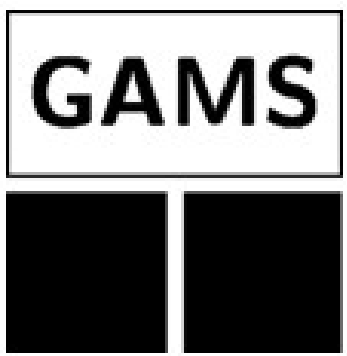
Hooking your solver to GAMS

The COIN-OR/GAMSlinks project

Michael Bussieck Stefan Vigerske



INFORMS Annual Meeting, Washington D.C.
12.10.2008

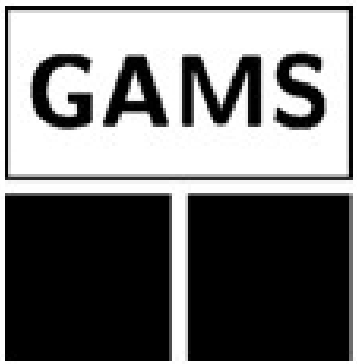
Overview

Background

Goals of the COIN-OR / GAMSlinks project:

- easy access to open source solvers (mainly from COIN-OR) via GAMS
  - ⇒ broadening the audience of COIN-OR
  - ⇒ broadening the audience of GAMS
- help developers to connect their solvers to GAMS
- provide access to GAMS benchmarking and quality assurance tools

www.coin-or.org



www.gams.com

https://projects.coin-or.org/GAMSlinks

Timeline

2004 Michael Bussieck: links to GLPK and COIN-OR/CBC (code is public)

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Aug. '07	link to general OSI solver (rudimentary links to Symphony, DyLP, Volume)
Dec. '07	link to Optimization Services (OSiL, OSrL)
Jan. '08	support of GAMS Branch-Cut-Heuristic (BCH) facility for CBC

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now	6 supported platforms: Linux (Intel 32+64 bit), Solaris (Intel 64bit), MacOS (Intel PowerPC), Windows (32+64 bit)

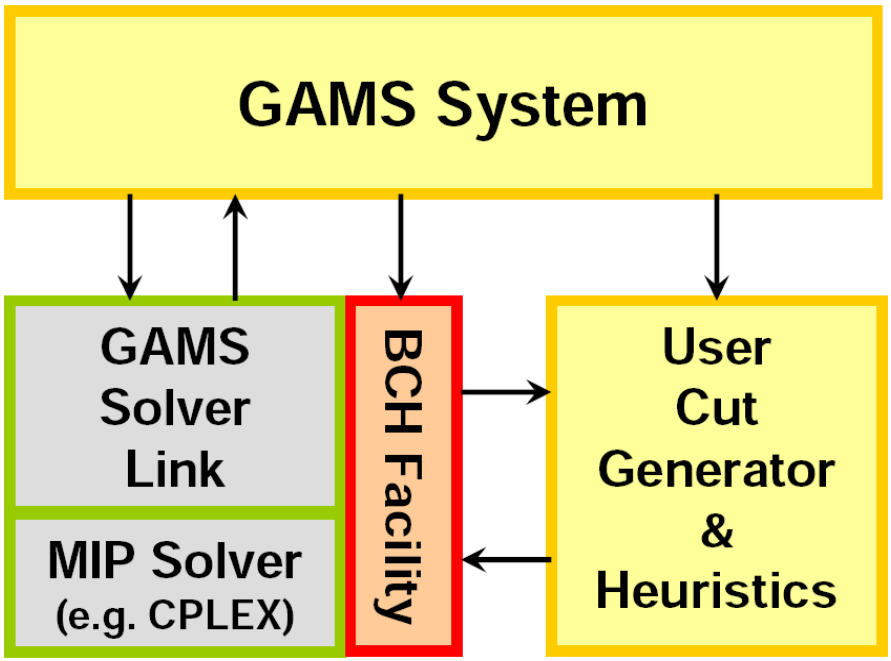
Overview

Branch-Cut-Heuristic Facility

BCH Facility: pass solver callbacks back into GAMS model space

http://www.gams.com/docs/bch.htm

- represent cut generator and heuristic in terms of original GAMS formulation
- independent of specific MIP solver
- can use any other solver in GAMS for computations



Availability:

CBC	cutting planes and heuristics
SCIP	cutting planes, heuristics, and incumbent report callback
BONMIN B&B	heuristics
BONMIN Hyb+OA	cutting planes and heuristics

Example: Trim Loss Minimization

Reference: I. Harjunkoski, T. Westerlund, R. Porn, H. Skrifvars. Different Transformations for Solving Non-Convex Trim Loss Problems by MINLP. EJOR 105 (1998), 594–603. `http://www.gams.com/modlib/libhtml/bchtlbas.htm`

- The task is to cut out some paper products of different sizes from a large raw paper roll, in order to meet a customer's order.
- nonconvex MINLP (bilinear terms)
- Heuristic:

	best solution	bound
Bonmin alone	–	87.6
Bonmin w/ user heu.	112.1	87.6
SBB alone	–	88.4
SBB w/ user heu.	107.5	88.1

Timelimit: 30 minutes

Example: Difficult Network Problem

Single-commodity, uncapacitated, fixed-charge network flow problem:

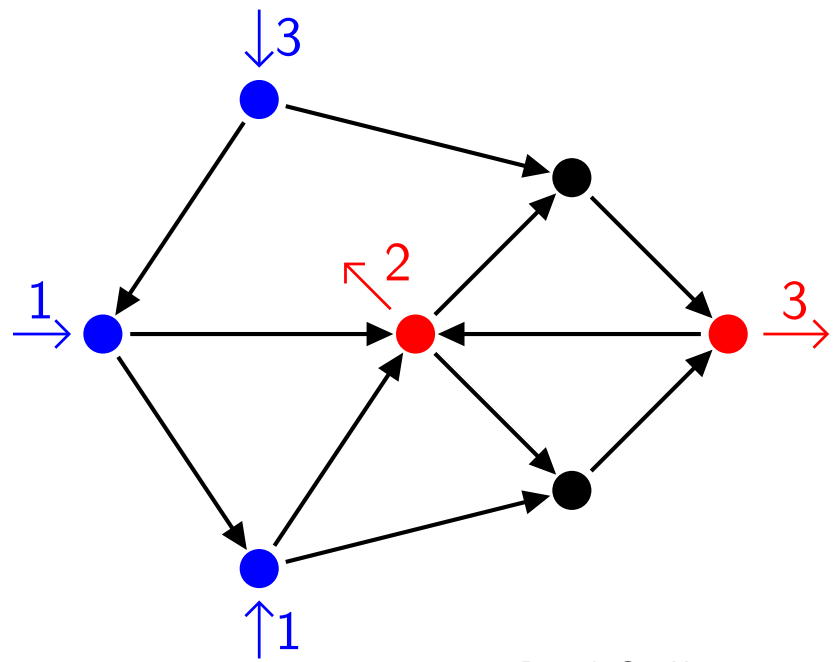
$$\min \sum_{(i,j)\in A} f_{ij}y_{ij} + c_{ij}x_{ij}$$

$$\text{s.t.} \sum_{(j,i)\in\delta^-(i)} x_{ij} - \sum_{(i,j)\in\delta^+(i)} x_{ij} = b_i, \qquad i \in V$$

$$0 \le x_{ij} \le My_{ij}, \quad y_{ij} \in \{0,1\}, \qquad (i,j) \in A$$

Reference: F. Ortega, L. Wolsey, A branch-and-cut algorithm for the single-commodity, uncapacitated, fixed-charge network flow problem. Networks 41 (2003), No. 3, 143-158

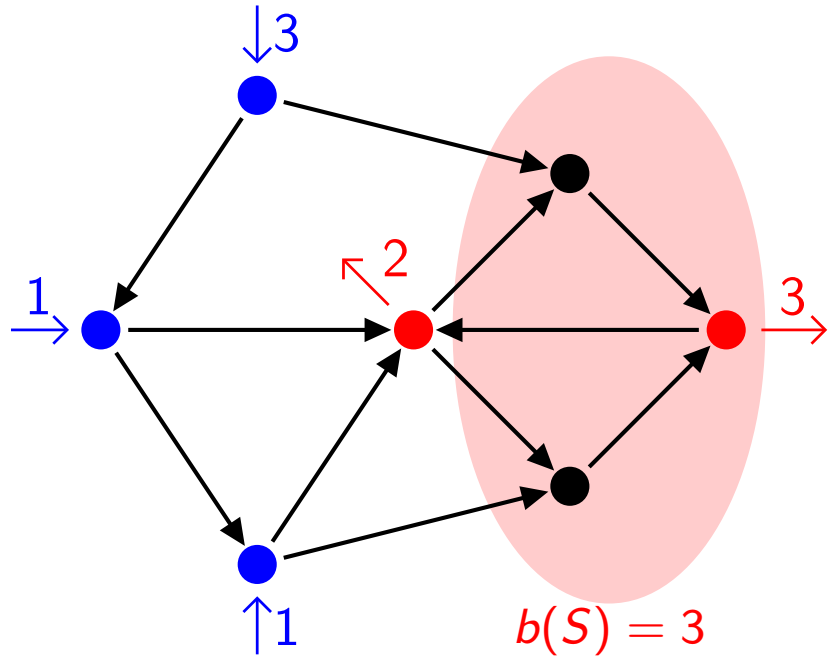
`www.gams.com/modlib/libhtml/bchfcnet.htm`



Simple Dicut Inequalities

Dicut: For $S \subset V$ with $b(S) > 0$:

$$\sum_{(i,j) \in \delta^-(S)} y_{ij} \geq 1$$



Simple Dicut Inequalities

Dicut: For $S \subset V$ with $b(S) > 0$:

