

# Class Scheduling at United States Military Academy West Point, NY

Fred O'Brien
United States Military Academy

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### **USMA MISSION**

To educate, train, and inspire the Corps of Cadets so that each graduate is a commissioned leader of character committed to the values of Duty, Honor, Country; professional growth throughout a career as an officer in the United States Army; and a lifetime of selfless service to the nation.



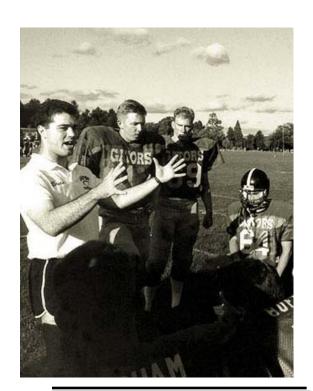
### **Program at USMA**

"... each student's daily activities are a carefully regimented balance of academic, military, and physical requirements."









### **USMA** is Different

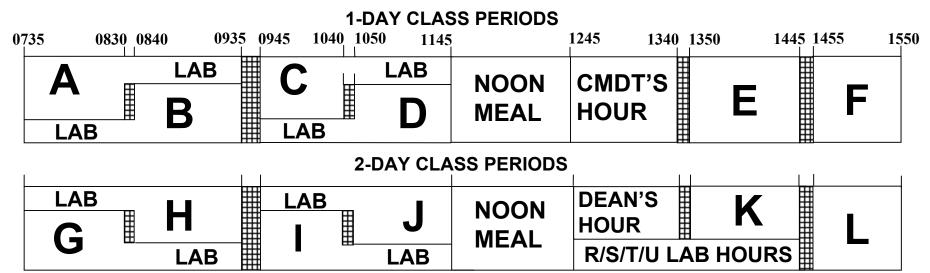
- Technically
  - Day1/day2 schedule
  - Special rules (e.G. < 30% athletes in class)
- Scheduling around the cadets needs
  - No conflicting activities
  - Individual schedule of activities is compliant to vast catalogue of *business rules*
- ➤ Proper planning

# 2 Day Schedule



AUGUST 1999 (EDITION OF AUG 98 IS OBSOLETE)

### **ATTENDANCE PERIODS**



### 1-DAY/2-DAY SCHEDULE: AY 99/00



	EG TES A		ND B SATURDAY	
DATE	1	Α	LESSON	
1-DAY or 2-DAY	_ 2		NUMBER FOR 40 LESSON	
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NOVEMBED 1000

SUNDAY MONDAY TUESDAY WEDNESDAY THURSDAY FRIDAY										
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15	16Begins 2-1	<b>F</b> K 1-1	1 8 2-2	19 1-	20 2-3	21 B RING WEEKEND				
22	23 1-	24 2- R	25 1-4	26 2- 5	27 1-	28 A/C				
<b>29</b> ⊃ <b>Ų</b> R	30 2- 1	31 <sup>4</sup> 1-6		30	3					

SUNDAY	SUNDAY MONDAY TUESDAY WEDNESDAY THURSDAY FRIDAY										
SATURDA		10230	1 2-7	2 1-	3 2-8 U	4 B					
5	6 LABOR DAY	7 1-8	8 2-9 R	9	10 2-10 S	11 A/D HOME FOOTBALL WAKE					
12	13 1- 10	14 2-11 T	15 1-11	16 2-12 U	17 1- 12	18 A/ AWAY FOOTBALL TILLANE					
19	20 2-13 R	21 1-13	22 2-	23 1-	24 2- 15	25 A/D HOME FOOTBALL					
26	27 1-15	28 2 <u>-</u> 16	29 <sup>14</sup> 1-16	30 <sup>14</sup> 2-17	15	STATE					

