



### **An Introduction**

Tim Johannessen & Franz Nelißen GAMS Software GmbH



### Company

- Roots: World Bank, 1976
- Went commercial in 1987
- Locations
  - GAMS Development Corporation (Washington)
  - GAMS Software GmbH (Germany)
- Product: The General Algebraic Modeling System



### **Agenda**



**GAMS – Elements and Examples** 

Scenarios in GAMS

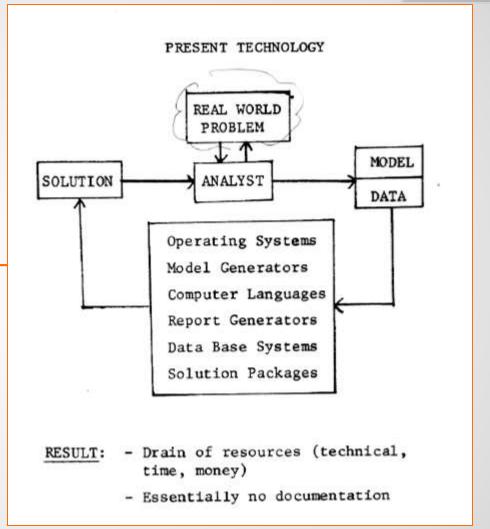
Some Enhancements





### 1976 - Two World Bank Slides



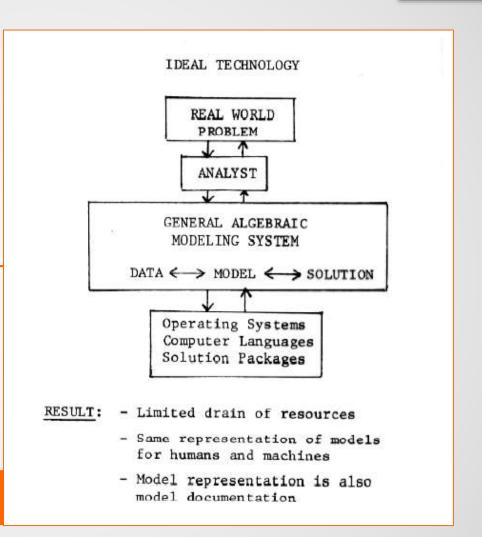




#### 1976 - Two World Bank Slides



**GAMS** came into being!





### What did this give us?



Simplified model development & maintenance

Increased productivity tremendously

Made mathematical optimization available to a broader audience (domain experts)

> 2012 INFORMS Impact Prize

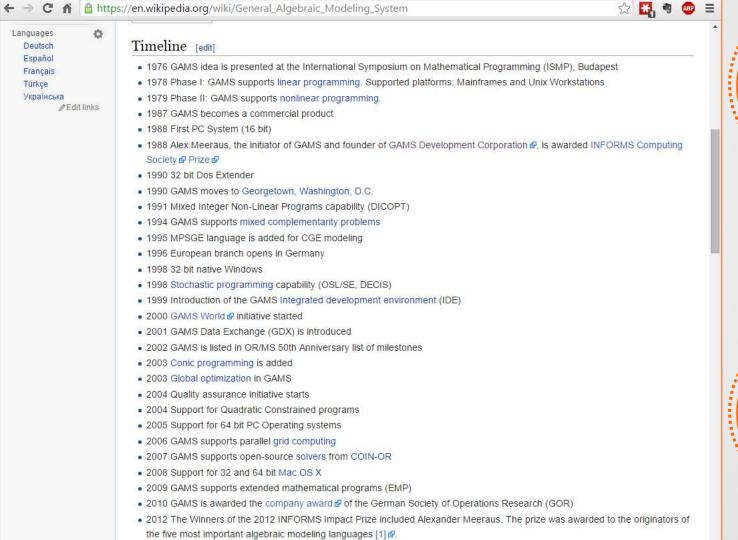






### GAMS

### **GAMS** - Evolution







### **Broad User Community and Network**



11,500+ licenses

Users: 50% academic, 50% commercial

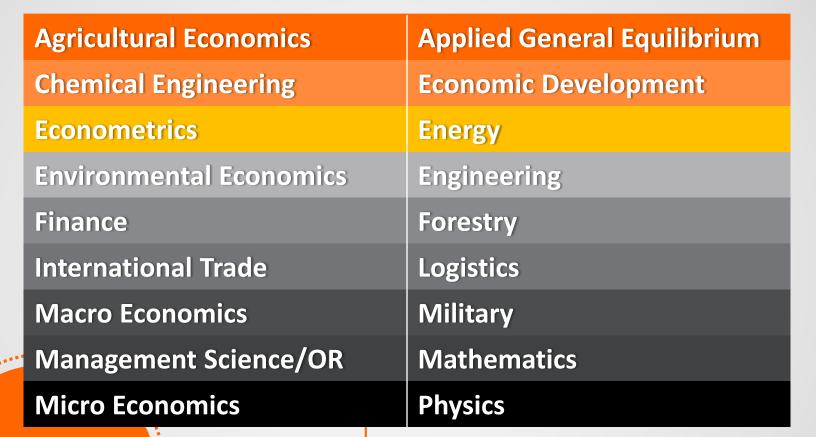
GAMS used in more than 120 countries

Uniform interface to more than 30 solvers





### **Broad Range of Application Areas**



25+ Years
GAMS Development

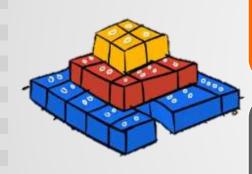






#### **Foundation of GAMS**





Powerful algebraic modeling language

Open architecture and interfaces to other systems, independent layers



### **Powerful Declarative Language**



Similar to mathematical notation

Easy to learn - few basic language elements: sets, parameters, variables, equations, models

Model is executable (algebraic) description of the problem



# Mix of Declarative and Imperative Elements



## Control Flow Statements (e.g. loops, for, if,...), macros and functions

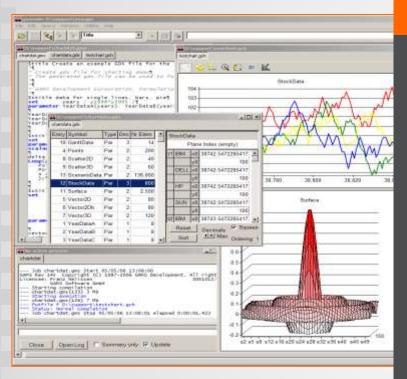
#### Advantages:

- Build complex problem algorithms within GAMS.
- Simplified interaction with other systems:
  - Data exchange
  - GAMS process control









#### **GAMS IDE**

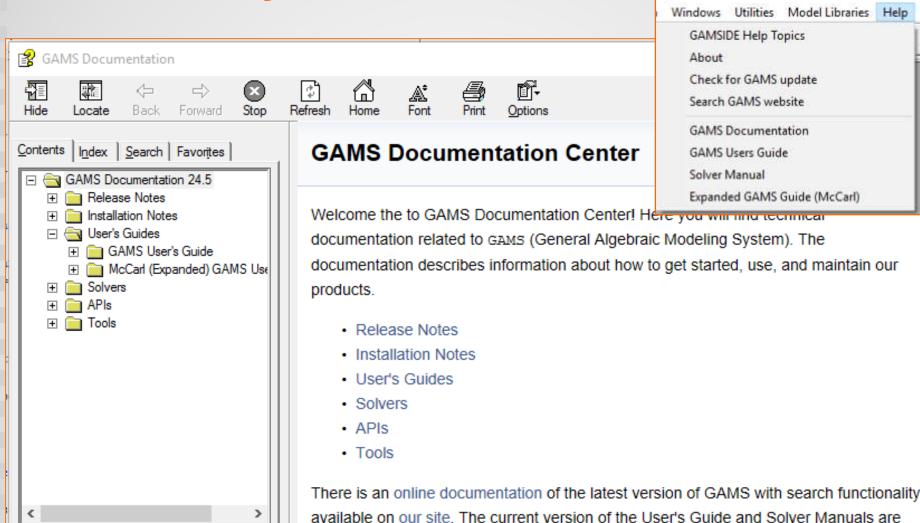
- Project management
- Editor / Syntax coloring / Spell checks
- Tree view / Syntax-error navigation
- Model Debugging & Profiling
- Solver selection & setup
- Data viewer
  - Export
  - Charting
- GAMS Processes Control