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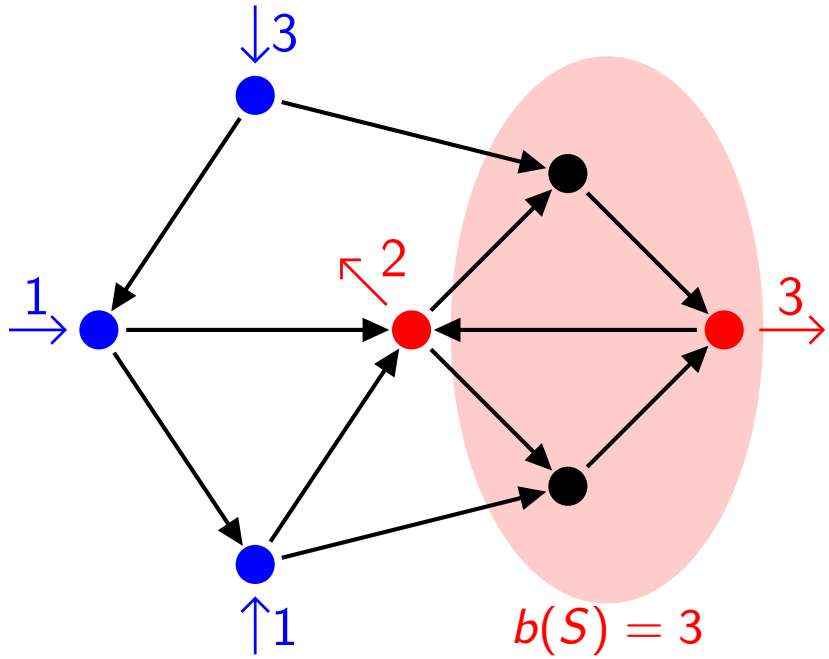
Separation problem: find a good set S

$$\begin{aligned} \min \quad & \sum_{(i,j)\in A} \bar{y}_{ij} z_j (1 - z_i) \\ \text{s.t.} \quad & \sum_{i\in V} b_i z_i > 0 \\ & z_i \in \{0,1\}, \quad i \in V \end{aligned}$$



$\Rightarrow$ nonconvex quadratic binary program

$\Rightarrow$ let's use GAMS MIQCP solver

Example: Berlin52 Instance

Instance: Berlin52 (SteinLib): 52 nodes (1 source, 15 sinks), 1326 edges

Note: There are more efficient ways to solve Steiner tree problems...

Solver: SCIP 1.0

	no BCH		
# cuts	0		
# nodes	1470		
Time [s]	1000		
Gap	209.42%		

(Pentium IV 3GHz, 1GB, Linux 2.6.11, gcc 3.3.5)

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Cuts: at most 20 cuts per round

	no BCH	with BCH using CPLEX
# cuts	0	316
# nodes	1470	1
Time [s]	1000	1000
Gap	209.42%	81.67%

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Cuts: at most 20 cuts per round (stop BARON when 20 solutions have been found)

	no BCH	with BCH using CPLEX	with BCH using BARON
# cuts	0	316	610
# nodes	1470	1	1
Time [s]	1000	1000	268
Gap	209.42%	81.67%	0%

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Overhead of BCH $\approx$ wall clock time – time in SCIP – time in BARON

126s (47%) 268s 124s 18s

Computational Experience

FCNetLib: `http://www.gamsworld.org/performance/fcnetlib`

- 83 instances from Wolsey's web page
  (`http://www.core.ucl.ac.be/wolsey/ufcn.htm`)
- translated into GAMS models with 83 data files (by Alexey Koptsevich)
- rerun BCH benchmarks originally done by Alexey Koptsevich (2004)

Detailed Results: `http://www.coin-or.org/GAMSlinks/benchmarks`

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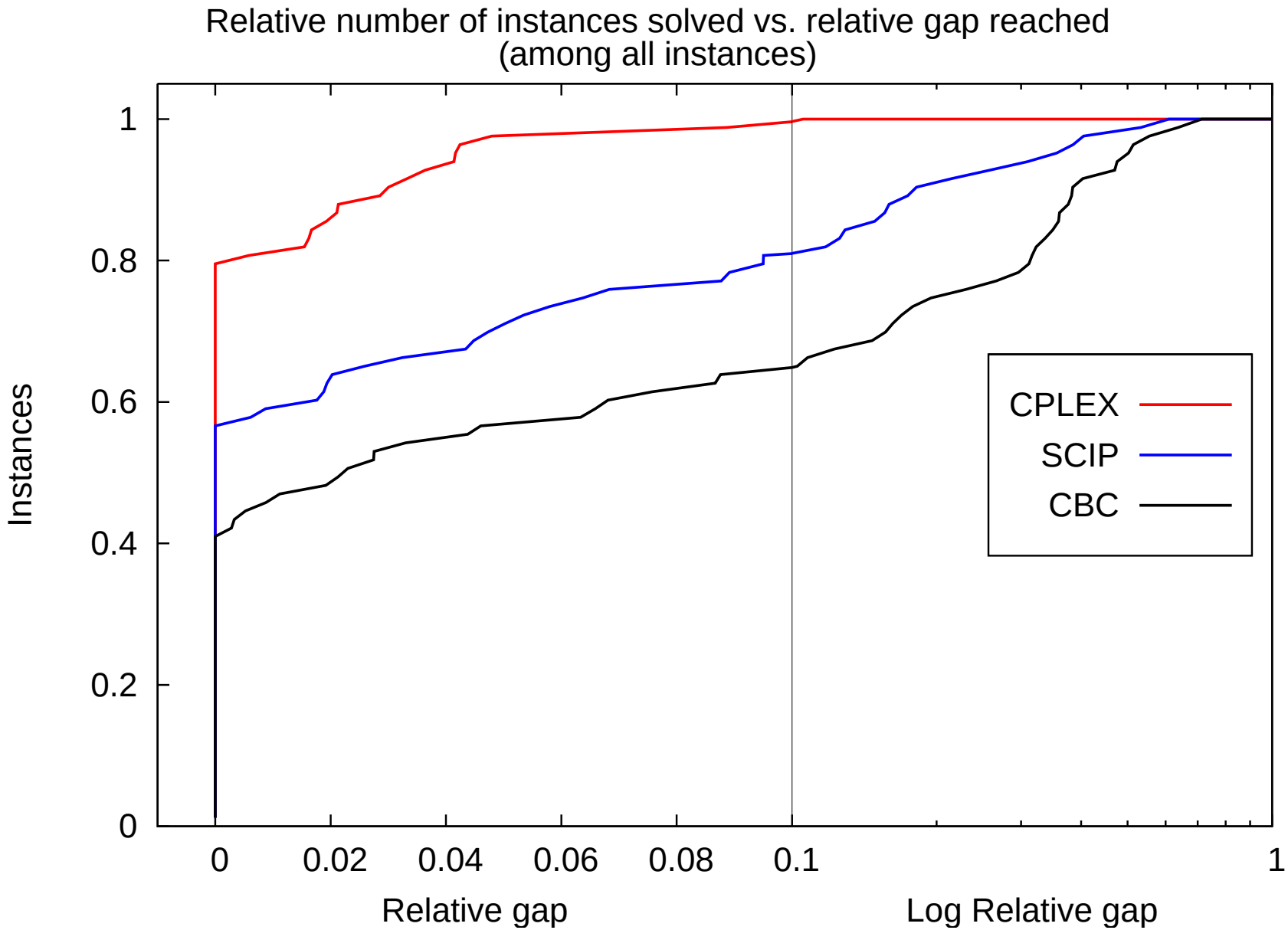
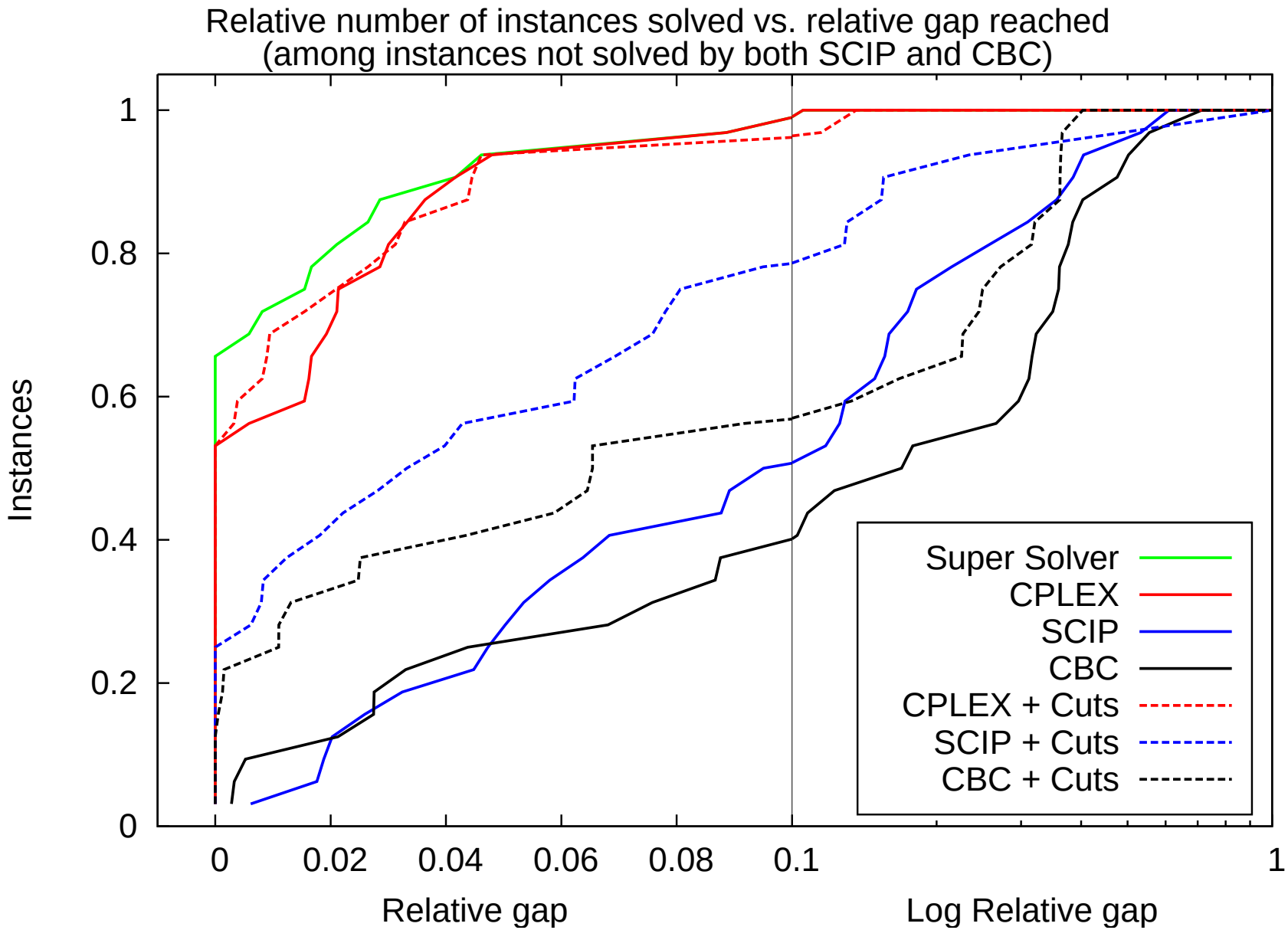
Computational Environment:

