

An Introduction To Modelling with GAMS^{Py}

Workshop

Frederik Fiand
ffiand@gams.com

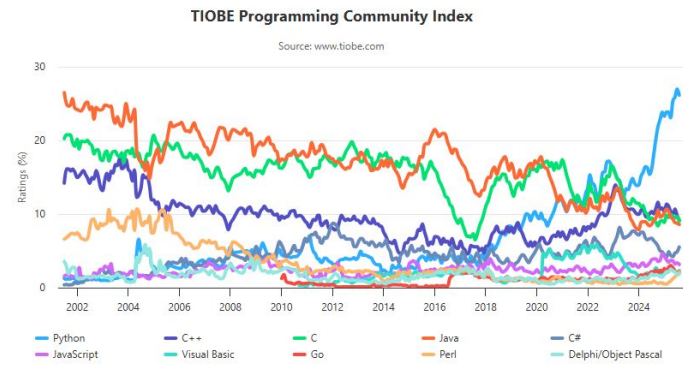
Lutz Westermann
lwestermann@gams.com

Outline

- Motivation
- GAMS**Py** Design
- GAMS**Py** Features
- From GAMS to GAMS**Py**

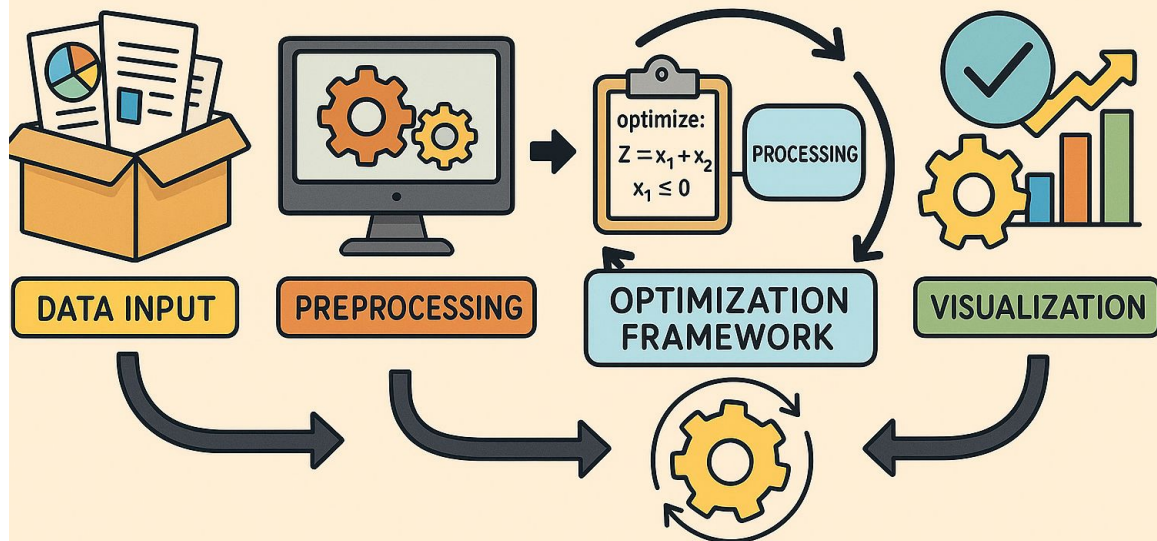
Solving Real-World Problems

- Not *all* about the model
- Data cleaning
- Data manipulation
- Data visualization



Optimization Pipeline

MATHEMATICAL PROGRAMMING (OPTIMIZATION) PIPELINE



GAMS Strengths

- Algebraic modeling language (AML)
- Backward Compatibility - *stable!*
- Active development since 1987 - *stable!*
- Familiar syntax - *human readable!*
- Data is held in GAMS structures - *fast!*
- GAMS Structures - *very large models!*
- *Solver Independence – use what you need!*