Help

Model Libraries

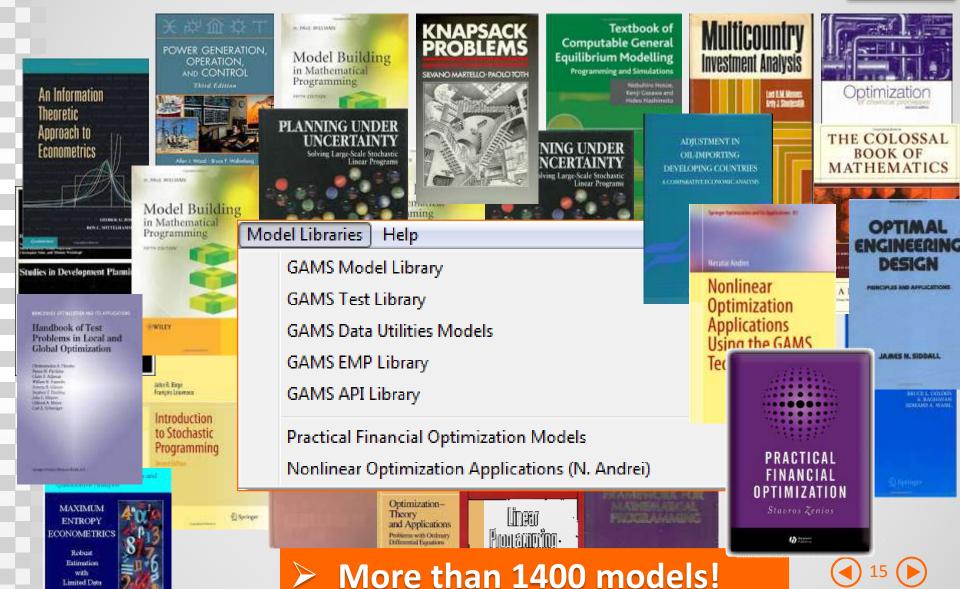
**Uniform System Documentation** 



#### **GAMS**

### **Free Model Libraries**

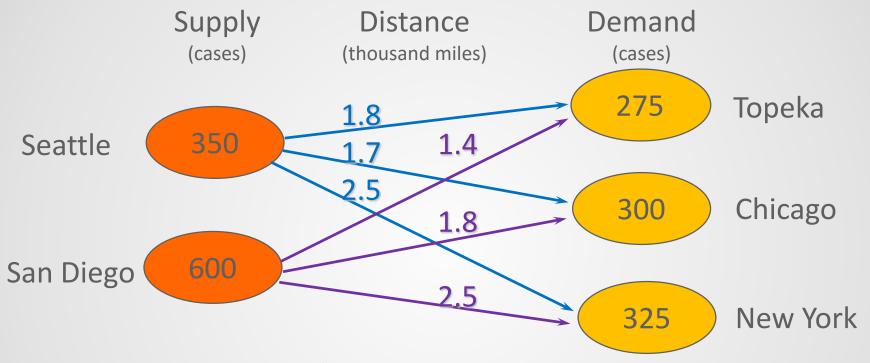
Limited Data





### **Example: A Transportation Model**





Freight: \$90 case / thousand miles

Minimize	Transportation cost
subject to	Demand satisfaction at markets
	Supply constraints





### **Example: Mathematical Model**

```
Indices:
                               (Canning plants)
                               (Markets)
                               (Number of cases to ship)
Decision variables: x_{ii}
                               (Transport cost per case)
Data:
                         C_{i,i}
                              (Capacity in cases)
                         a_i
                         b_i
                               (Demand in cases)
min
       \sum_{i} \sum_{j} c_{ij} \cdot x_{ij}
                               (Minimize total transportation cost)
subject to
      \sum_{i} x_{ij} \leq a_i \quad \forall i \quad \text{(Shipments from each plant } \leq \text{supply capacity)}
      \sum_i x_{ij} \geq b_i
                       \forall j (Shipments to each market \geq demand)
      x_{ij} \geq 0
                         \forall i, j (Do not ship from market to plant)
      i, j \in \mathbb{N}
```



### **Example: GAMS Algebra**

```
D:\Dropbox\GAMS\OR2015-Vienna\pre confernce ws\models\vienna.gms
data.gdx data.gms vienna.gms rep.gdx
     i canning plants,
     i markets:
         a(i) capacity of plant i in cases,
         b(j) demand at market j in cases,
         d(i,j) distance in thousands of miles,
         c(i,j) transport cost in thousands of dollars per case;
  Variables
                total transportation costs in thousands of dollars,
           x(i,j) shipment quantities in cases ;
  Positive Variable x;
  Equations
         cost define objective function,
       supply(i) observe supply limit at plant i,
         demand(j) satisfy demand at market j;
  cost .. z = e = sum((i,j), c(i,j)*x(i,j));
  supply(i) .. sum(j, x(i,j)) = l = a(i);
  demand(j) .. sum(i, x(i,j)) = q = b(j);
  Model modelLP /all/;
  $include data.gms
  * or via ddx
  * $qdxin data.qdx
  * $load i<d.dim1 j<d.dim2 d b a c
  Solve modelLP using lp minimizing z ;
  Parameter repl(i,j,*) Shipments between plants and markets
            rep2(*) Objective value;
  rep1(i,j,'lp') = x.l(i,j);
  rep2('lp') = z.1;
  display rep1, rep2;
```



### **Example: Data Input**

\$include data.gms data.gdx | data.gms | vienna.gms | rep.gdx |

onfernce ws\models\data.gms

```
Sets
    i canning plants / seattle, san-diego /
    i markets / new-york, chicago, topeka /;
Parameters
    a(i) capacity of plant i in cases
     / seattle
                     350
         san-diego 600 /
    b(j) demand at market j in cases
        new-york 325
          chicago 300
          topeka 275 /;
Table d(i,j) distance in thousands of miles
                new-vork
                             chicago
                                        topeka
                                           1.8
   seattle
                  2.5
                              1.7
   san-diego
                 2.5
                              1.8
                                          1.4 :
Scalar f freight in dollars per case per thousand miles /90/;
Parameter c(i,j) transport cost in thousands of dollars per case ;
        c(i,j) = f * d(i,j) / 1000;
```

\$gdxin data.gdx ce ws\models\data.gdx \$load i<d.dim1 j<d.dim2 d b a c</pre>

Entry	Symbol	Туре	Dim	Nr Elem
3	a	Par	1	2
4	b	Par	1	3
7	С	Par	2	6
5	d	Par	2	6
6	f	Par	0	1
-		A .		_

b(j): demand at market j in cases					
new-yor	325				
chicago	300				
topeka	275				

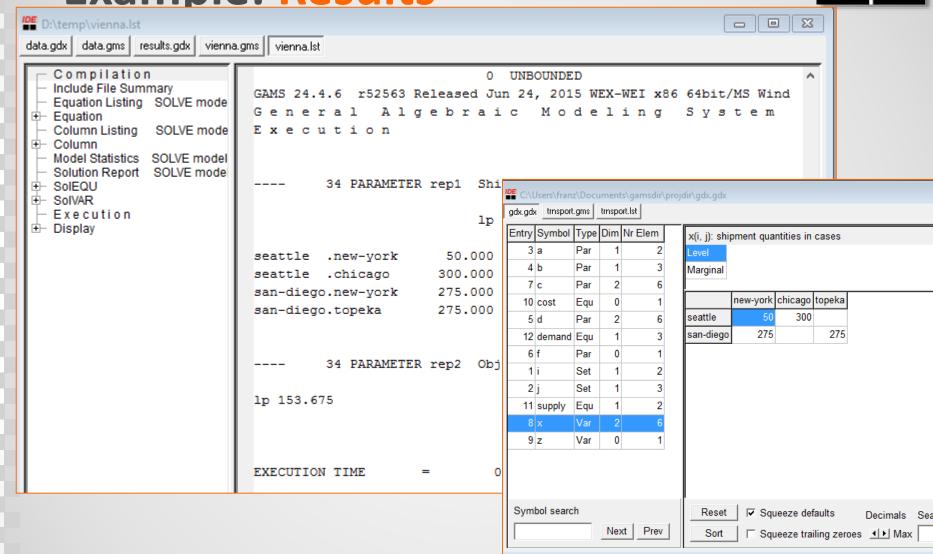








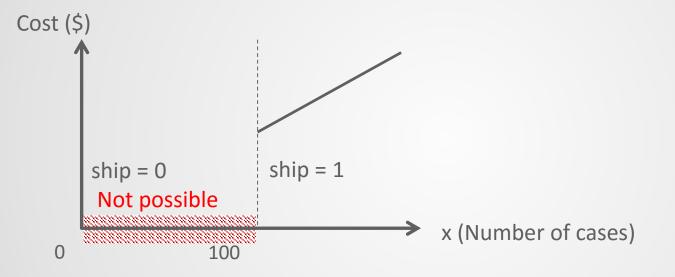
### **Example: Results**





### + MIP Model: Minimum Shipments

- Shipment volume: x (continuous variable)
- Discrete decision: **ship** (binary variable)



#### add constraints:

```
x_{i,j} \ge 100 \cdot ship_{i,j} \quad \forall i,j (if ship=1, then ship at least 100) x_{i,j} \le bigM \cdot ship_{i,j} \quad \forall i,j (if ship=0, then do not ship at all) ship_{i,j} \in \{0,1\}
```



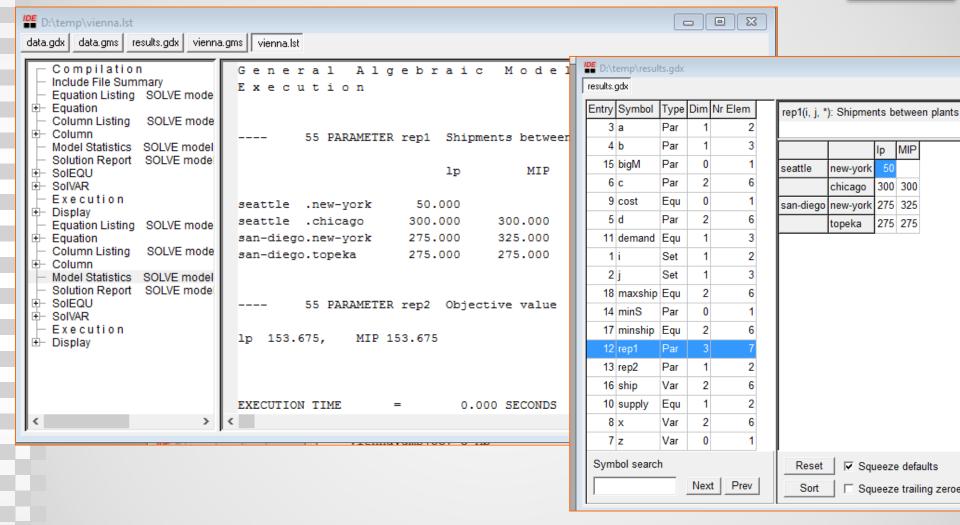


### + MIP Model: GAMS Algebra

```
D:\temp\vienna.gms
                                                                                               data.gdx data.gms results.gdx vienna.gms vienna.lst
   * MTP
   scalar minS minimum shipment /100/
          bigM big M;
   bigm = min(smax(i,a(i)), smax(j,b(j)));
   display bigm:
   binary variable ship(i,j) '1 if we ship from i to j, 0 otherwise';
   equations
          minship(i,j) minimum shipment
          maxship(i,j) maximum shipment;
    minship(i,j)...x(i,j) = g = mins*ship(i,j);
     maxship(i,j)...x(i,j) = l = bigM*ship(i,j);
   Model modelMIP /modelLP, minship, maxship/;
   option optcr =0;
   Solve modelMIP using mip minimizing z;
   repl(i,j,'MIP') = x.l(i,j);
   rep2('MIP') = z.1;
```