- Intel Core2 Duo T7500, 2 GB, Linux 2.4.16, GCC 4.2.1
- GAMS 22.6, CPLEX 11.0.0, CBC 2.1, SCIP 1.0
- Timelimit: 30 minutes

Results: no dicuts, all instances



Results: with dicuts, only difficult instances (32)



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Testing a solver with the GAMS model libraries

Testlib Library:

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- E.g. `lp03.gms`: examine behavior of LP solver on model with many free variables and when it restarts from an optimal basis
- `quality.gms`: driver for quality tests of all sorts
- Number of failed tests of GAMS / COIN-OR solvers on testsuites:

	LP (12)	MIP (5)	QCP (4)	NLP (2)
BONMIN	0	0	0	0
CBC/CLP	2	0	–	–
GLPK	0	0	–	–
IPOPT	0	–	0	0
SCIP	0	2	0	0

(date: 09.10.2008)

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Model Library:

- a collection of small to medium-size models from various applications
- `gmstest.gms`, `slvtest.gms`: runs solvers on models and checks results

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Both test libraries are part of the tests in the COIN-OR nightly builds.

Overview

The GAMS World (www.gamsworld.org)

A collection of many worlds:

- CONE World: Conic Optimization
- GLOBAL World: Global Optimization of NLPs
- MINLP World: Mixed Integer Nonlinear Programming
- MPEC World: Mathematical Programs with Equilibrium Constraints
- MPSGE World: Mathematical Programming System for General Equilibrium
- Translation: translate GAMS models into other languages
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Detail for benchmarks from next slides at
`http://www.coin-or.org/GAMSlinks/benchmarks`

MIP Benchmarks

Benchmark Setting:

- all MIPs from LINLib (incl. miplib3) $\Rightarrow$ 125 models
- Competitors:
  - CPLEX 11.1.1
  - CBC 2.2
  - SCIP 1.1 (with CLP 1.8)
  - SCIP 1.0 (with CLP 1.8)
  - GLPK 4.30
- timelimit: 1 hour
- gap tolerance: 0%

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- timelimit: 1 hour
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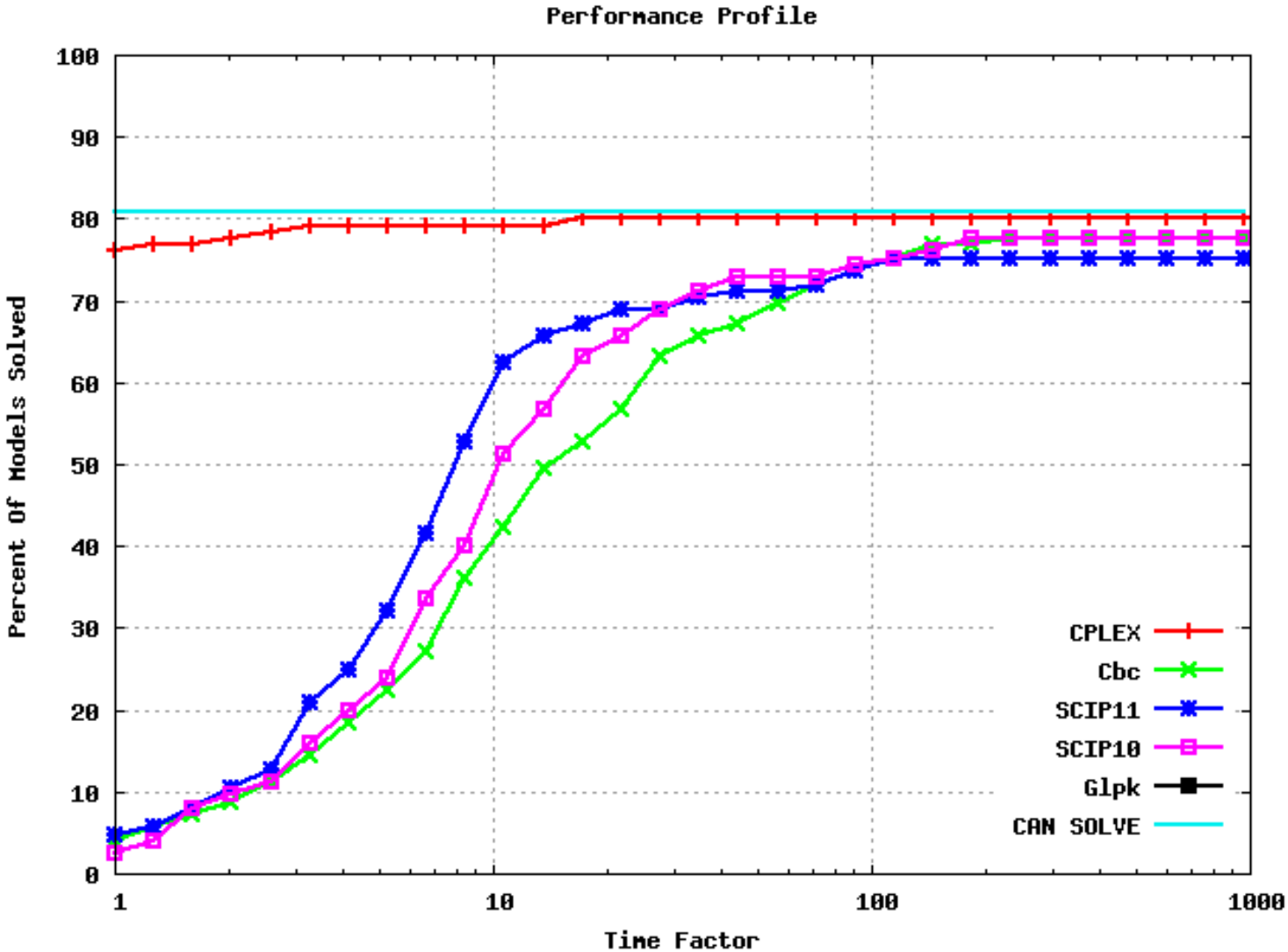
Results:

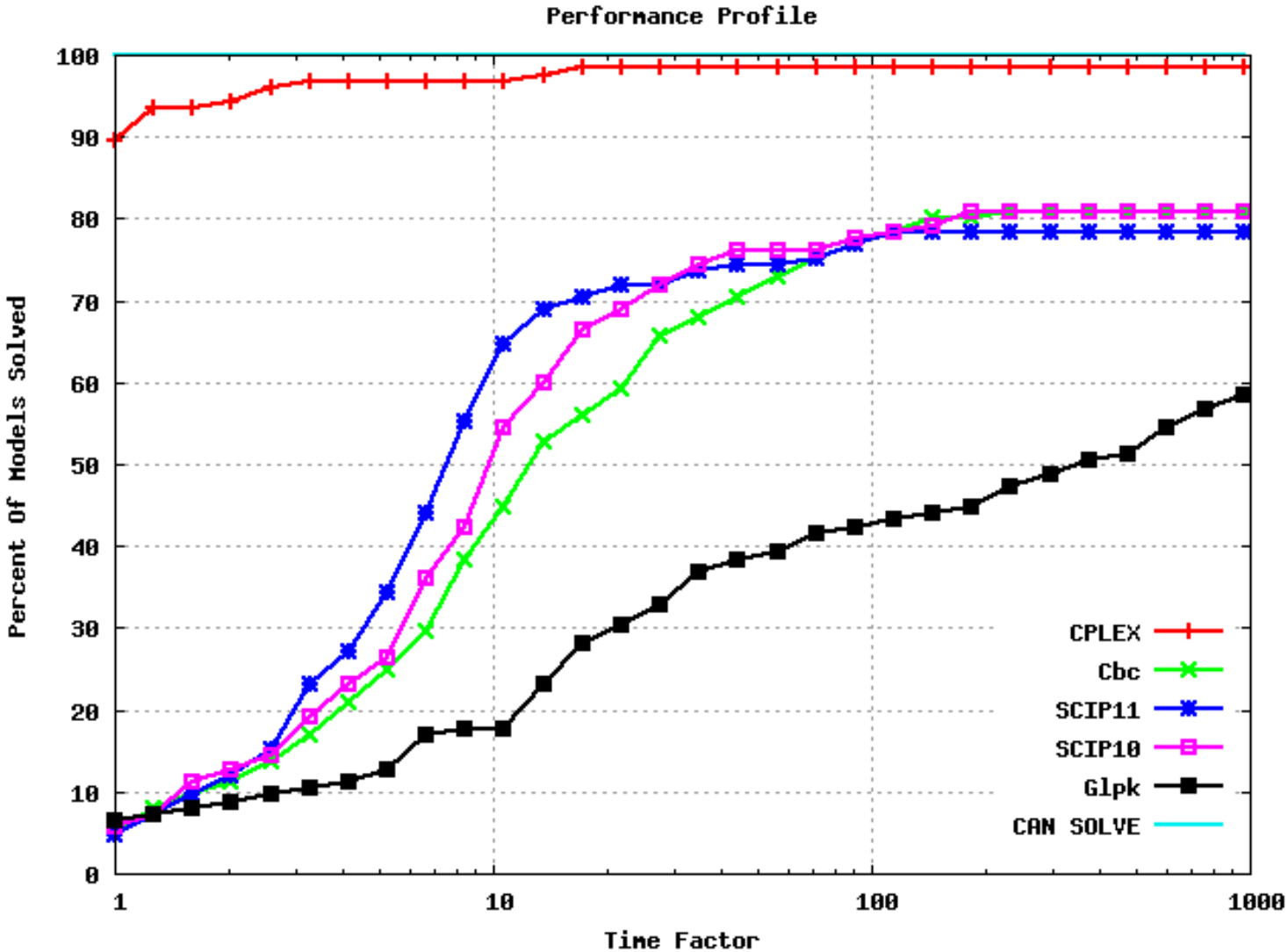
	CPLEX	CBC	SCIP 1.1	SCIP 1.0	GLPK
solved to optimality	80.0%	77.6%	75.2%	77.6%	48.8%
integer feasible solution found	19.2%	22.4%	24.8%	20.8%	48.0%
no solution – timelimit exceeded				1	3
no solution – failed	1			1	1

MIPs from LINLib - Performance profile



- solved = gap closed to 0% (and found best solution among all solvers)
- GLPK not included because no report of dual bound

MIPs from LINLib - Performance profile



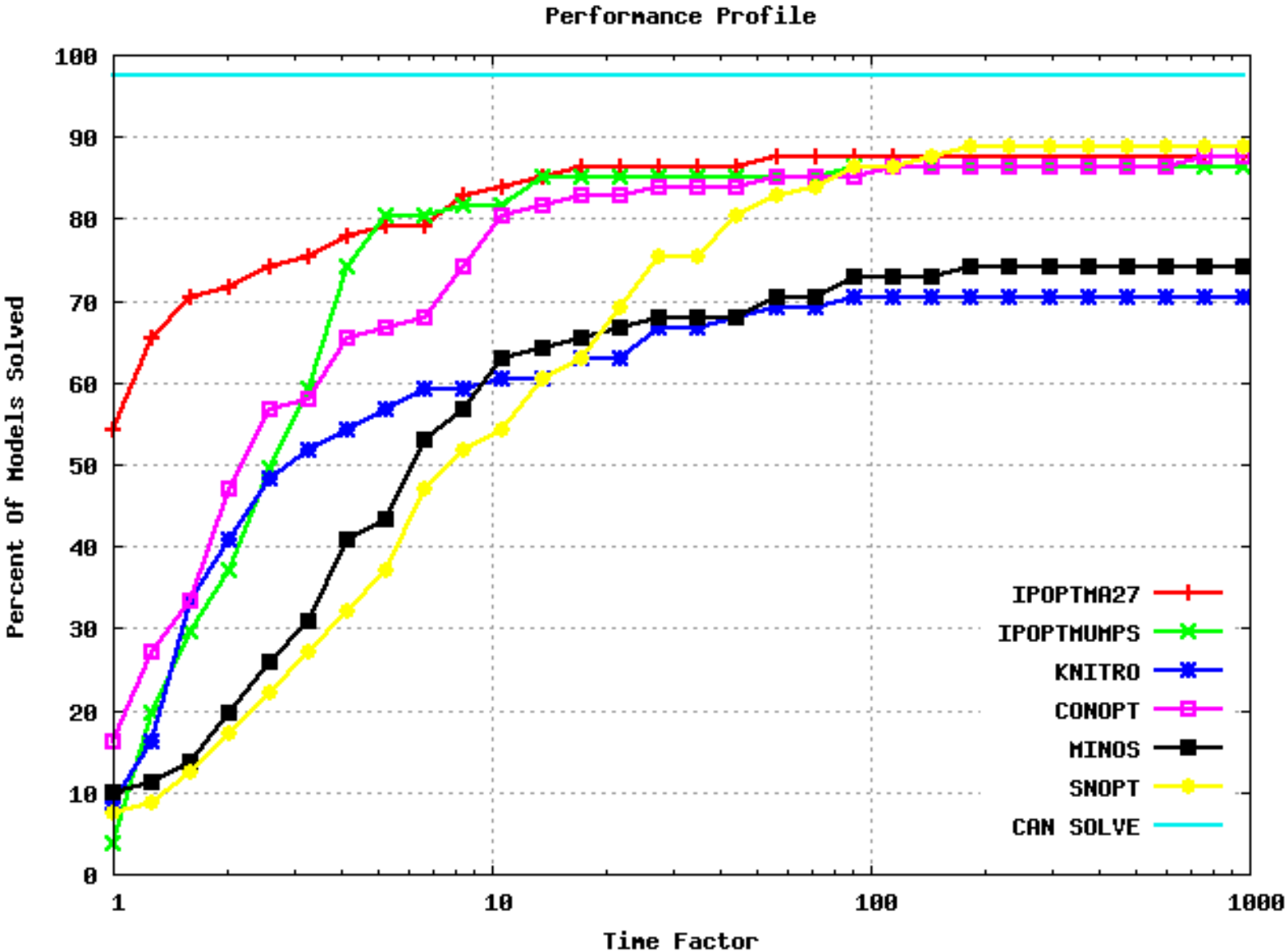
- solved = found best solution among all solvers
- performance profile visualizes only quality of primal bound

NLP Benchmarks

Benchmark Setting:

- 81 models with at least 1000 nonlinear nonzeros from the GAMS GlobalLib
- Competitors:
  - IPOPT 3.5 with MA27
  - IPOPT 3.5 with MUMPS 4.8.2
  - KNITRO 5.1.2
  - CONOPT 3.14S
  - MINOS 5.51
  - SNOPT 7.2-4
- timelimit: 1 hour
- relative tolerance: 10^{-8}

81 NLPs from GlobalLib - Performance profile



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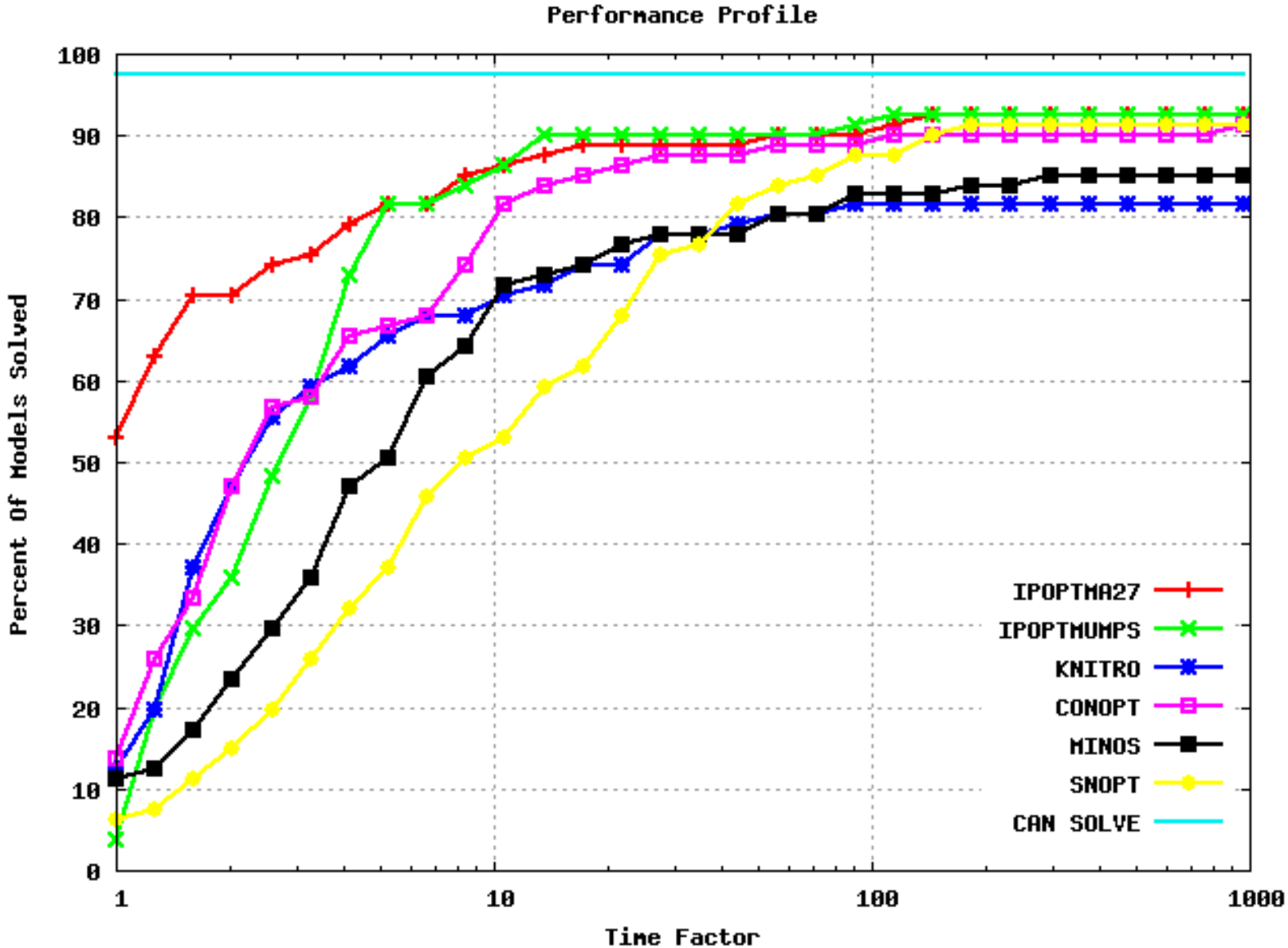