- Streamlined data pipeline
- Huge variety of third-party packages
- GAMS-like performance

 python +  G A M S =  G A M S Py

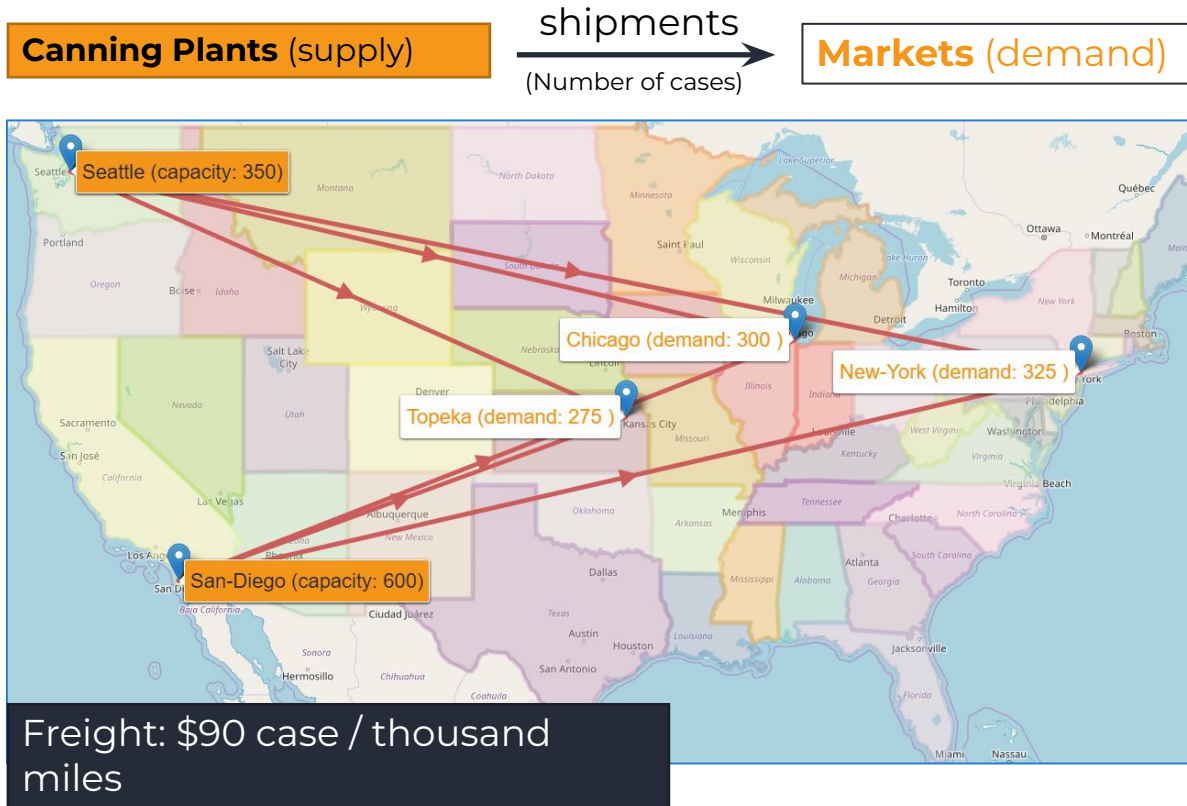
Ease of installation

```
pip install gamspy
```

- Stable version released: <https://pypi.org/project/gamspy/>
- Documentation: <https://gamspy.readthedocs.io/en/latest/>
- Model library (100+ models): <https://github.com/GAMS-dev/gamspy-examples>
- Google Colab Notebooks: <https://gamspy.readthedocs.io/en/latest/user/examples.html>

GAMSPy Design

A Simple Transportation Problem



Mathematical Model Formulation

Indices: i (Canning plants)
 j (Markets)

Decision variables: x_{ij} (Number of cases to ship)

Data: c_{ij} (Transport cost per case)
 a_i (Capacity in cases)
 b_j (Demand in cases)

min $\sum_i \sum_j c_{ij} \cdot x_{ij}$ (Minimize total transportation cost)

subject to

$\sum_j x_{ij} \leq a_i \quad \forall i$ (Shipments from each plant $\leq$ supply capacity)

$\sum_j x_{ij} \geq b_j \quad \forall j$ (Shipments to each market $\geq$ demand)

$x_{ij} \geq 0 \quad \forall i, j$ (Do not ship from market to plant)