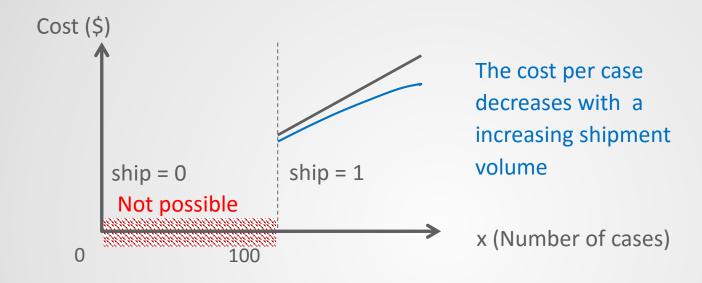
### GAMS

### + MIP Model: Results





### + non-linear: Cost Savings



#### Replace:

min 
$$\sum_i \sum_j c_{ij} \cdot x_{ij}$$
 (Minimize total transportation cost) With min  $\sum_i \sum_j c_{ij} \cdot x_{ij}^{beta}$  (Minimize total transportation cost)

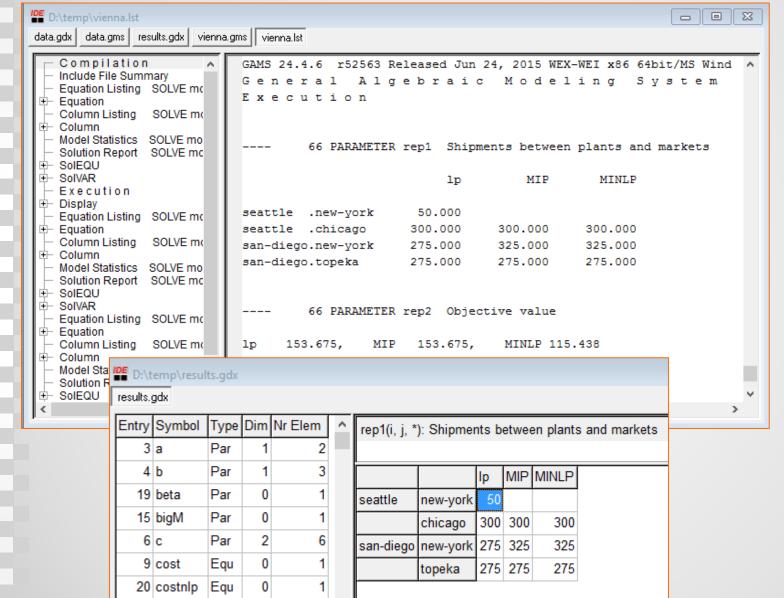


### + non-linear: GAMS Algebra

```
D:\temp\vienna.gms
                                                                                             data.gdx data.gms results.gdx vienna.gms vienna.lst
   * MINLP
   scalar beta /0.95/;
   Equation costnlp define non-linera objective function;
   costnlp .. z = e = sum((i,j), c(i,j)*x(i,j)**beta);
   Model modelMINLP /modelMIP - cost + costnlp/;
   Solve modelMINLP using minlp minimizing z ;
   rep1(i,j,'MINLP') = x.1(i,j);
   rep2('MINLP') = z.1;
   display rep1, rep2;
```

#### **GAMS**

#### + non-linear Results

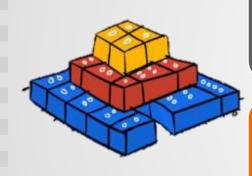






### **Foundation of GAMS**





Powerful algebraic modeling language

Open architecture and interfaces to other systems, independent layers







### Independence of Model and Platform

#### **Supported Platforms**











Move models between platforms with ease!











#### **Local and distributed / remote execution**

- Distributed Algorithm (CPLEX, GUROBI)
- Grid Computing Facility
- NEOS (Kestrel)

Model
Platform Solver Data Interface





### **GAMS/Kestrel**

- Remote Solver Execution on NEOS Servers
- > Stay in your GAMS environment
- Results are being processed as with any local solver



#### **Local Machine**

# Model transport /all/; Option lp=kestrel; transport.optfile=1; \$onecho > kestrel.opt kestrel\_solver xpress

\$offecho

Solve transport using lp minimizing z;

### Remote Cluster (NEOS)

--- Executing KESTREL: elapsed 0:00:00.006

```
Connecting to: http://neos-server.org:3332
NEOS Solver: xpress
NEOS job#=3631352, pass=iJLdAkhP

Check the following URL for progress report: http://neos-server.org/neos/cgi-bin/nph-neos-solver.cgi?admin=results&jobnumber=3631352&pass=iJLdAkhP
Job 3631352 dispatched password: iJLdAkhP
------ Begin Solver Output ---------
Job submitted to NEOS HTCondor pool.
```

FICO-Xpress 24.3.3 r48116 Released Sep 19,

2014 LEG x86 64bit/Linux





### Independence of Model and Solver





**GAMS**: Model building and interaction with solvers & environments

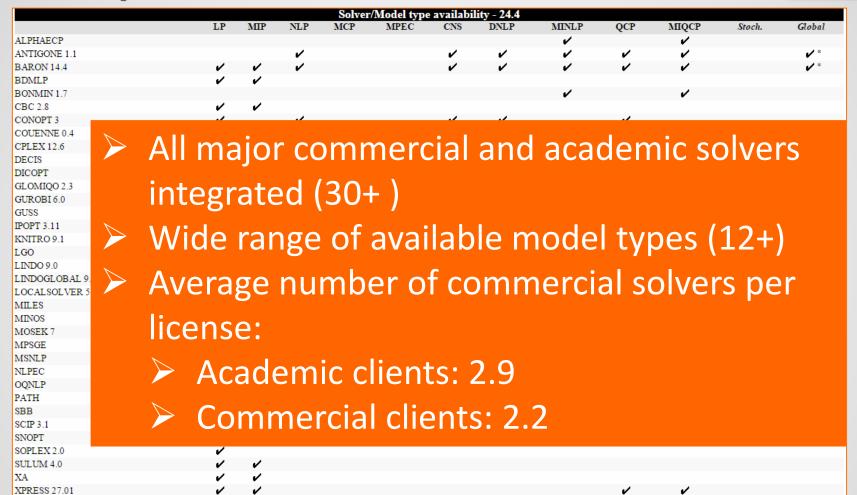
**Solver**: Solve an model instance (model + numerical data) using mathematical optimization







### Independence of Model and Solver



Model

deterministic global solver



### Independence of Model and Solver



One environment for a wide range of model types and solvers

All major commercial LP/MIP solver

Open Source Solver (COIN)

Also solver for NLP, MINLP, global, and stochastic optimization











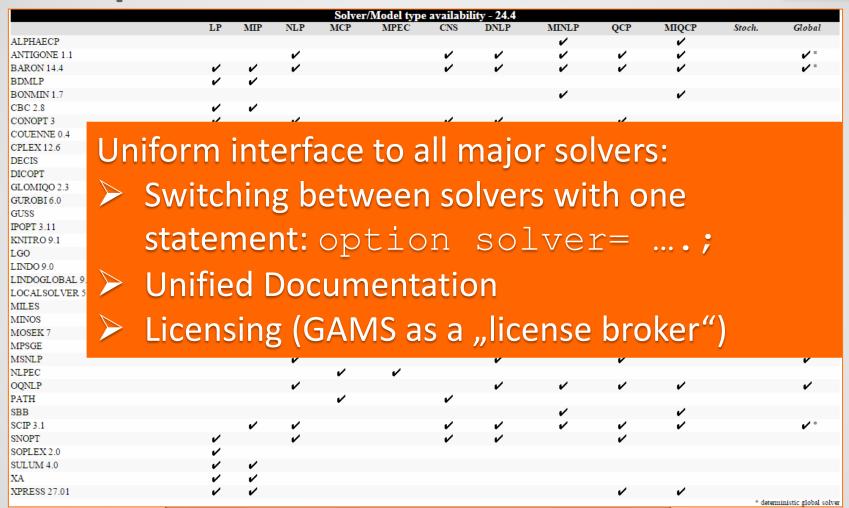
More than 30 Solvers integrated!