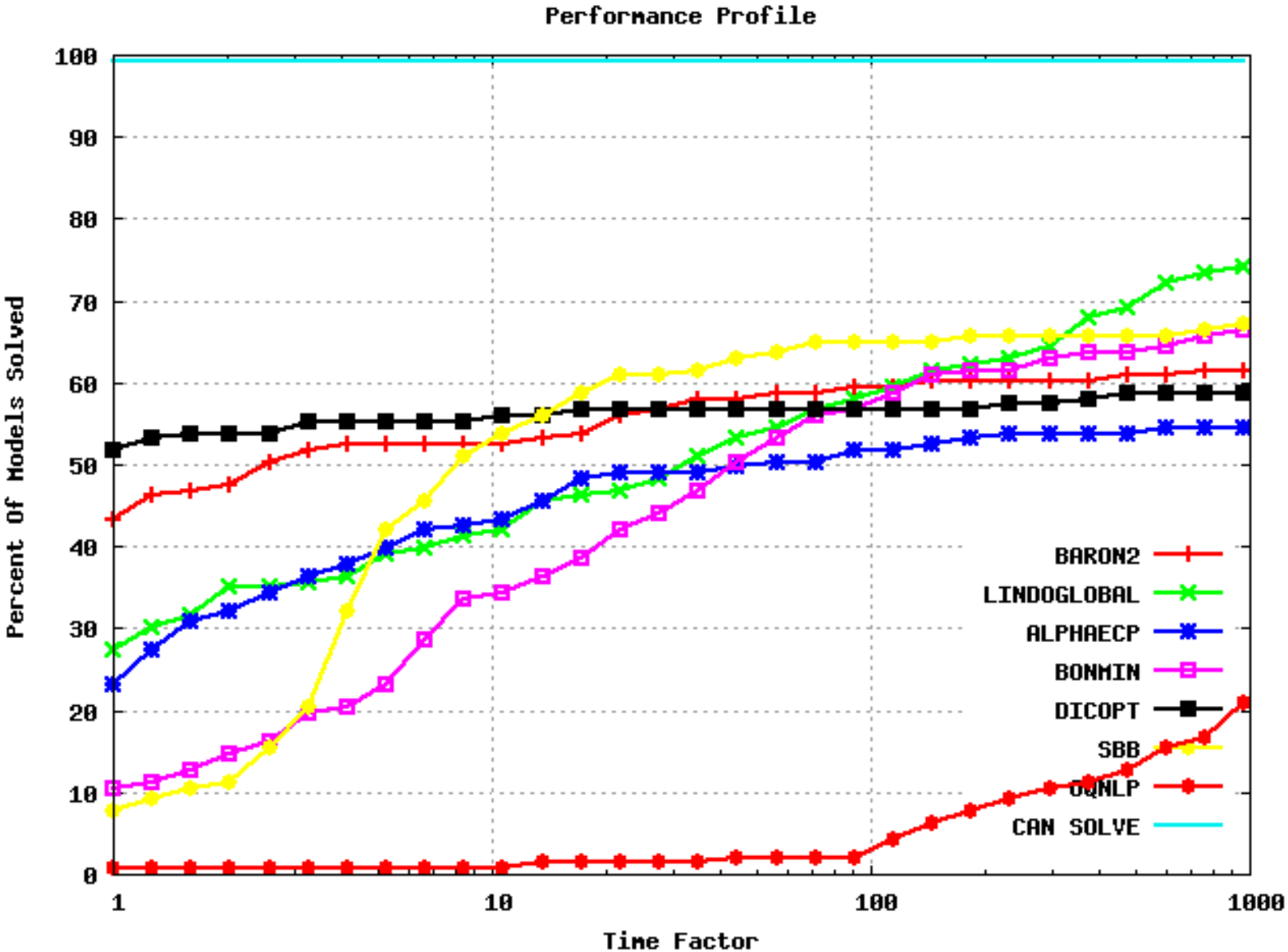
- solved = found a feasible solution

MINLP Benchmarks

Benchmark Setting:

- 143 models from the GAMS MINLPLib
- Competitors:
  - BARON 8.1.5
  - LINDOGLOBAL 5.0.1.292
  - AlphaECP 1.63
  - BONMIN 0.99
  - DICOPT 2x-C
  - SBB
  - OQNLP
- timelimit: 1 hour
- gap tolerance: 1%

143 MINLPs from MINLPLib - Performance profile



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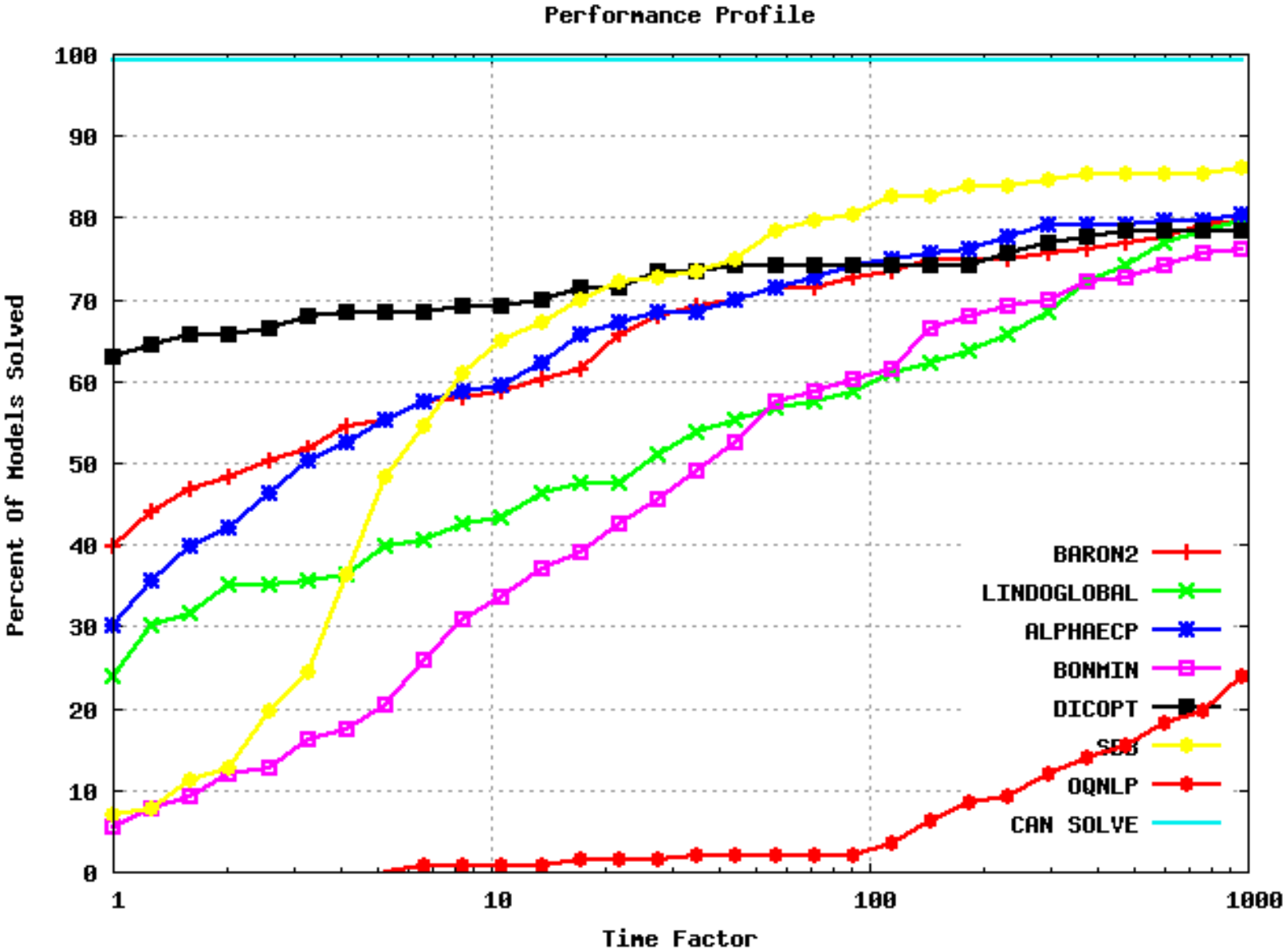
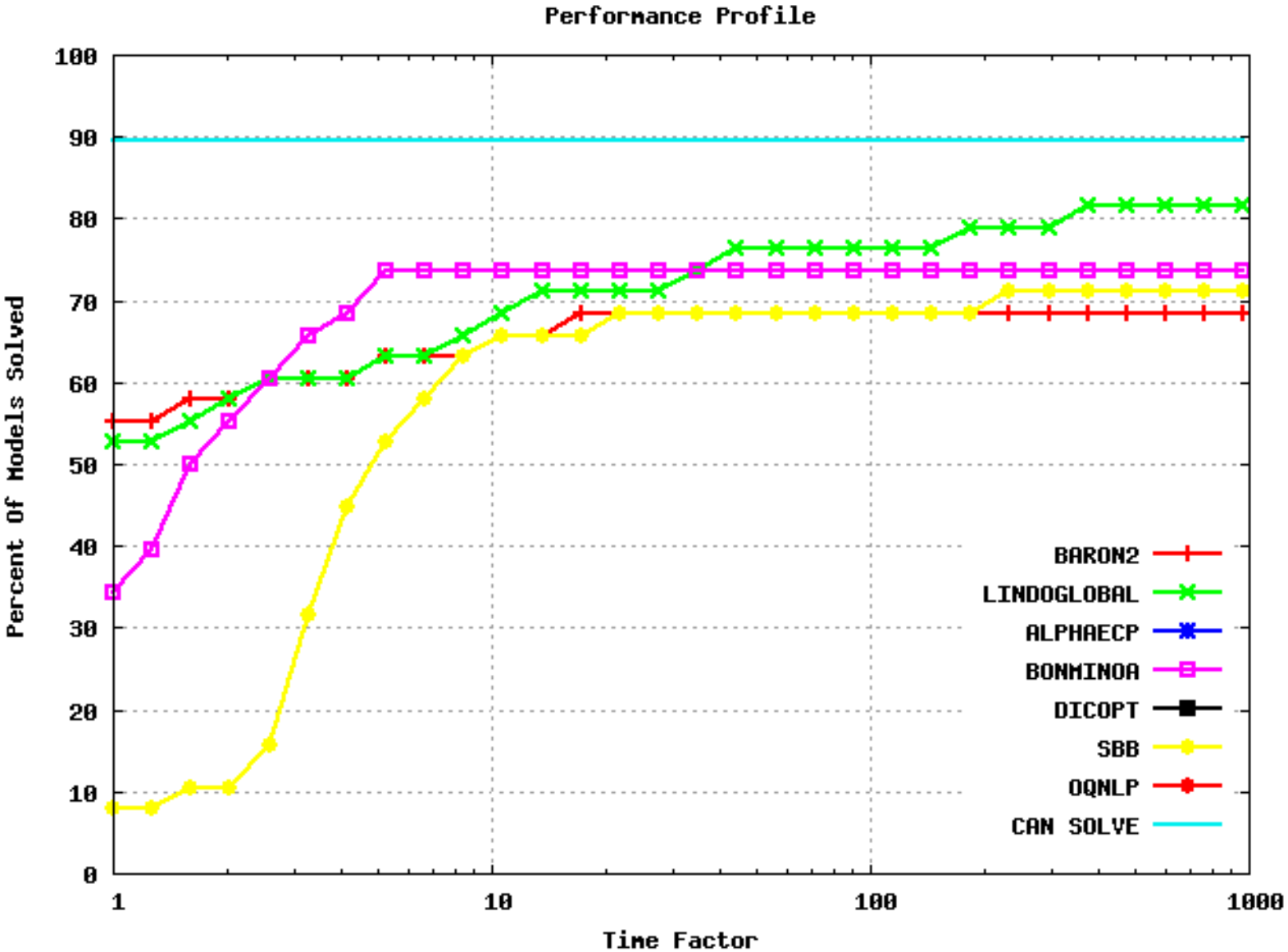