**SEPTEMBER 1999** 

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3	4 2-18 R	5 1-18	6 2-19 S	7 <sub>1-</sub> HOME FOOTBALL	PAR	GAROLINAB EBE ENT
10 PLEBE PARENT WEEKEND	11 COLUMBUS DAY (No Classes)	12 2-20 T	13 1-20	14 <sup>E</sup> 2-21 U	15 <sup>(NO CL</sup> 1-21	ASSES) 16Class Da 2- WAY-GOTBAL
17	18 1-22	19 2- 2 <b>R</b>	20 1-	21 2- 2S	22 1-	23 A/C HOMECOMIN G FOOTBALL
24	25 2- 2 <b>T</b>	26 <sup>3</sup> 1-25	27 2-26 U	28 <sup>-4</sup> 1-26	29 <sup>-4</sup> 2-27 R	3W <sup>EXICO</sup> A/D
31	23					

	110	<u> </u>	MID	<u>LK 1</u>	<u> </u>	
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7	8	9	10	11	12	13 A/D
	2-30	1- 30	2-31 R	VETERANS DAY (No Classes)	1-31	AWAY FOOTBALL MEMPHIS
14	152-32	16 1-32	17 <sub>2-33</sub>	18 1-33	19 2-34	20 A/C
	s		Т		Make ahead WPPWE	FOOTBALL HOUSTON
21	22	23	24	25	26	27
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	12	13°	14 TERM	15 END E	16 Xamin	17 ATION	18 S
	19 WINTER LEAVE REGINS	20 <b>◄</b>	21	22 WINTE	23 R LEA	24 /E	25
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**DECEMBER 1999** 

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	23	24	2 <del>5</del>	26	27	28	29 A/C	,			
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				R		S	WEEKEND	ı			
	30	31									
		1-5	l								
	MAY 2000										

JANUARY 2000

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	6	7 2-8 R	8 1-8	9 2-9 S	10 1-9	11 2-10 T	12 A	\/I
	13	14 1-10	15 2-11	16 1-11	17 2-	18 1-	19	В
			U_		1R	12		
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FEBRUARY 2000

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			1 2-16 U	2 1-16	3 2-	4 CLASS DAY 1-17
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12	1 3 1-20	14 2-21 U	15 1- 21	16 2- 2 <b>R</b>	17 1- compress	18 SPRING LEAVE BEGINS
19	20	21	22	23	SCHEDULE 24	25
$\blacksquare$		- 8	PRING	_		<b></b>
26 SPRING LEAVE ENDS	27 1- 23	28 <sub>2-</sub>	- <b>E∳VE</b> 1-24	30 2- 21	3 1 1-25	

MARCH 2000

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	9	10 2-28 S	11 1- 29	12 2- 25	13 1- 30	14 2-30 U	15 A/D FEE
	16	1 71- 31	18 2-31 R	19 1- 32	20 2- 3 <b>S</b>	21 1- Make ahead WPPWE	22 B
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**APRIL 2000** 

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7	8 2-38	9 1-39	10 2-39	11 1-	12 2-40	13	A/D
14	15 T	16 ERM E	17 ND EX	18 AMIN <i>A</i>	1 JIONS	20	
21	2 2 TAP BEGINS	23	24	25	26	27 GRADU	
28	29 MEMORIAL DAY	30	31			5,1	
	IN SESSION						

SUNDAY	SUNDAY MONDAY TUESDAY WEDNESDAY THURSDAY FRIDAY										
SATURDAY				1	2	3					
4	5	6	7	8	9	10					
11	12	13	1 4	15	16 STAP ENDS	17 STAP GRADUATION					
18	19	20	21	22	23	24					
25	26	27	28	29 RECEPTION "R" DAY	30						

# **Academic Program**

- 8 Term Academic Program (8TAP)
- E.g MATHEMATICS MAJOR: Statistics/Optimization

	4	5	6	7	8
1	PH202	ENG SEQ	ENG SEQ	ENG SEQ	ENG SEQ
2	MA206	ENG SEQ	MA363	MA386	MA476*
3	LX2XX	MA376	MA371	MA381*	MA481*
4	SS20X	MA383	MA387	MA492D	MA491
5	EV203	SS307	EN302	HI301	HI302
6	MA 391	PL300		LW403	