Model
Platform Solver Data Interface





### Independence of Model and Solver



Model







### CyBio Scheduler

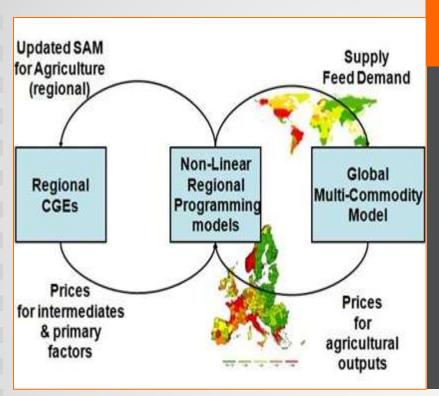
- Scheduling software for high throughput screening
- Used in the pharmaceutical industry (drug discovery)
- Model optimizes throughput of robotic screening systems
- Solver
  - COIN for smaller instances
  - Commercial MIP solver for large problems
- Developed by analytikjena





### Independence of Model and Solver





#### **CAPRI**

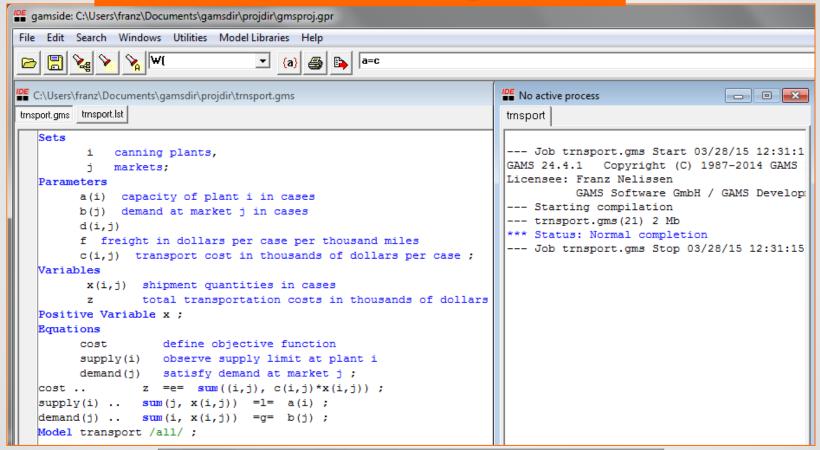
- Global agricultural sector models with focus on EU27 members
- Evaluates impacts of agricultural and trade policies on production income, markets, trade, and the environment
- **Different NLP solvers**
- Open source approach with an active network of developers and users coordinated by University of Bonn





### Independence of Model and Data









### Independence of Model and Data

### Initial Model Development – ASCII

- Input: Part of model input (\$include file.gms)
- Output: Display / Put Command (File)

```
file fy /result.csv/;
fy.pc = 5; fy.nd = 4;
loop((i,j)$x.l(i,j),
     put fy i.te(i) j.te(j) x.l(i,j) /;
     );
"seattle", "new-york", 50.00
"seattle", "chicago", 300.00
"san-diego", "new-york", 275.00
"san-diego", "topeka", 275.00
                       Model
```



Interface

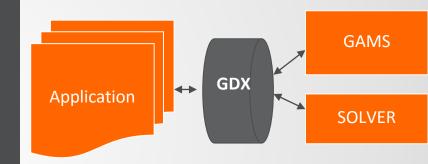






**GDX:** Binary Data layer ("contract") between GAMS and applications

- Fast exchange of data at any stage
- Platform independent
- Direct GDX interfaces and OO APIs
- No license required
- Scenario Management Support



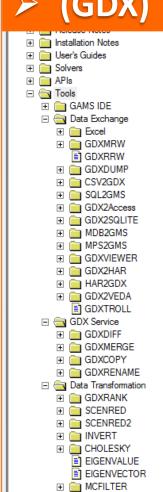






## Independence of Model and Data

### (GDX) Tools included in the GAMS distribution



CSDP CSDP → Other Tools A large number of tools are included in GAMS distribution. Below we give a functional categorization of all tools as well as a brief description of each tool with the Supported Platforms.

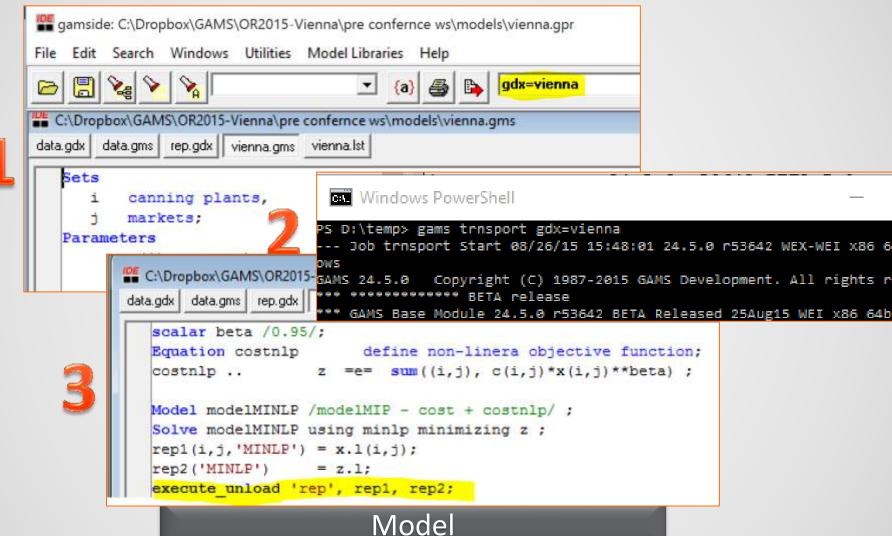
- GAMS IDE an integrated model development environment including a general text editor with the ability to launch and monitor the compilation and execution of GAMS models.
- Data Exchange a collection of tools that provide functionality to exchange data between GAMS and other data sources. This category contains tools for popular data sources and high-level programming environment and like databases, Matlab, and R. There are also tools for specialized systems like HAR, TROLL, and VEDA. The tools to communicate with Microsoft Excel are grouped in a subcategory Excel. Many of the tools described here use the GAMS Data eXchange facility GDX.
- GDX Service a collection of tools that operate directly on GDX containers to e.g. compare, copy, and merge the content of GDX..
- · Data Transformation a collection of tools that perform very specific tasks that are awkward or inefficient to implement in GAMS directly. Through GDX and the execution of the tools in this category allow to perform complex tasks from a GAMS model like identifying eigenvalues or the inverse of a matrix.
- Other Tools a collection of more exotic tools that can become handy in some some special circumstances. Most notably, the collection contains the tool MODEL2TEX to document the model algebra in LaTeX format.

The following table gives an alphabetically sorted list of all available tools.

Tool	Description
ASK	The utility can be used to get input from an user interactively.
BIB2GMS	Analyses BibTeX files with file extension .bib and writes GAMS source files that can be used to create various author, reference and cross reference reports.
CHK4UPD	Checks whether the user can update to a more recent GAMS version.
CHOLESKY Calculates the Choleksy decomposition of a symmetric positive definite matrix.	
CCDD	The semidefinite programming CSDP solver from COIN-OR. The communication with CSDP requires

### **GAMS**

# Creating a GDX file





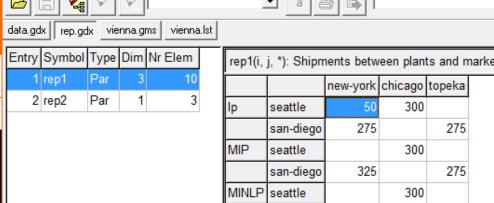
Interface



# Looking at a GDX file

#### **GAMS IDE-GDX Browser**

- Data cube with Drag&Drop
- Searching and Charting
- Export to Excel, HTML,...



san-diego

325

Windows PowerShell S D:\temp> gdxdump .\rep.gdx Parameter rep1(\*,\*,\*) Shipments between plants and markets seattle'.'new-york'.'lp' 50, seattle'.'chicago'.'lp' 300, seattle'.'chicago'.'MIP' 300, 'seattle'.'chicago'.'MINLP' 300, san-diego'.'new-york'.'lp' 275, san-diego'.'new-york'.'MIP' 325, san-diego'.'new-york'.'MINLP' 325, 'san-diego'.'topeka'.'lp' 275, san-diego'.'topeka'.'MIP' 275, san-diego'.'topeka'.'MINLP' 275 /; Parameter rep2(\*) Objective value / 'lp' 153.675, MIP' 153.675, MINLP' 115.437925639658 /;

\$offempty D:\temp>

> Model Platform Solver Interface Data





275



### **GDX2XLS**

### Dumping a GDX container to Excel

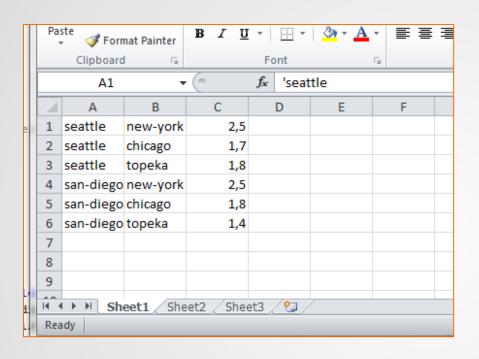
gdx2xls rep.gdx shellexecute rep.xlsx



	A1	▼ ( f <sub>x</sub>			v k
1	А	В	С	D	E .
1					fe
2	rep1	(parameter)	Shipments betwe	en plants and mar	kets
3	dim1 ▼	dim2 ▼	dim3 ▼	Value <b>▼</b>	
4	seattle	new-york	lp	50	
5	seattle	chicago	lp	300	
6	seattle	chicago	MIP	300	
7	seattle	chicago	MINLP	300	
8	san-diego	new-york	lp	275	
9	san-diego	new-york	MIP	325	
10	san-diego	new-york	MINLP	325	
11	san-diego	topeka	lp	275	
12	san-diego	topeka	MIP	275	
13	san-diego	topeka	MINLP	275	_
H ◀ ▶ H rep1 rep2 ધ					
Ready 100% — — — — — — — — — — — — — — — — — —					



# **GDXXRW – Accessing Excel Files**



\$call GDXXRW dist.xlsx par=d rng=A1 rdim=2 cdim=0
\$if errorlevel 1 \$abort "Problems with Excel file!"
\$gdxin dist
\$load d