- solved = found a feasible solution

38 convex MINLPs from MINLPLib - Performance profile



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Overview

GAMS I/O libraries

precompiled GAMS I/O libraries via `GAMSlinks/ThirdParty/GAMSIO/get.GAMSIO`

supported architectures:

- Linux on 32- and 64-bit x86-CPUs with GNU or Intel compilers
- Solaris on 64-bit x86-CPUs with GNU compiler
- MacOS on x86-CPUs with GNU or Intel compiler
- Windows 64-bit x86 with Intel Compiler
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- IOLib: used for CBC, GLPK, OSI
- SMAG: used for Ipopt, Bonmin, SCIP, OS

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several choices for accessing GAMS models:

- IOLib: used for CBC, GLPK, OSI
- SMAG: used for Ipopt, Bonmin, SCIP, OS
- GMO: will replace IOLib and SMAG
  - distributed with newer GAMS systems
  - interfaces to C, C++, C#, Delphi, Fortran90, Java, VisualBasic
  - easier to link against than IOLib or SMAG
  - more than just an I/O library

Classes in the GAMSlinks project

GamsModel: (IOLib)

- hides IOLib functions, allows easy access to a linear mixed-integer model
- provides an OSI - compatible problem representation
- writes GAMS solution file given OSI object or primal/dual values, basis status, status codes, ...

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GamsOptions: (IOLib, SMAG)

- easy access to GAMS option file reader

Classes in the GAMSlinks project

GamsModel: (IOLib)

- hides IOLib functions, allows easy access to a linear mixed-integer model
- provides an OSI - compatible problem representation
- writes GAMS solution file given OSI object or primal/dual values, basis status, status codes, ...

GamsDictionary: (IOLib, SMAG)

- access to variable and equation names and texts

GamsOptions: (IOLib, SMAG)

- easy access to GAMS option file reader

GamsMessageHandler, SmagJournal: (IOLib, SMAG)

- redirects output into GAMS output channels (logfile, statusfile)

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GamsGDX (in development): (IOLib, SMAG)

- reads and writes files in GAMS Data Exchange format

Gams Modeling Object: Instance → Solver

Access a model and write solution file via GMO:

```
gmoLoadInfoGms          Load Gams control file
gmoLoadDataGms          Load model data defined by control file

gmoM                    Number of equations
gmoN                    Number of variables

gmoGetVarLower          Get variable lower bounds
gmoGetMatrixRow         Get constraint matrix in row order

gmoEvalFunc             Evaluate the constraint i
gmoEvalGrad             Update nonlinear gradients of constraint
gmoEvalHessLag          Evaluate Hessian of Lagrangian

gmoSetSolution          Set solution values
gmoUnloadSolutionGms    Unload solution to the Gams solution file
...
```

Gams Modeling Object: Solver → Instance

Create or modify a model via GMO:

```
gmoInitData              Initializes GMO data
gmoAddRow                Add a row
gmoAddCol                Add a column

gmoSetAltRHS             Set alternative RHS
gmoSetAltVarBounds       Set alternative variable bounds

...
```

Gams Modeling Object: Solver → Instance

Create or modify a model via GMO:

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gmoSetAltRHS             Set alternative RHS
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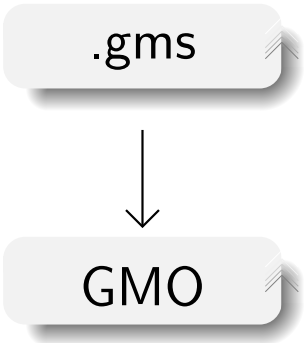
...
```

Solve a GMO instance with a GAMS solver:

```
conReadyAPI        Define the conopt API and load the option object
conCallSolver      Call conopt