$i, j \in \mathbb{N}$

Mathematical Model Formulation



MODEL – SOLVE – DEPLOY

Indices:	i	(Canning plants)	}	Sets
	j	(Markets)		
Decision variables:	x_{ij}	(Number of cases to ship)	}	Variables
Data:	c_{ij}	(Transport cost per case)		
	a_i	(Capacity in cases)	}	Parameters
	b_j	(Demand in cases)		
min	$\sum_i \sum_j c_{ij} \cdot x_{ij}$	(Minimize total transportation cost)	}	Equations
subject to				
	$\sum_j x_{ij} \leq a_i$	$\forall i$ (Shipments from each plant $\leq$ supply capacity)		
	$\sum_j x_{ij} \geq b_j$	$\forall j$ (Shipments to each market $\geq$ demand)		
	$x_{ij} \geq 0$	$\forall i, j$ (Do not ship from market to plant)		
	$i, j \in \mathbb{N}$			

```
from gamspy import Container, Equation, Model, Parameter, Sense, Set,
Sum, Variable

m = Container()

i = Set(m, "i")
j = Set(m, "j")
a = Parameter(m, "a", domain=i)
b = Parameter(m, "b", domain=j)
c = Parameter(m, "c", domain=[i, j])
x = Variable(m, "x", type="positive", domain=[i, j])
supply = Equation(m, "supply", domain=i)
demand = Equation(m, "demand", domain=j)

supply[i] = Sum(j, x[i, j]) <= a[i]
demand[j] = Sum(i, x[i, j]) >= b[j]
```

Abstract Model

Declared/defined over sets

Logically consistent (no domain violations, uncontrolled sets)

Compact

Like “writing on paper”

Completely abstract (no data)

Leverages operator overloading

```
from gamspy import Container, Equation, Model, Parameter, Sense, Set,  
Sum, Variable
```

```
m = Container()
```

```
i = Set(m)
```

```
j = Set(m)
```

```
a = Parameter(m, domain=i)
```

```
b = Parameter(m, domain=j)
```

```
c = Parameter(m, domain=[i, j])
```

```
x = Variable(m, type="positive", domain=[i, j])
```

```
supply = Equation(m, domain=i)
```

```
demand = Equation(m, domain=j)
```

```
supply[i] = Sum(j, x[i, j]) <= a[i]
```

```
demand[j] = Sum(i, x[i, j]) >= b[j]
```

Nameless
Syntax!

Abstract Model

Declared/defined over sets

Logically consistent (no domain violations, uncontrolled sets)

Compact

Like “writing on paper”

Completely abstract (no data)

Leverages operator overloading

Model objects need
a Container, but
live outside

```
transport = Model(  
    m,  
    name="transport",  
    equations=m.getEquations(),  
    problem="LP",  
    sense=Sense.MIN,  
    objective=Sum((i, j), c[i, j] * x[i, j]),  
)  
  
transport.solve()
```

Abstract Model

Declared/defined over sets

Logically consistent (no domain violations, uncontrolled sets)

Compact

Like “writing on paper”

Completely abstract (no data)

Leverages operator overloading

```
z = Variable(m, "z")
objective = Equation(m, "objective")
objective[...] = z == Sum((i, j), c[i, j] * x[i, j])
transport = Model(
    m,
    name="transport",
    equations=m.getEquations(),
    problem="LP",
    sense=Sense.MIN,
    objective=z,
)

transport.solve()
```

Abstract Model

Declared/defined over sets

Logically consistent (no domain violations, uncontrolled sets)

Compact

Like “writing on paper”

Completely abstract (no data)

Leverages operator overloading

```
[...]  
  
transport = Model(  
    m,  
    name="transport",  
    equations=m.getEquations(),  
    problem="LP",  
    sense=Sense.MIN,  
    objective=Sum((i, j), c[i, j] * x[i, j]),  
)  
  
transport.solve()
```

Is there
anything
missing?

Abstract Model

Declared/defined over sets

Logically consistent (no domain violations, uncontrolled sets)

Compact

Like “writing on paper”

Completely abstract (no data)

Leverages operator overloading

```
transport = Model(  
    m,  
    name="transport",  
    equations=m.getEquations(),  
    problem="LP",  
    sense=Sense.MIN,  
    objective=Sum((i, j), c[i, j] * x[i, j]),  
)  
  
# load data  
m.loadRecordsFromGdx("trnsport_input_data.gdx")  
  
transport.solve()
```

Data

Abstract Model

Declared/defined over sets

Logically consistent (no domain violations, uncontrolled sets)

Compact

Like “writing on paper”

Completely abstract (no data)