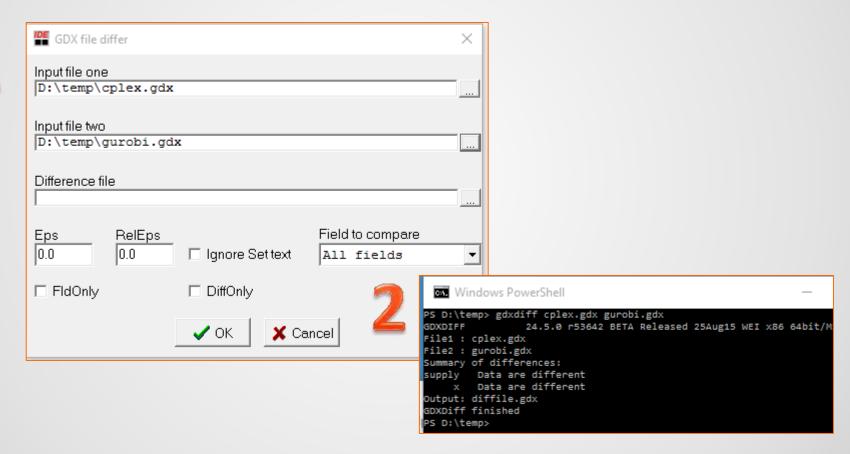




### **GDXDiff**

Comparing two gdx files

1

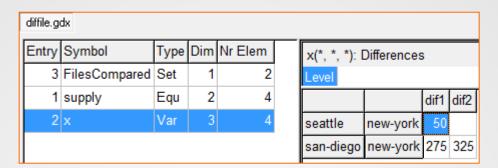






### **GDXDiff** - Results





2

```
Windows PowerShell
quation supply(*,*) Differences /
seattle'.'dif1'.L 350,
'seattle'.'dif1'.M Eps,
'seattle'.'dif1'.UP 350,
seattle'.'dif2'.L 300,
seattle'.'dif2'.UP 350,
san-diego'.'dif1'.L 550,
'san-diego'.'dif1'.UP 600,
'san-diego'.'dif2'.L 600,
san-diego'.'dif2'.UP 600 /;
ositive Variable x(*,*,*) Differences /
'seattle'.'new-york'.'dif1'.L 50,
'seattle'.'new-york'.'dif2'.M Eps,
san-diego'.'new-york'.'dif1'.L 275,
san-diego'.'new-york'.'dif2'.L 325 /;
et FilesCompared(*) /
File1' D:\temp\cplex.gdx,
File2' D:\temp\gurobi.gdx /;
offempty
S D:\temp>
```









# Independence of Model and User Interface



1

Open architecture and interfaces to other systems

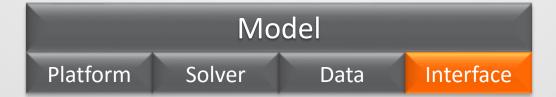
→ No preference for a particular user interface

2

(OO) Application Programming Interfaces

3 <

Smart Links to popular environments: Excel, MATLAB, R, ...







Independence of Model and User Interface

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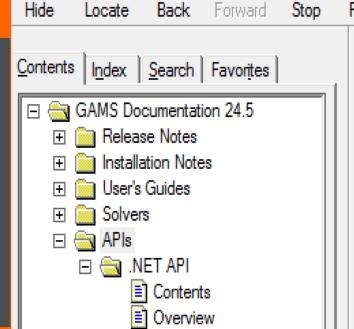


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Font

### API's

- Low Level
- Object Oriented: .Net, Java, Python
- No modeling capability:
  Model is written in GAMS
- Wrapper class that encapsulates a GAMS model



**GAMS** Documentation

APIs - Appli

# **High-Lev**

There are three ve with .NET framewo oriented GAMS AF

Model
Platform Solver Data Interface







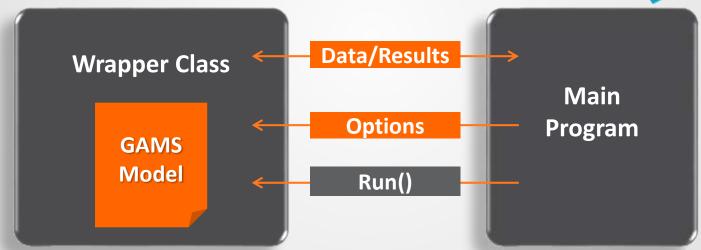


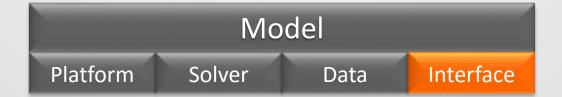


#### **Simple API interface**

- Properties to communicate input data and results
- > Properties to change options like the solver to use
- Run() method to run the model





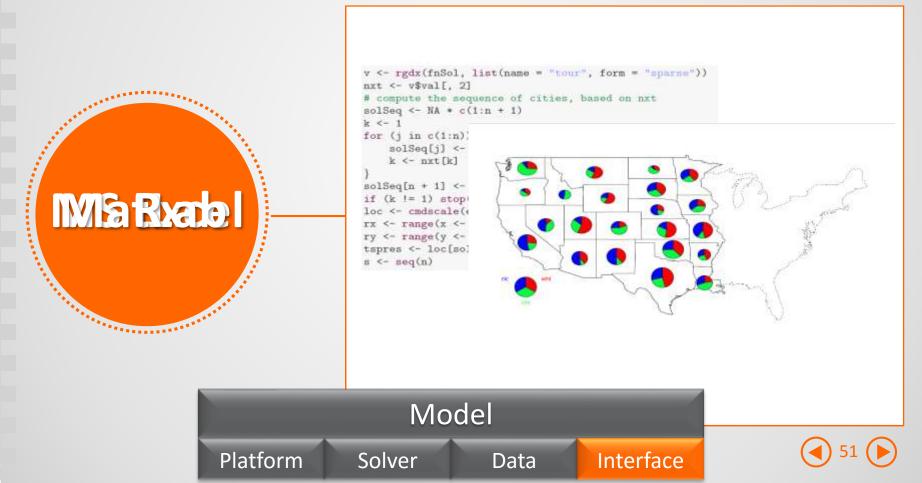






### **Smart Links to other Applications**

- User keeps working in his productive tool environment
- > Application accesses all optimization capabilities of GAMS through API
- Visualization and analysis of model data and results in the application





# **Agenda**

GAMS – Elements and Examples

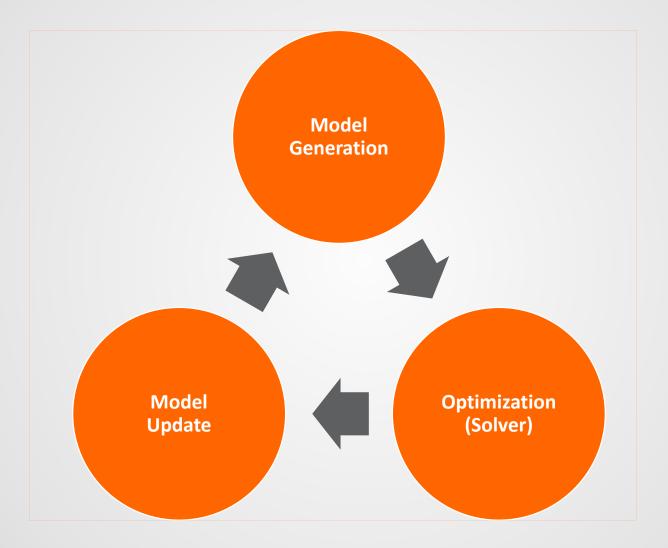
**Scenarios in GAMS** 

Some Enhancements





# **Solving Scenarios**





# Simple Serial Solve Loop



```
Set s /s*s10/;
                                                      Loop
Parameter
A_s(s,i,j) "scenario data",
xlo_s(s,i,j) "scenario lower bound for x.l",
                                                     Generation
 em_s(s,i) "scenario solution for e.m;
Loop(s,
                                                      Solution
     A(i,j) = A_s(s,i,j);
     x.lo(j)=xlo_s(s,j);
                                                      Update
     solve mymodel min z using lp;
     xl_s(s,j) = x.l(j);
     em_s(s,i) = e.m(i);
    );
```



## **Simple Serial Solve - Performance**

```
nce
```

```
trnsport.gms (LP) solved 500 times with CPLEX:
```

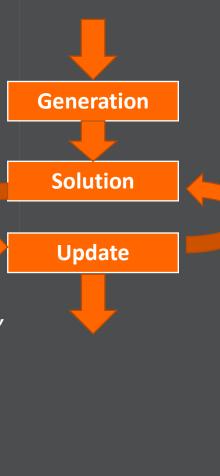
```
Loop(s,
    d(i,j) = dd(s,i,j);
    f = ff(s);
    solve transport using lp minimizing z;
    rep(s) = transport.objval;
);
```

Setting	Solve time (secs)
Solvelink=%Solvelink.ChainScript%	52.221
Solvelink=%Solvelink.CallModule%	37.366
Solvelink=%Solvelink.LoadLibrary%	03.252



# **Scenario Solver (GUSS)**

- Generates model once and updates the algebraic model keeping the model "hot" inside the solver
- Platform independent, works with all solvers
- Performance close to native solver API
- Example:





### **Scenario Solver - Performance**



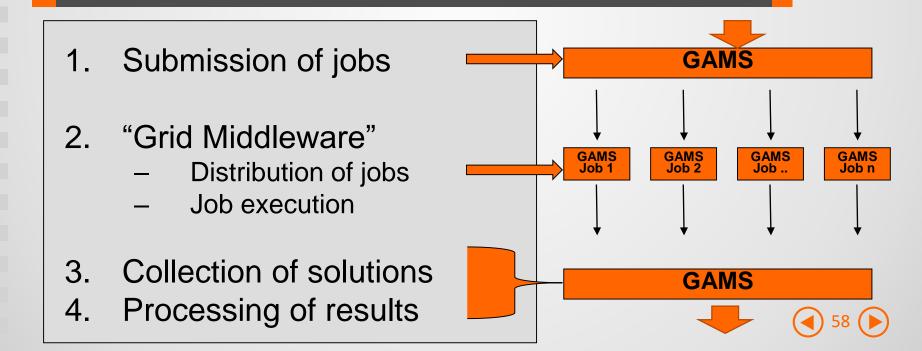
Setting	Solve time (secs)	
Loop: Solvelink=%Solvelink.Chainscript (default)	7,204	Factor
Loop: Solvelink=%Solvelink.LoadLibrary%	2,481	18.3
GAMS Scenario Solver	392	
CPLEX Concert Technology	210	1.86