### **Enterprise Academy Management System**

Management of:

Redbook

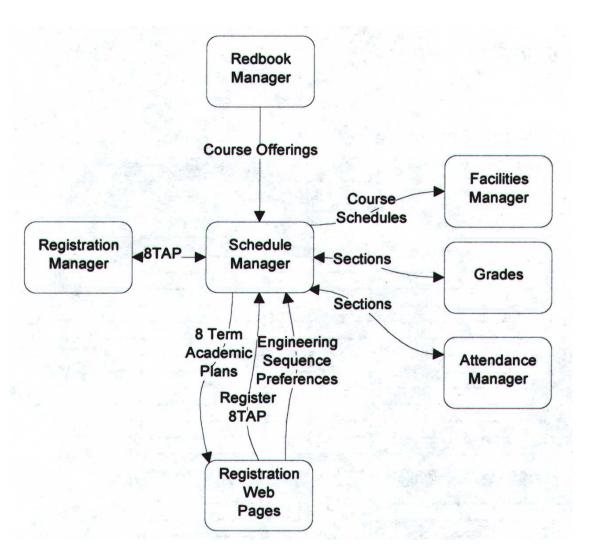
Registration

**Schedule** 

Facility

Attendance

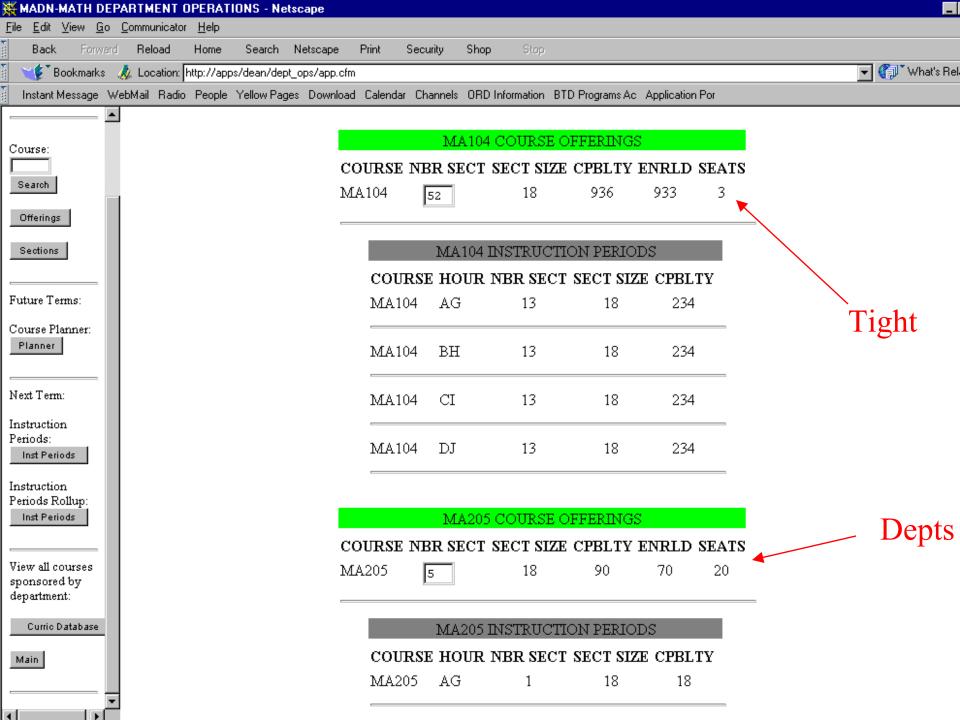
Grades



### **Academic Scheduling**

- Course scheduling
  - For a given set of course offerings find good
     schedules for all cadets.
  - Scheduling preps
    - Term balancing (department resources)
    - Initial course offerings
  - Scheduling
  - Manual post scheduling

- Term end exam (TEE)e scheduling
  - Find good schedules for exam courses and cadets.



