personal computer, along with the model generation time (GAMS) and solution time (solver), both in minutes. These examples were run on an 8 MHz AT with an 80287 coprocessor and 640K of RAM. The times shown are to give you a rough idea of what is possible: these are not precisely controlled benchmarks, and we have a host of performance improvements in mind for the near future.

Table 17.1: Problem Characteristics

Name	Number of Rows	Number of Columns	Number of Nonzeroes	Generation Time ^a	Solution Time ^a	Iterations	Solver
DINAMICO	318	425	4156	3.0	30.1	628	MINOS
SARF	532	542	3949	37.7	115.8	2775	MINOS
$FERTD^b$	458	2968	7252	11.4	28.3	1368	ZOOM
$CAMCGE^{c}$	243	280	1356	0.8	7.0	189	MINOS
$GANGES^d$	274	357	1405	1.8	7.3	187	MINOS
YEMCEM	168	258	953	0.9	7.6	600	ZOOM
$EGYPT^f$	281	618	3168	4.0	25.3	1551	ZOOM

^aMeasured in minutes.



^bThe problem is too big for MINOS. ZOOM was used instead.

^cA nonlinear problem. 63% of the non-zeroes are nonlinear.

^dA nonlinear problem. 58% of the non-zeroes are nonlinear.

^eA mixed binary problem, with 55 binary variables (solved with a relative termination criterion of 10%).

^fA linear problem, solved using XMP which is contained within ZOOM.



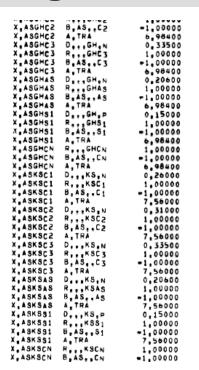
... and now

	Туре	s in 1988	s in 2008	Improvement Factor
camcge	NLP	468	0.031	15097
dinamico	LP	1986	0.125	15888
egypt*	MIP	1758	0.015	117200
fertd*	MIP	2382	0.062	38419
ganges	NLP	546	0.109	5009
sarf	LP	9210	0.139	66259
yemcem*	MIP	510	0.140	3643

^{*} MIP 1988 solver ZOOM, 2008 solver CPLEX



Change in Focus: Past





Computation

→ Users left out

Model

→ Users involved

Application

→Users hardly aware of model



Change in Focus: Now

```
C:\Users\Franz\Documents\gamsdir\projdir\trnsport.gms
data.inc trnsport.gms trnsport.lst
              canning plants
   Sets
              markets;
   Parameters a(i)
                     capacity of plant i in cases
               b(j)
                     demand at market j in cases
               d(i,j) distance in thousands of miles
                      freight in dollars per case per thousand miles
               c(i,j) transport cost in thousands of dollars per case ;
   Variables
             x(i,j) shipment quantities in cases
                       total transportation costs in thousands of dollars
   Positive Variable x :
                        define objective function
   Equations cost
              supply(i) observe supply limit at plant i
              demand(j) satisfy demand at market j ;
                  z = e = sum((i,j), c(i,j)*x(i,j));
   supply(i) .. sum(j, x(i,j)) = l = a(i);
   demand(j) .. sum(i, x(i,j)) = g = b(j);
   Model transport /all/ ;
   Sinclude data.inc
   c(i,j) = f * d(i,j) / 1000;
   Solve transport using lp minimizing z ;
```

Computation

Display x.1, x.m;

→ Users left out

Model

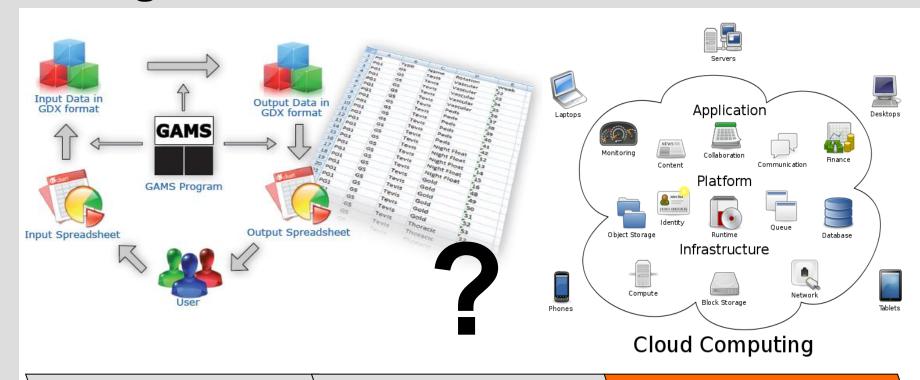
→ Users involved

Application

→Users hardly aware of model



Change in Focus: Future



Computation

→ Users left out

Model

→ Users involved

Application

→Users hardly aware of model



Summary

What is GAMS

- Algebraic Modeling Language
- Balanced mix of declarative and procedural elements
- Platform and solver independence
- Open architecture and independent layers

Role of a Model

- Communication Vehicle
- Analytic Framework
- Cost Saver

Market Demands:

- Minimize Risks
- Provide cutting edge technology
- Protect user investments



Thank You!

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