# **Grid Computing Facility**



- Scalable: supports large grids, but also works on local machine
- Platform independent, works with all solvers/model types
- > Only minor changes to model required





### **Grid Computing Facility - Example**

```
trnsgrid.gms trnsgrid.lst vienna.gms
  transport.solvelink = %solvelink.AsyncGrid%; // turn on grid optio
  transport.limcol
  transport.limrow = 0:
  transport.solprint = %solprint.Quiet%;
  set s scenarios / 1*5 /:
  parameter dem(s,j) random demand
            h(s) store the instance handle;
  dem(s,j) = b(j) *uniform(.95,1.15); // create some random demands
  loop (s,
     b(j) = dem(s, j)
     Solve transport using lp minimizing z;
     h(s) = transport.handle );
                                 // save instance handle
  parameter repx(s,i,j) solution report
                        summary report;
            repv
  repy(s,'solvestat') = na;
  repy(s,'modelstat') = na;
  * we use the handle parameter to indicate that the solution has bee
  repeat
     loop (s$handlecollect (h(s)),
        repx(s,i,j) = x.l(i,j);
        repy(s,'solvestat') = transport.solvestat;
        repv(s,'modelstat') = transport.modelstat;
        repy(s,'resusd') = transport.resusd;
        repy(s,'objval') = transport.objval;
        display$handledelete(h(s)) 'trouble deleting handles' ;
        h(s) = 0 ); // indicate that we have loaded the solution
     display$sleep(card(h)*0.2) 'was sleeping for some time';
  until card(h) = 0 or timeelapsed > 10; // wait until all models ar
```

abort\$sum(s\$(repy(s,'solvestat')=na),1) 'Some jobs did not return';

Di\temp\trnsgrid.gms

display repx, repy;

### GAMS Model Library: Transgrid

```
** ********** BETA release
icensee: Franz Nelissen
                                                        S150326/0001CN-GE
        GAMS Software GmbH
                                                                    DC345
-- Starting compilation
-- trnsgrid.gms(101) 3 Mb
-- Starting execution: elapsed 0:00:00.003
-- trnsgrid.gms(75) 4 Mb
-- Generating LP model transport
-- trnsgrid.gms(77) 4 Mb
-- LOOPS s = 1
    6 rows 7 columns 19 non-zeroes
-- Submitting model transport with handle grid145000001
-- Executing after solve: elapsed 0:00:00.017
-- trnsgrid.gms(75) 4 Mb
-- Generating LP model transport
-- trnsgrid.gms(77) 4 Mb
-- LOOPS s = 2
   6 rows 7 columns 19 non-zeroes
-- Submitting model transport with handle grid145000002
-- Executing after solve: elapsed 0:00:00.094
- trnsgrid.gms(75) 4 Mb
-- Generating LP model transport
-- trnsgrid.gms(77) 4 Mb
    6 rows 7 columns 19 non-zeroes
-- Submitting model transport with handle grid145000003
-- Executing after solve: elapsed 0:00:00.121
-- trnsgrid.gms(75) 4 Mb
-- Generating LP model transport
-- trnsgrid.gms(77) 4 Mb
    6 rows 7 columns 19 non-zeroes
-- Submitting model transport with handle grid145000004
-- Executing after solve: elapsed 0:00:00.134
-- trnsgrid.gms(75) 4 Mb
-- Generating LP model transport
-- trnsgrid.gms(77) 4 Mb
-- LOOPS s = 5
   6 rows 7 columns 19 non-zeroes
-- Submitting model transport with handle grid145000005
-- Executing after solve: elapsed 0:00:00.147
 - trnsgrid.gms(88) 4 Mb
-- GDXin=D:\temp\225a\grid145000001\gmsgrid.gdx
-- Removed handle grid145000001
-- GDXin=D:\temp\225a\grid145000002\gmsgrid.gdx
-- Removed handle grid145000002
-- GDXin=D:\temp\225a\grid145000003\gmsgrid.gdx
- Removed handle grid145000003
```



# Solving "many" Scenarios

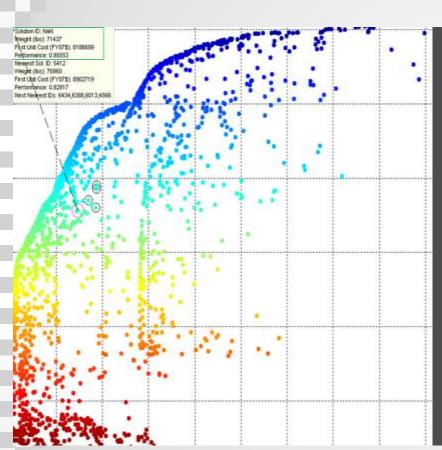


- Small Ratio of solver time / GAMS time -> Scenario Solver
- Large ratio i.e. only solver time is relevant (pre/post processing not critical) -> Grid Computing Facility
- Entire model run including pre processing / optimization / post processing is costly  $\rightarrow$  Parallel execution of entire model in the cloud



# **Application - Scenario Solver**





- Generation of Efficient Frontiers
- > GAMS/CPLEX solution pool to collect 1,000,000+ solutions of a small MIP
- Compact representation of solutions
- Uses an ACE algorithm to filter out dominated solutions



# **Application - Scenario Solver**



Implementation	Number of MIP models	Solve time	Rest of algorithm	Total time
Traditional GAMS loop	100,000	1068 sec	169 sec	1237 sec
Scenario Solver	100,000	293 sec	166 sec	459 sec

Implementation			Parallel sub- problem time		Total time
Parallel + Scenario Solver	100,000	4	116 sec	67 sec	183 sec

http://yetanothermathprogrammingconsultant.blogspot.de/2012/04/parallel-gams-jobs-2.html







### **Application - Grid Computing Facility**



- 4096 MIP models on HT Condor
- > Submission started Jan 11,16:00
- All jobs submitted by Jan 11, 23:00
- All jobs returned by Jan 12, 12:40
  - 20 hours wall time, 5,000 CPU hours
  - Peak number of CPU's: 500











# xyz – Energy Company

- ➤ Task: Solve 1,000 scenarios (MIPs, ~1 hour per scenario) once a week overnight in parallel
- Implementation:
  - Amazon Cloud: 1000 parallel machines (instances), Python, GAMS + OO API
  - > Issues: Automation / Licensing / Security
  - Hardware Costs / run: \$70!
    (1,000 instances/run \* \$0.07 instance / hour)



# **Agenda**

GAMS – Elements and Example

Scenarios in GAMS

**Some Enhancements** 





# Striving for Innovation and Compatibility

#### Models must benefit from:

Advancing hardware / New Platforms

Enhanced / new solver and solution technology

Improved / upcoming interfaces to other systems

New Modeling and Solution Concepts

#### **Protect investments of Users**

Life time of a model: 15+ years

New maintainer, platform, solver, user interface

**Backward Compatibility** 

**Software Quality Assurance** 





## **New Modeling and Solution Concepts**



- > Bilevel Programs
- Extended Nonlinear Programs
- Stochastic Programming
- Disjunctive Programs

#### **Issues:**

- Breakouts of traditional Mathematical Programming classes
- Limited support with common model representation
- > Incomplete/experimental solution approaches
- ➤ New and interesting solver features driven by implementation choices → May break solver independence of models

#### **Challenge:**

Find a concept that combines the essentials of new features independent of the particular implementation choices.



# The "GAMS" - Approach



### Extended Mathematical Programming

**Experimental framework** for **automated** mathematical programming **reformulations** 

Keep the language simple: Do **not overload** existing GAMS notation

Use **existing language features** to specify additional model features, structure, and semantics

Express extended model information in symbolic (source) form and apply existing modeling/solution technology

Package new tools with the production system

GAMS is conservative when it comes to syntax extensions

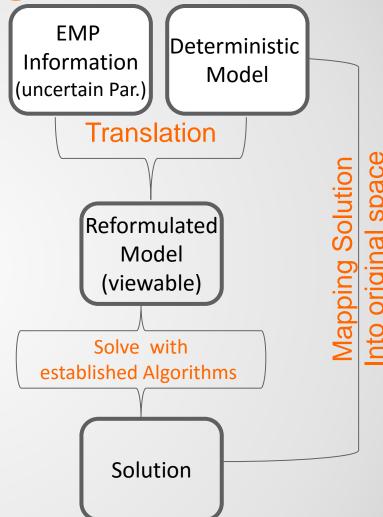




# **Stochastic Programming in GAMS**

### EMP/SP

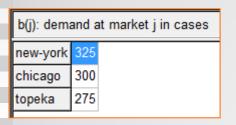
- ➤ Simple interface to add uncertainty to existing deterministic models
- ➤ (EMP) Keywords to describe uncertainty include: discrete and parametric random variables, stages, chance constraints, Value at Risk, ...
- > Available solution methods:
  - Automatic generation of
     Deterministic Equivalent (can be solved with any solver)
  - Specialized commercial algorithms (DECIS, LINDO)