# **Scheduling Courses to Hours**

- Difficult to handle automatically
- Rotating unpleasant hours year by year

Helpful in negotiations with departments:
 MA481 CD \( \rightarrow\) AB

Drop in conflicts and other improvements

# **Scheduling Cadet Courses to Hours**

• Given course hours & capacity

MA481,AB,36 MA481,CD,18 MA481,EF,18 PE300,C,180 PE300,J,60 MA371,F,18

• Given cadet's course registration

043671XXX,MA481 043671XXX,PE300

• Objective: Find a *good* assignment of cadet's course requests to course hours

043671XXX,MA481,CD 043671XXX,PE300,J

# **Scheduling System Objectives**

- Produced in a timely fashion
- Complies with *most* constraints/rules...
  - Individual:
    - Cadet can't be at two places at the same time
    - Course hours are balanced over Day-1, Day-2
    - Free hour
    - Cadet gets scheduled for all courses he/she has registered for
- Capacity:
  - Enrollment of course hour cannot exceed capability
  - Course enrollment of freshmen which are also athletes cannot exceed 60% of the total enrollment

# **Legacy Scheduling System**

- Matching algorithm based on cadet's course registration only
- Reporting programs check schedule against all constraints and business rules
- Last years: 80% of cadets rescheduled manually
- Time to generate schedule: 4 weeks (3 Schedulers)

### Problems with a MP Model

- There is no solution subject to *all* constraints/rules for real data
- What is the objective for the model?
- Goal Programming:
  - Relax constraints/rules by penalizing violations.
     Select penalties for violations: Calibration of the model.

### **An Optimization Model**

$$\min \sum_{ro} (p1_{ro} * \pi1_{ro} + p2_{ro} * \pi2_{ro}) + \sum_{c} (p3_{c} * \pi3_{c} + p4_{c} * \pi4_{c})$$

$$\sum_{ro} x_{c,ro} = 1 \qquad \text{(for all 8TAP entries)}$$

$$\sum_{ro \text{ on day-1}} x_{c,ro} \leq 1 + \pi3_{c} \qquad \text{(for all cadets $c$ for all time slots $o$)}$$

$$-\sigma - \pi4_{c} \leq \sum_{ro \text{ on day-1}} x_{c,ro} - \sum_{ro \text{ on day-2}} x_{c,ro} \leq \sigma + \pi4_{c} \qquad \text{(for all cadets $c$)}$$

$$x_{c,ro} = 0 \qquad \text{(for all $c$, $ro$ where $c$ has activity at $o$)}$$

$$\sum_{c} x_{c,ro} \leq cap_{ro} + \pi1_{ro} \text{ (for all course hours $ro$)}$$

$$\sum_{c \text{ freshman&athlete}} x_{c,ro} - 0.6 \sum_{c} x_{c,ro} \leq \pi2_{ro} \qquad \text{(for all course hours $ro$)}$$

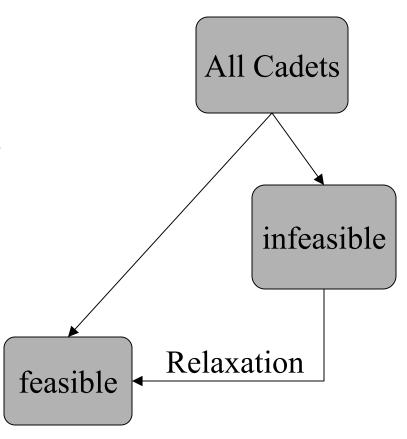
- 60,000 Variables, 500,000 Non-Zeros
- 24 hours CPLEX 6.6 and no integer solution

# A 2-Stage Approach

- Prescheduling
  - Filter cadets with no feasible schedule
  - Overcome infeasibility by relaxation/data changes
- Scheduling
  - All individual constraints/rules are hard constraints
  - Find assignment that does not exceed capacity (or penalize overloads)

# Prescheduling

- One cadet at a time
  - Check feasibility
  - If infeasible produce several infeasible schedules ranked by severeness of infeasibility
    - Hour Conflict
    - Day Day Balance
    - Last Hour Free
  - Human Intervenes