cpxReadyAPI        Define the cplex API and load the option object
cpxModifyProblem   Update Cplex object with rhs, obj, bounds, jac.
cpxCallSolver      Call cplex
```

GAMS / GMO / Optimization Services (OS)



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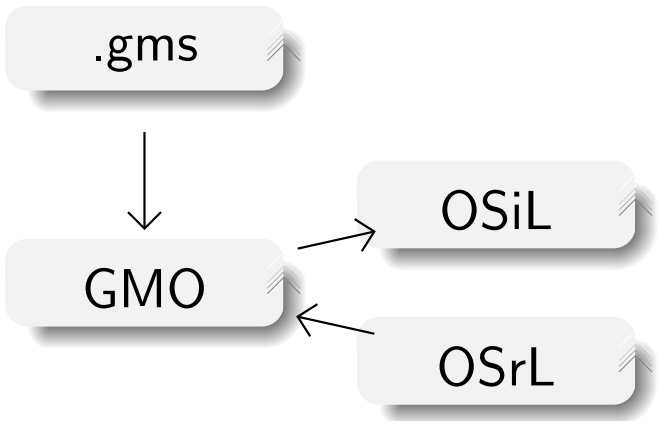

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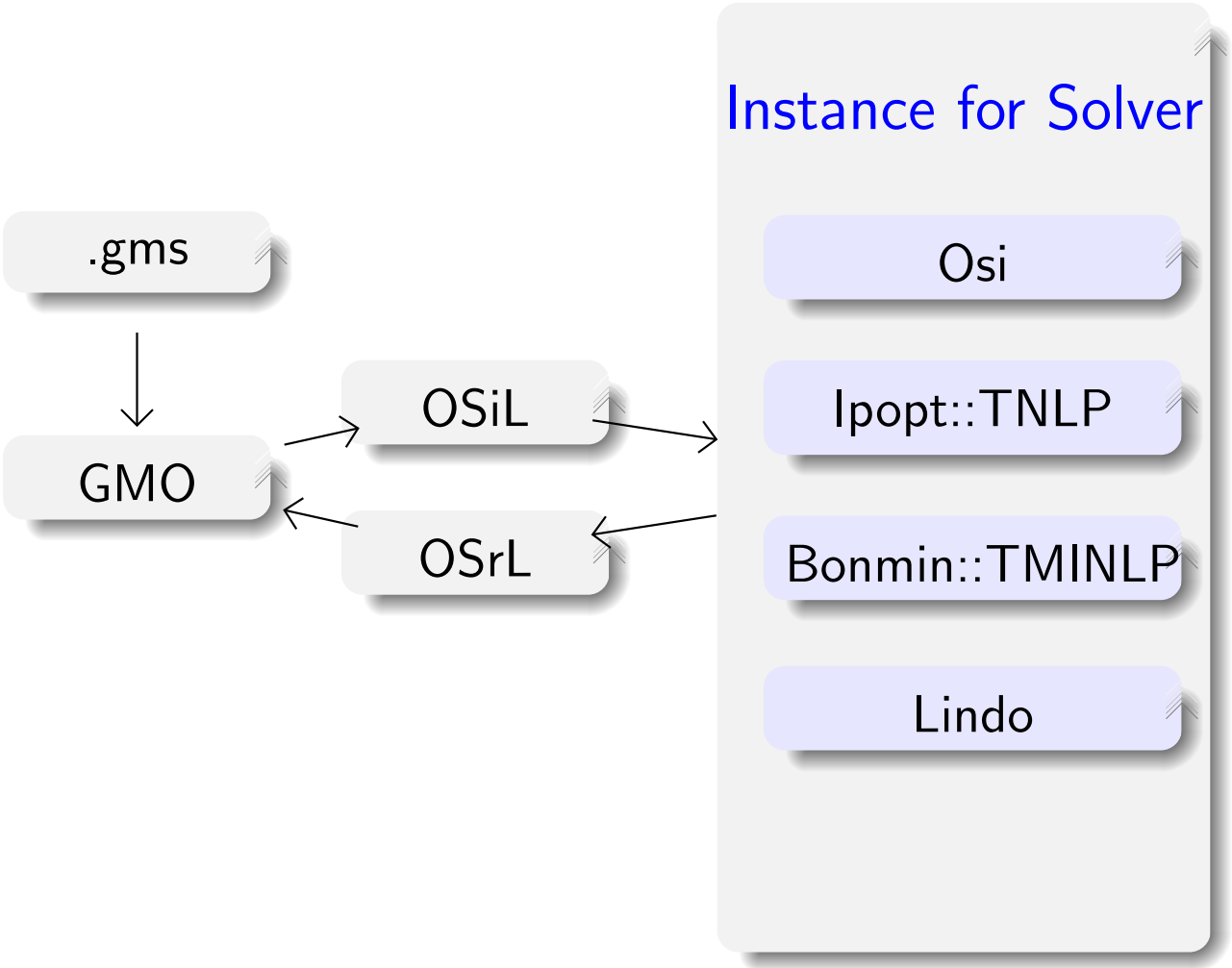

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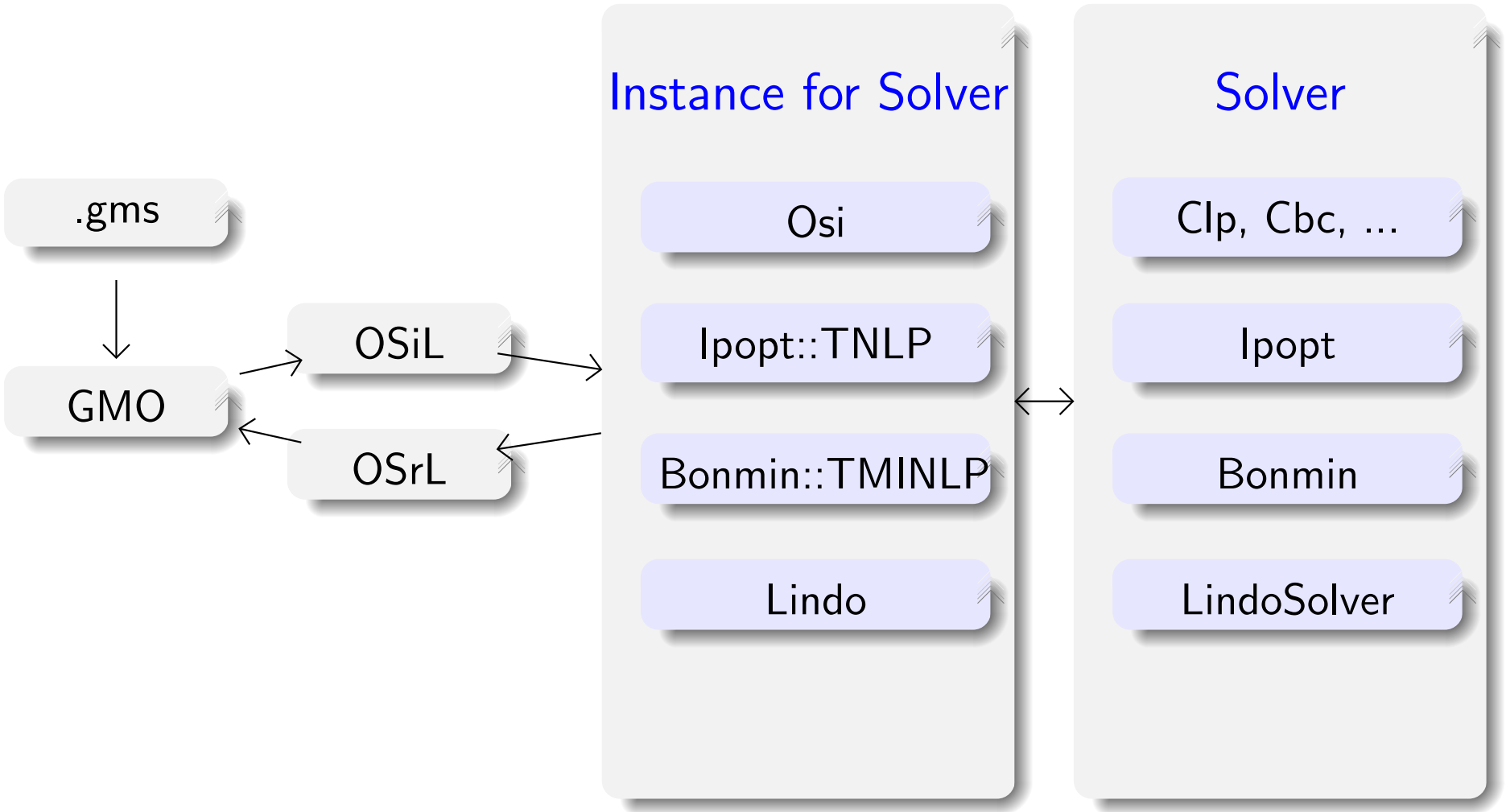

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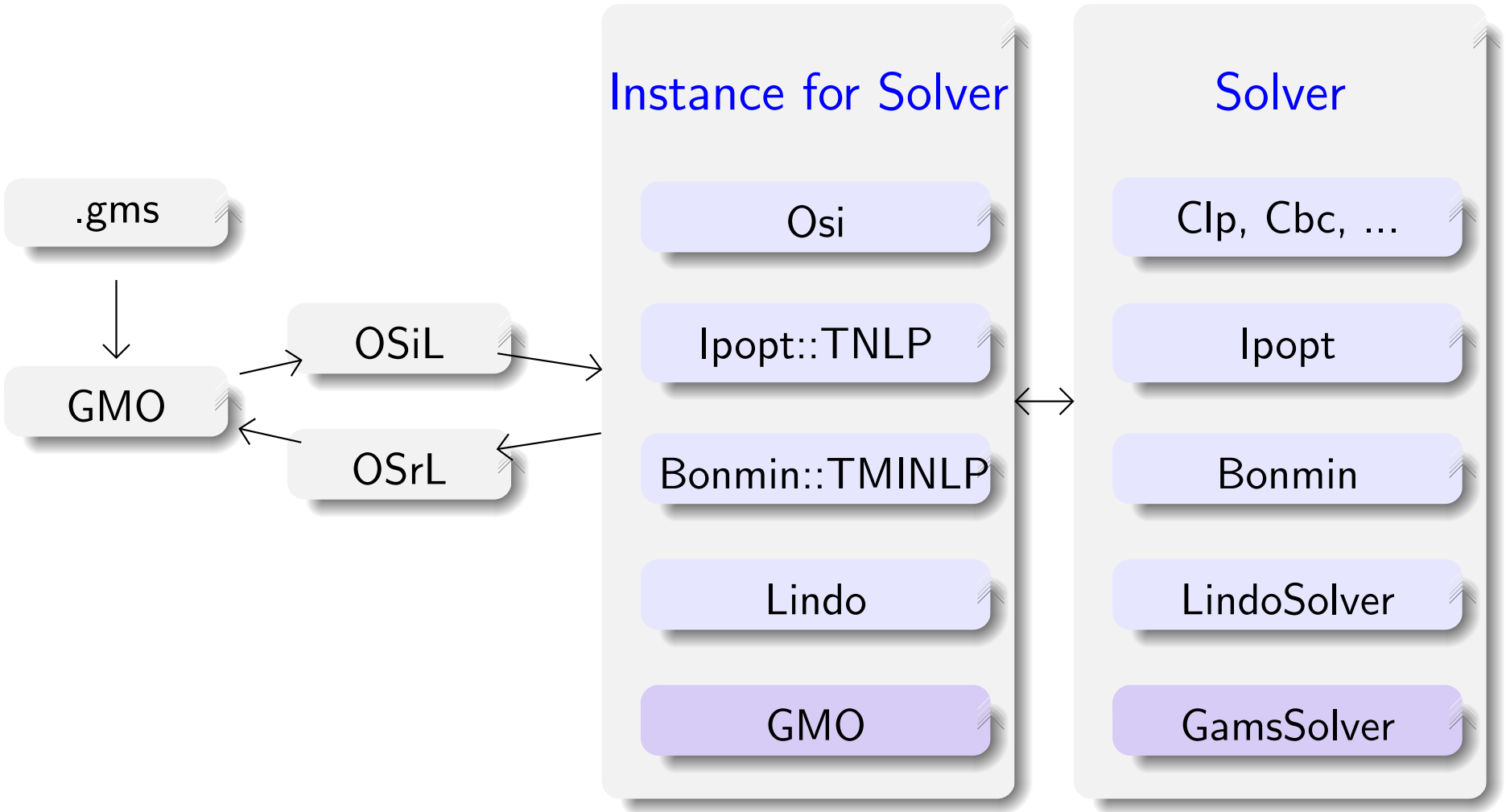

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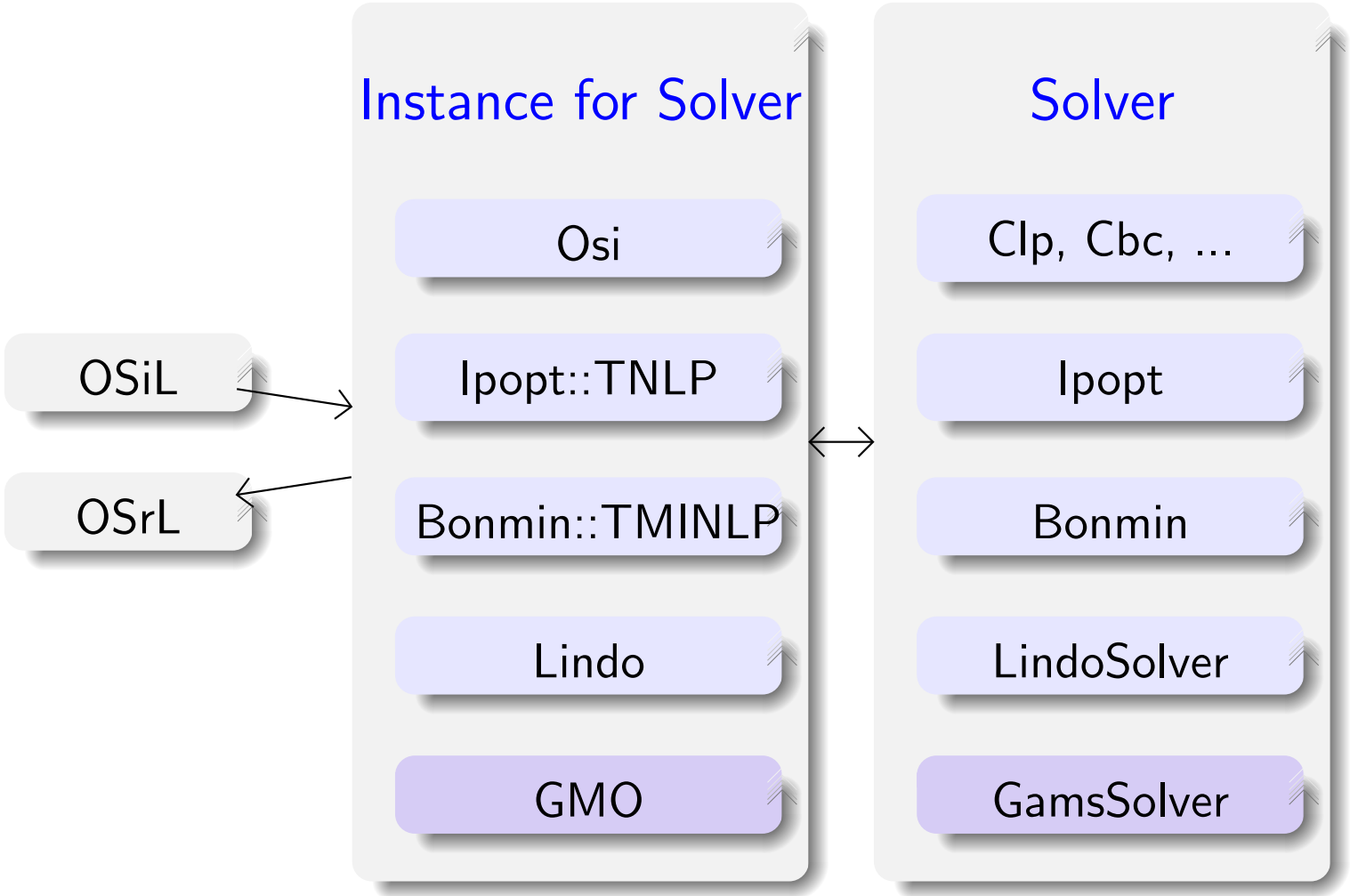


That's it.

Thanks!

PS: GAMS evaluation licences (2 months, all solvers) at

- `http://www.gams.com/evals/dc/l/gamslice.txt` (Linux)
- `http://www.gams.com/evals/dc/m/gamslice.txt` (MacOS X)
- `http://www.gams.com/evals/dc/w/gamslice.txt` (Windows)