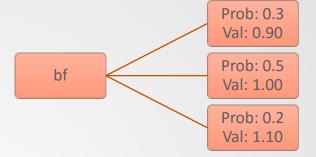




### **Transport Example - Uncertain Demand**



Uncertain demand factor *bf* 



### **Decisions to make**

- First-stage decision: How many units should be shipped "here and now" (without knowing the outcome)
- Second-stage (recourse) decision:
  - How can the model react if we do not ship enough?
  - Penalties for "bad" first-stage decisions, e.g. buy additional cases u(j) at the demand location:

```
costsp .. z =e= sum((i,j), c(i,j)*x(i,j))+

sum(j,0.3*u(j));

demandsp(j) .. sum(i, x(i,j)) =g= bf*b(j) - u(j);
```







### **Uncertain Demand - GAMS Algebra**

```
data.gdx data.gms rep.gdx vienna.gms vienna.lst
   * Stochastic
  Positive Variable u(j) unmet demand;
  scalar bf demand factor /1/;
  equation costsp, demandsp;
            z = e = sum((i,j), c(i,j)*x(i,j)) + sum(j,0.3*u(j));
  demandsp(j) .. sum(i, x(i,j)) = g = bf*b(j) - u(j);
  Model modelsp /costsp, demandsp, supply/;
  file emp / '%emp.info%' /; put emp '* problem %gams.i%'/;
  Sonput
  randvar bf discrete 0.3 0.9
                      0.5 1.0
                      0.2 1.1
  stage 2 bf demandsp u
  Soffput
  putclose emp;
  Set scen scenarios / s1*s3 /;
  Parameter
      s bf(scen) demand factor realization by scenario
     s x(scen,i,j) shipment per scenario
      s u(scen, j) cases bought per scenario;
  Set dict / scen .scenario.''
            bf .randvar .s bf
             x .level .s x
             u .level .s u /;
  option solver=lindo;
  Solve modelsp using emp minimizing z scenario dict;
  Display s bf, s x, s u;
```



### **Uncertain Demand - Results**

```
vienna.lst rep.gdx
        103 PARAMETER s bf demand factor realization by scenario
 s1 0.900, s2 1.000, s3 1.100
        103 PARAMETER s x shipment per scenario
             new-york chicago topeka
 s1.seattle 50.000 300.000
 s1.san-diego 242.500
                                275.000
 s2.seattle 50.000 300.000
 s2.san-diego 242.500
                                275.000
 s3.seattle 50.000 300.000
 s3.san-diego 242.500
                                275.000
       103 PARAMETER s u cases bought per scenario
      new-york chicago topeka
      32.500
 32
      65.000 30.000 27.500
```



### **Stochastic Programming in GAMS**



- Start with a deterministic model and define uncertain model parameters
- > EMP/SP replaces these parameters and generates stochastic model
- > EMP/SP supports:
  - Discrete and continuous distributions
  - Multi-stage problems
  - Chance constraints
  - Various Risk Measures (EV, VaR, CVaR)
- ➤ EMP/SP can use specialized algorithms (DECIS, LINDO) or create the Deterministic Equivalent (free solver DE)
- Further Information:
  http://www.gams.com/dd/docs/solvers/empsp/index.html



# **Logical Constraints**

- **Example:** If y=1 => x1 + x2 + x3=L= 0;
- > EMP supports **automatic reformulation** of logical constraints (disjunctive programming) in various formats, e.g.
  - BigM-Formulation

```
constr01.. x1 + x2 + x3 = L = M*(1-y);
y \in \{0,1\};
```

- Indicator Constraints (CPLEX, XPRESS, SCIP):
   constr01.. x1 + x2 + x3 = L= 0;
   indic constr01\$y 1
- > Alternative: SOS1 (GUROBI): constr01.. x1 + x2 + x3 = L = M;SOS1:(y, M);
- Further Information: http://www.gams.com/dd/docs/solvers/jams/index.html





## **Quality Assurance at GAMS**

		Solver/Plat	form avai	lability -	24.4		
	x86 32bit MS Windows	x86 64bit MS Windows	x86 64bit Linux	x86 64bit MacOS X	x86 64bit SOLARIS	Sparc 64bit SOLARIS	IBM Power 64bit
ALPHAECP	~	~	~	~	~	~	~
ANTIGONE 1.1	V	~	~	/			
BARON 14.4	~	~	~				
BDMLP	~	~	~	~	V	~	~
BONMIN 1.7	~	~	~	~	~		
CBC 2.8	V	~	~	~	~		
COUENNE 0.4	~	~	~	/	~		
CONOPT 3	V	~	~	~	~	~	~
CPLEX 12.6	~	V	~	~	~	~	~
DECIS	V	~	~			~	
DICOPT	~	~	~	~	~	~	~
SLOMIQO 2.3	~	~	~	~			
SUROBI 6.0	V	~	V	~			~
		1 - 1 -			~		
> 7 st	upporte	d Plat	torm	S			
	appoi co				8.0		
A 20.	lasks suc	4 - d C			8.0		
> 30+	· Integra	ited 50	oiver	S	~	~	
MILES	V	V	7	V	V	~	~
MINOS		- 5	•	- 1			

- > What are the impacts of
  - > new features
  - updated or new solvers?
- > Is the new distribution backward compatible?

SULUN 4.0	~	V	~				
XA	~	~	~				
XPRESS 27.01	V	~	~	~	~	~	~





# **Quality Assurance - Motivation**



## Quality Assurance

- > Essential component in most industries
- > Important in most software engineering sectors

## Mathematical Programming

- Less attention to quality assurance (small community)
- Specific QA issues for modeling systems (initially expensive)
- > Different focus for industry and academia

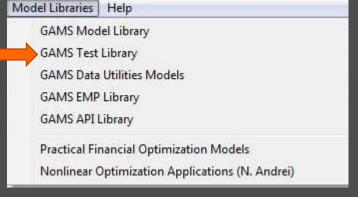
# Industry Academia Focus on reliability Focus on performance



# **Quality Test Model Library**

- > Tests to verify proper behavior of the system
- More than 680 quality test models, each containing numerous pass/fail tests
- > Assurance about the basic functionality of the software!
- ➤ Give the tools in the hand of the user: Included in any

distribution!



- ➤ Automatically executed every night for all solver combinations:
  - > 13,000+ runs / platform (all tests)
  - Test summaries with different level of information





# **Nightly Quality Tests: Results**



#### **Latest GAMS System Builds and Test Results**

Sunday 12Apr15 15:22 (UTC)

[ Latest Builds | Alpha Builds | Beta Builds | Nightly Builds | a Help System | Glossary ]

Comments?

NOTE: The (nightly) alpha builds are internal development versions of the GAMS system. They may have known bugs, unfinished features, beta versions of third-party software, or may not function at all! Not for production use!

nightly a	System	Libraries	Build	Rev	Status ar	nd Time (UTC)	Initial Tests		Full Tests	
<u>Saturday</u>	<u>aix</u>	Download	24.5.0	51758	Test done	11Apr2015 09:29:07	385 runs 0 failures (q=0,s=0)	Report	3569 runs 1 failures (q=0,s=1)	Report
<u>Saturday</u>	deg	Download	24.5.0	51758	Test started	11Apr2015 01:47:52	619 runs 1 failures (q=1,s=0)	Report	results pending	
<u>Saturday</u>	<u>leg</u>	Download	24.5.0	51758	Test started	11Apr2015 02:01:21	647 runs 0 failures (q=0,s=0)	Report	results pending	
<u>Saturday</u>	legONdrcooper	Download	24.5.0	51758	Test done	11Apr2015 09:05:50	629 runs 0 failures (q=0,s=0)	Report	10832 runs 0 failures (q=0,s=0)	Report
<u>Saturday</u>	sig	Download	24.5.0	51758S	Test done	12Apr2015 04:24:15	493 runs 0 failures (q=0,s=0)	Report	7110 runs 0 failures (q=0,s=0)	Report
<u>Saturday</u>	vs8	Download	24.5.0	51758	Test started	11Apr2015 02:45:42	654 runs 0 failures (q=0,s=0)	Report	results pending	
Saturday	<u>wei</u>	Download	24.5.0	51758	Test started	11Apr2015 05:06:52	652 runs 0 failures (q=0,s=0)	Report	results pending	

l	nightly β	System	Libraries	Build	Rev	Status ar	nd Time (UTC)	Initial Tests		Full Tests	
	<u>Thursday</u>	<u>aix</u>	<u>Download</u>	24.4.4	51738	Test done	09Apr2015 17:39:11	394 runs 2 failures (q=0,s=2)	Report	3615 runs 3 failures (q=0,s=3)	Report
	<u>Monday</u>	deg	<u>Download</u>	24.4.4	51709	Test done	08Apr2015 19:01:03	602 runs 0 failures (q=0,s=0)	Report	13030 runs 0 failures (q=0,s=0)	Report



# **Nightly Quality Tests: Reports**



#### **GAMS System Builds and Test Results Archive**

Sunday 12Apr15 15:26 (UTC)

[ Latest Builds | Alpha Builds | Beta Builds | Nightly Builds | Glossary ]

```
Total:
                                  1 failures
               3569 runs
Quality:
                                  0 failures
               1117 runs
                                  1 failures
Slvtest:
               2339 runs
EMP:
                                  0 failures
                99 runs
                                  0 failures
Data:
                14 runs
**** SLVTEST FAILURES (failures slv.gms)
$call =gams slvtest lo=2 --prefix=aix --fail=failures slvI.gms --test=bchtlbas u1="ord(s)=286" --runall=no --c1=sbb --ftr
**** SLVTEST FAILURES DETAIL (slvtest.sum?)
 25020 04/11/15 05:45:16 bchtlbas
                                         MINLP
                                                              Bad ModelSolveStat[13,13] minlp=sbb
                                                 SBB
```



# **GAMS/CONVERT**

- Transforms a GAMS model instance into a scalar model into different formats: Models can then be passed on to others for investigation without confidentiality being lost
- A way of sharing GAMS test problems for use with other modeling systems or solvers
- ➤ More than 25 target formats