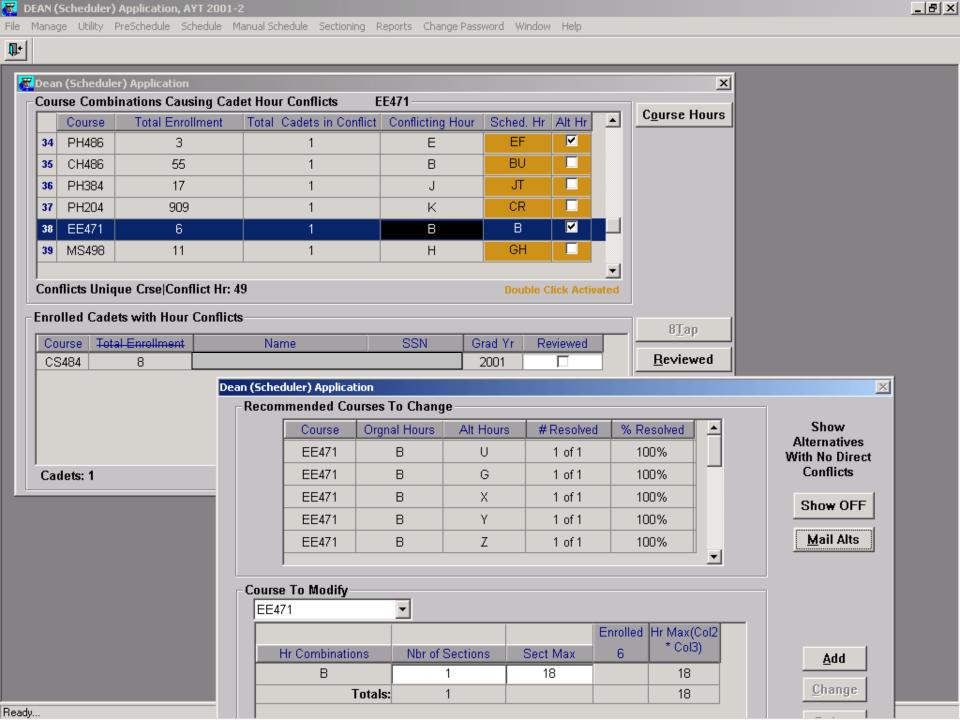


# **Conflicting Objectives**

- Departments want to teach minimum number of sections and good hours.
- Dean wants to keep course enrollment at 18 cadets per section.
- Registrar wants to ensure cadet's day to day balance is satisfied.
- ODIA want to ensure their star running back gets last hour free for football practice

### **Options**

- Change Model Data Inputs
  - Modify hours
  - Modify number of sections per hour
  - Modify cadets 8tap
- Waive Constraint
  - Unbalanced days
  - Last hour free
  - Design Group