Leverages operator overloading

```
transport = Model(  
    m,  
    name="transport",  
    equations=m.getEquations(),  
    problem="LP",  
    sense=Sense.MIN,  
    objective=Sum((i, j), c[i, j] * x[i, j]),  
)  
  
# load data  
m.loadRecordsFromGdx("trnsport_input_data.gdx")  
  
transport.solve()
```

```
# Different ways of loading/defining data  
  
# data assignment upon declaration  
i = Set(m, name="i", records=["seattle", "san-diego"])  
j = Set(m, name="j", records=["new-york", "chicago", "topeka"])  
  
# Set declaration and data assignment can also be done separately:  
i = Set(m, "i", description="plants")  
i.setRecords(["seattle", "san-diego"])  
  
# Loading particular symbol from GDX  
m.loadRecordsFromGdx("trnsport_input_data.gdx", symbol_names=["i","j"])  
  
...
```

```
transport = Model(  
    m,  
    name="transport",  
    equations=m.getEquations(),  
    problem="LP",  
    sense=Sense.MIN,  
    objective=Sum((i, j), c[i, j] * x[i, j]),  
)  
  
# load data  
m.loadRecordsFromGdx("trnsport_input_data.gdx")  
  
transport.solve()
```

```
# Different ways of loading/defining data  
  
# getting data from data frames  
distances_df = pd.DataFrame(  
    [  
        ["seattle", "new-york", 2.5],  
        ["seattle", "chicago", 1.7],  
        ["seattle", "topeka", 1.8],  
        ["san-diego", "new-york", 2.5],  
        ["san-diego", "chicago", 1.8],  
        ["san-diego", "topeka", 1.4],  
    ],  
    columns=["plant", "market", "distance"],  
)  
i = Set(m, name="i", records=capacities_df["plant"].tolist())  
j = Set(m, name="j", records=demands_df["market"].tolist())
```

```
[...]  
  
# load data  
m.loadRecordsFromGdx("transport_input_data.gdx")  
  
# redirect output to stdout  
transport.solve(output=sys.stdout)  
  
# redirect output to a file  
with open("my_out_file.log", "w") as file:  
    transport.solve(output=file)
```

Redirecting
Output

Abstract Model

Declared/defined over sets

Logically consistent (no domain violations, uncontrolled sets)

Compact

Like “writing on paper”

Completely abstract (no data)

Leverages operator overloading

```
[...]  
  
# load data  
m.loadRecordsFromGdx("transport_input_data.gdx")  
  
# redirect output to stdout  
transport.solve(solver="highs", output=sys.stdout)  
  
# redirect output to a file  
with open("my_out_file.log", "w") as file:  
    transport.solve(solver="cbc", output=file)
```

Changing
solvers

Abstract Model

Declared/defined over sets

Logically consistent (no domain violations, uncontrolled sets)

Compact

Like “writing on paper”

Completely abstract (no data)

Leverages operator overloading

```
[...]  
  
# load data  
m.loadRecordsFromGdx("transport_input_data.gdx")  
  
# redirect output to stdout  
transport.solve(solver="highs", output=sys.stdout)  
  
# redirect output to a file  
with open("my_out_file.log", "w") as file:  
    transport.solve(solver="cbc", output=file)
```

```
--- Job _SDEkpCCdTmBZwIT9mtl7g.gms Start 08/27/25 15:44:57 50.4.0 c55df396 WEX-WEI x86 64bit/MS  
Windows  
--- GAMS Parameters defined  
    LP highs  
[...]  
--- Generating LP model transport  
--- 6 rows 7 columns 19 non-zeroes  
--- Range statistics (absolute non-zero finite values)  
--- RHS      [min, max] : [ 2.750E+02, 6.000E+02] - Zero values observed as well  
--- Bound    [min, max] : [          NA,          NA] - Zero values observed as well  
--- Matrix   [min, max] : [ 1.260E-01, 1.000E+00]  
--- Executing HIGHS (SolveLink=2): elapsed 0:00:00.039  
[...]  
Model status      : Optimal  
Objective value    : 1.5367500000e+02  
Relative P-D gap   : 0.0000000000e+00  
HIGHS run time    : 0.00  
--- Reading solution for model transport  
--- Executing after solve: elapsed 0:00:00.097  
--- _SDEkpCCdTmBZwIT9mtl7g.gms(188) 4 Mb  
--- GDX File C:\Users\ffian\AppData\Local\Temp\tmp18kvqkxv\_SDEkpCCdTmBZwIT9mtl7gout.gdx  
*** Status: Normal completion  
--- Job _SDEkpCCdTmBZwIT9mtl7g.gms Stop 08/27/25 15:44:57 elapsed 0:00:00.117
```

```
i = Set(m, "i")
j = Set(m, "j")
[...]
supply = Equation(m, "supply", domain=i)
demand = Equation(m, "demand", domain=j)

supply[i] = Sum(j, x[i, j]) <= a[i]
demand[i] = Sum(i, x[i, j]) >= b[j]
[...]
```