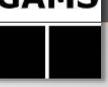
Generate an LGO Fortran file

Option	Description	LindoMPI	Generate Lindo N	/IPI file	lindo.mpi		
All	Generates all supported file formats	Lingo	Generate Lingo in	Generate Lingo input file			
AlphaECP	Generates AlphaECP input file	LocalSolver	Generate LocalS	olver input file (only with ConvertD)	localsolver.lsp		
Ampl	Generates Ampl input file	LSPSoI	Generate Output	function in LocalSolver input file (only with ConvertD)	lspsol.gms		
AmpINLC	Generate Ampl NLC compatible file	Memo	Generate a mem	o file containing model statistics and files created.	memo.txt		
Analyze	Generates three text files for rows columns and matrix	Minopt	Generate Minopt	input file	minopt.dat		
AnalyzeS	Generates short form of Analyze	— . — NLP2dual		Ife dual of a smooth optimization model	gamsdual.gms		
Baron	Generates Baron input file			· · · · · · · · · · · · · · · · · · ·			
CplexLP	Generate CPLEX LP format input file	NLP2MCP	Generates GAMS	S scalar MCP model	gamsmcp.gms		
CplexMPS	Generate CPLEX MPS format input file	OSiL	Generates Optim	ization Services instance Language (OSiI) file	osil.xml		
Dict	Generate Convert to GAMS Dictionary	Pyomo	Generates Pyom	o Concrete scalar model	gams.py		
DictMap	Generate Convert to GAMS Dictionary Map	SFS	Generates Solver	Foundation Services OML file	sfs.oml		
FileList	Generate file list of file formats generated	ViennaDag	Generate Vienna	Dag input file	vienna.dag		
FixedMPS	Generate fixed format MPS file		fixed.mps				
Gams	Cenerate CAMS scalar model. This is the default conversi	ion format used	game gme		<b>4</b> ) 80 ( <b>&gt;</b> )		

lgomain.for



# **GAMS/CONVERT - Example**



#### **GAMS Code**

#### Scalar Model

```
Variables
    x(i,j) shipment quantities in cases
    z    total transportation costs in thousands
Positive Variable x;
Equations
    cost         define objective function
        supply(i) observe supply limit at plant i
        demand(j) satisfy demand at market j;
cost ..     z === sum((i,j), c(i,j)*x(i,j));
supply(i) ..        sum(j, x(i,j)) === a(i);
demand(j) ..        sum(i, x(i,j)) =g= b(j);
Model transport /all/;
Solve transport using lp minimizing z;
```

```
Variables x1,x2,x3,x4,x5,x6,x7;

Positive Variables x1,x2,x3,x4,x5,x6;

Equations e1,e2,e3,e4,e5,e6;
e1.. - 0.225*x1 - 0.153*x2 - 0.162*x3 - 0.225*x4 - 0.162*x5 - 0.126*x6 + x7=E= 0;
e2.. x1 + x2 + x3 = L= 350;
e3.. x4 + x5 + x6 = L= 600;
e4.. x1 + x4 = G= 325;
e5.. x2 + x5 = G= 300;
e6.. x3 + x6 = G= 275;

Model m / all /;
m.limrow=0; m.limcol=0;
Solve m using LP minimizing x7;
```



# **Protecting IP and Sensitive Data**



## Obfuscate or hide sensitive information

- > Extrinsic function libraries
- External Equations
- Secure (encrypted) binary source files
- Obfuscated binary file: Obfuscates all names and other documentation related to a specific model instance



## **Obfuscated Binary File - Example**

## **Solver Log**

#### Normal

```
Reduced LP has 5 rows, 6 columns, and 12 nonzeros.
Presolve time = 0.00 sec. (0.00 ticks)
Iteration Dual Objective
                                        In Variable
                                                             Out Variable
                  73,125000
                                x(seattle.new-york) demand(new-york) slack
                  119.025000
                               x(seattle.chicago) demand(chicago) slack
                  153.675000
                                x(san-diego.topeka)
                                                    demand(topeka) slack
                              x(san-diego.new-york)
                                                     supply(seattle) slack
                  153.675000
LP status(1): optimal
```

#### **Obfuscated**









## **Obfuscated Binary File - Example**

## **Looking at Results**

## **Normal**

12	demand	Equ	1	3
6	f	Par	0	1
1	i	Set	1	2
2	j	Set	1	3
11	supply	Equ	1	2
8	x	Var	2	6
9	z	Var	0	1

		Level	Marginal
seattle	new-york	50	
	chicago	300	
	topeka		0.036
san-diego	new-york	275	
	chicago		0.00900000000000001
	topeka	275	

## **Obfuscated**

3	С	Par	1	2
4	D	Par	1	3
5	E	Par	2	6
6	F	Par	0	1
7	G	Par	2	6
8	Н	Var	2	6
9	I	Var	0	1

		Level	Marginal
"!!!!!!	"!!!!!!!	50	
	#!!!!!!!	300	
	"!!!!!		0.036
"!!!!!!!!!	"!!!!!!!	275	
	#!!!!!!!		0.00900000000000001
	"!!!!!	275	







# **Obfuscated Binary File - Example**



#### **New options**

- > saveobfuscate (so) and xsaveobfuscate (xso): generate obfuscated binary file (regular or compressed)
- restartNamed (rn): brings back original names when restarting from an obfuscated binary file

#### **Example**

- Compile GAMS model into named and obfuscated binary file: gams trnsport a=c s=0named saveobfuscate=0anon
- Move obfuscated binary file to non-secure machine, execute it, and save (obfuscated) to a gdx file: gams dummy r=0anon s=1anon gdx=demo
- ➤ Bring new (still obfuscated) save file with results back to safe machine and do continued compilation with reporting and export:

  gams dummy r=lanon restartNamed=0named gdx=res





## **Model2Tex**

#### Translates a GAMS model instance into Latex Format

# Sets i canning plants / seattle, san-diego / j markets / new-york, chicago, topeka Parameters a(i) capacity of plant i in cases b(j) demand at market j in cases c(i,j) transport cost in thousands of dollars pe Variables x(i,j) shipment quantities in cases z total transportation costs in thousands o Equations cost define objective function supply(i) observe supply limit at plant i demand(j) satisfy demand at market j;

z = e = sum((i,j), c(i,j)\*x(i,j));

gams trnsport docfile=trans model2tex trans

supply(i) .. sum(j, x(i,j)) = l = a(i);demand(j) .. sum(i, x(i,j)) = q = b(j);

Model transport /all/;

#### Symbols

#### Sets

Name	Domains	Description
i	*	canning plants
j	*	markets

#### Parameters

Name	Domains	Description	
a	i	capacity of plant i in cases	
Ъ	j	demand at market j in cases	
c	i, j	transport cost in thousands of dollars per case	

#### Variables

Name	Domains	Description	
X	i, j	shipment quantities in cases	
z	1240540	total transportation costs in thousands of dollars	

#### Equations

Name	Domains	Description	
cost		define objective function	
supply	i	observe supply limit at plant i	
demand	j	satisfy demand at market j	

#### **Equation Definitions**

#### cost

$$\mathbf{z} = \sum_{i,j} (\mathbf{c}_{i,j} \cdot \mathbf{x}_{i,j})$$

#### supply,

demand,

$$\sum_{j} (\mathbf{x}_{i,j}) \leq \mathbf{a}_i$$

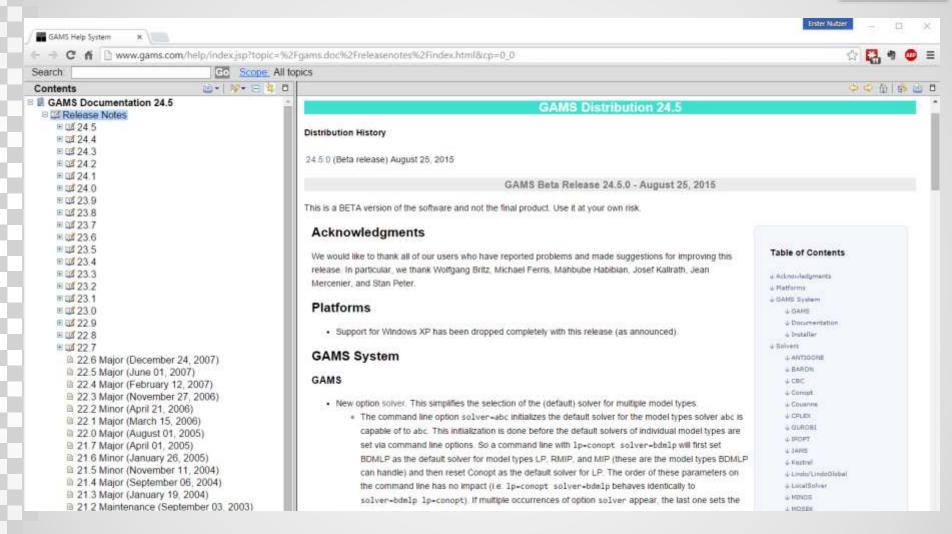








## What else is new?









# Summary

# GAMS – Elements, Examples, and Enhancements

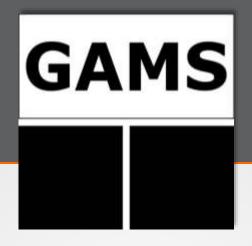
- Simple, but powerful language
- Designed to **interact**, different **layers** (platform, solver, data, interface)
- Evolution through more than 35 years of R&D and user feedback
- Maturity through experience and rigorous testing

## Striving for Innovation and Compatibility

- Provide cutting edge technology
- Increase productivity
- Don't lock developers and users into a certain environment
- Protect investments of users







# **Thank You**

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