Performance Profiles

E.D. Dolan and J.J. More, Mathematical Programming, 91, 2002:

- compare performance of solver $s \in \mathcal{S}$ on problem $p \in \mathcal{P}$ with best performance by any solver on problem p:

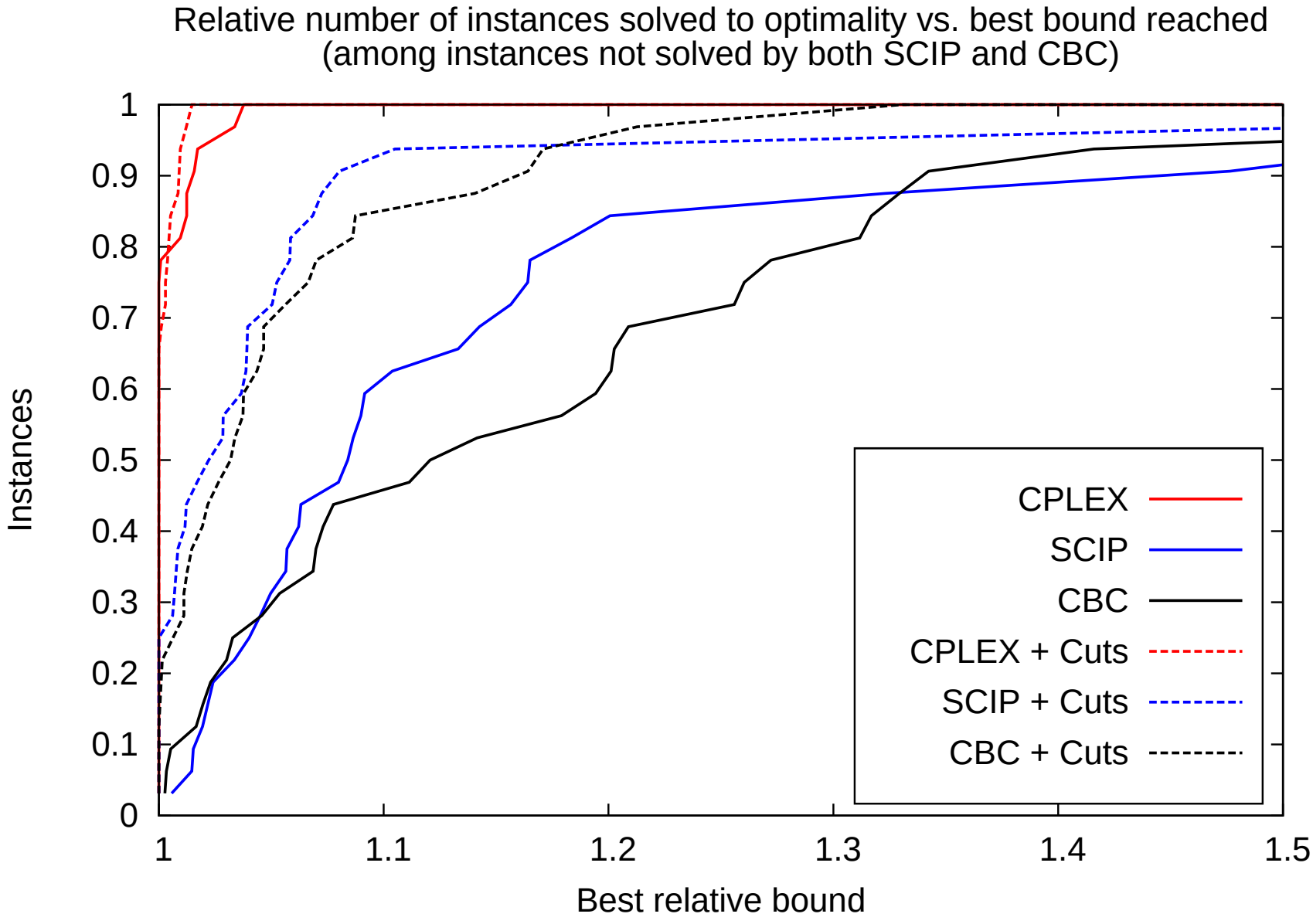
$$\rho(p,s) := \frac{t_{p,s}}{\min_{s' \in \mathcal{S}} t_{p,s'}}$$

- $t_{p,s}$ = time solver s spend on p, $\quad t_{p,s} = \infty$ if s did not *solve* p
- $P_s(\tau)$ = probability that performance ratio $\rho(p,s)$ within factor of τ of best possible ratio:

$$P_s(\tau) := \frac{|\{p \in \mathcal{P} : \rho(p,s) \leq \tau\}|}{|\mathcal{P}|}$$

- percentage of models that solver s will *solve* if for each model, s can have a maximum resource time of τ times the minimum time
- s solved p: found feasible point *or* found best solution among all solvers

Results: with dicuts, only difficult instances (32)



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