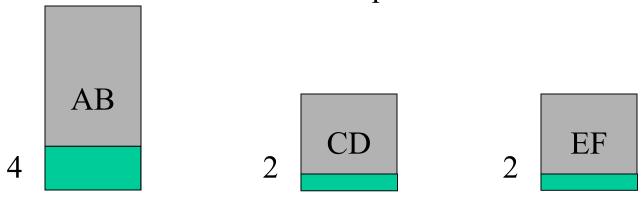


# Scheduling

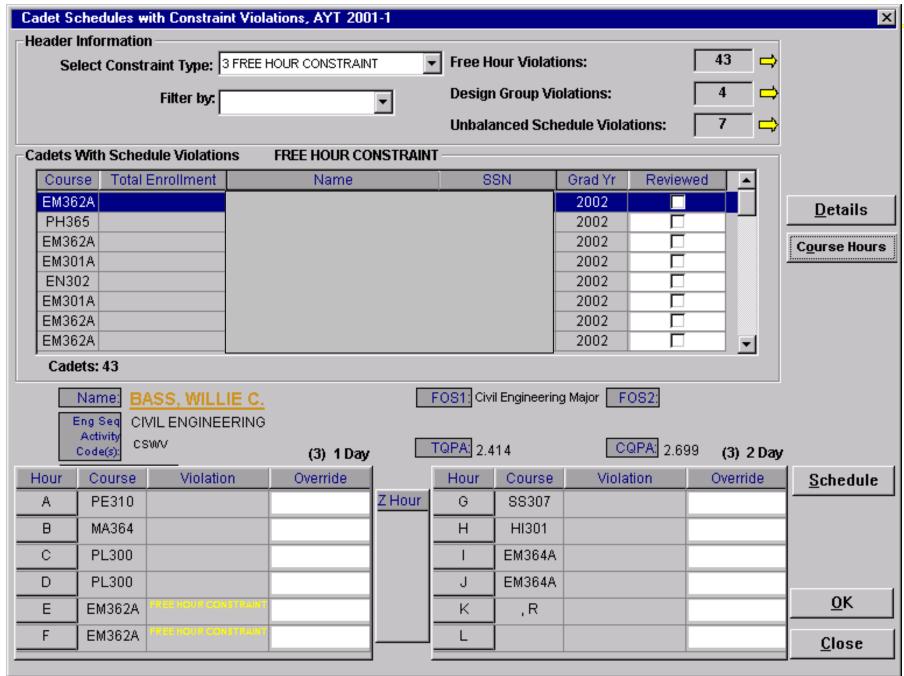
- Now individual constraints allow feasible schedules for all cadets (hard constraints)
- Tight Capacity of Course Hours may still result in an infeasible model:
  - → Assign Overload Penalties
- Model with all cadets still unsolvable!

# Scheduling in Batches

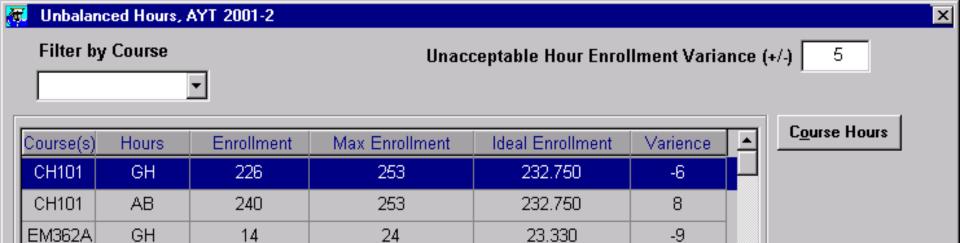
- Take a batch of cadets (10-30) and schedule them independent of the others
- Objective: Meet the capacity profile of the course hours (Penalize Over- and Underload)
- Example:
  - 3 course hours MA481 AB (20), CD,IJ (10)
  - Batch contains 8 cadets with request for MA481



OR 2001 in Duisburg



OK 2001 in Duisdurg



35,000

307.140

291,790

Number of Courses: 47

EF

F

Е

41

254

300

EM362A

EN101

EN101

**Double Click Activated** 

6

-53

9

Schedule.

Enrollment For: CH101 Hour: GH									
Name	SSN	Grad Yr	Activity						
	·	2004	CSRI						
		2004	CSSR						
		2004							
		2004							
		2004	CSFT						
		2004	CSIT						
		2004	CSBA						
Cadet Count: 225 Double Click Activated									

36

340

323

<u>C</u>ancel

### Results

- AY 2000/2 parallel tested
- AY 2001/1 deployed

	Legacy System	New System	
Individual Relaxations free/group/unbal	203/304/116	58/25/4	
Capacity Overloads Courses/seats	12/54	9/21	
Number of Schedulers	3	1	
Time to produce Schedule	4 Weeks	1 Day	

### Conclusion

- Model is only one component of the system
- Human intervention throughout the process
- "Solved" difficult real world scheduling problem
- No large MIP formulation but simple heuristic based on solution of hundreds of small MIPs