Early Errors

Abstract Model

Declared/defined over sets

Logically consistent (no domain violations, uncontrolled sets)

Compact

Like “writing on paper”

Completely abstract (no data)

Leverages operator overloading

```
i = Set(m, "i")
j = Set(m, "j")
[...]
supply = Equation(m, "supply", domain=i)
demand = Equation(m, "demand", domain=j)
```

Early Errors

```
supply[i] = Sum(j, x[i, j]) <= a[i]
demand[i] = Sum(i, x[i, j]) >= b[j] #wrong equation domain!
[...]
```

Traceback (most recent call last):

File "myFile.py", line 18, in <module>

demand[i] = Sum(i, x[i, j]) >= b[j]

[...]

gamspy.exceptions.ValidationError: `Given set `i` is not a
valid domain for declared domain `j`

GAMS Philosophy

Tight syntax leads to
better modeling

```
from rich.traceback import install
install()
[...]
supply = Equation(m, "supply", domain=i)
demand = Equation(m, "demand", domain=j)
```

Early Errors

```
supply[i] = Sum(j, x[i, j]) <= a[i]
demand[i] = Sum(i, x[i, j]) >= b[j] #wrong equation domain!
```

Traceback (most recent call last)

```
c:\Users\ffian\Documents\projects\gamspy-examples\models\trnsport\4_transport_domainviol.py:18
in <module>
```

```
15 demand = Equation(m, "demand", domain=j)
16
17 supply[i] = Sum(j, x[i, j]) <= a[i]
18 demand[i] = Sum(i, x[i, j]) >= b[j] #wrong equation domain!
19
```

ValidationError: `Given set `i` is not a valid domain for declared domain `j``

GAMS Philosophy

Tight syntax leads to
better modeling

```
i = Set(m)
j = Set(m)
[...]
supply = Equation(m, domain=i)
demand = Equation(m, domain=j)

supply[i] = Sum(j, x[i, j]) <= a[i]
demand[i] = Sum(i, x[i, j]) >= b[j] #wrong equation domain!
```

Early Errors

Nameless
Syntax!

```
Traceback (most recent call last):
c:\Users\ffian\Documents\projects\gamspy-examples\models\transport\5_transport_domainviol_nameless.py:18 in <module>
    15 demand = Equation(m, domain=j)
    16
    17 supply[i] = Sum(j, x[i, j]) <= a[i]
> 18 demand[i] = Sum(i, x[i, j]) >= b[j] #wrong equation domain!
    19
```

```
ValidationError: `Given set `swZIYTYDVRzmbekoVmhYFcggpauto` is not a valid domain for declared domain `sTKcGVC17RuqOqtbBWEZOywgpauto`
```

GAMS Philosophy

Tight syntax leads to
better modeling

GAMSPy Design



MODEL – SOLVE – DEPLOY

```
from gamspy import Container, Equation, Model, Parameter, Sense, Set,  
Sum, Variable, set_options
```

```
set_options({"USE_PY_VAR_NAME": "yes"})
```

```
i = Set(m)
```

```
j = Set(m)
```

```
[...]
```

```
supply = Equation(m, domain=i)
```

```
demand = Equation(m, domain=j)
```

```
supply[i] = Sum(j, x[i, j]) <= a[i]
```

```
demand[i] = Sum(i, x[i, j]) >= b[j] #wrong equation domain!
```

Early Errors

Nameless
Syntax!

Traceback (most recent call last):

```
c:\Users\ffian\Documents\projects\gamspy-examples\models\transport\5_transport_domainviol_nameless.py:18 in <module>
```

```
15 demand = Equation(m, domain=j)
```

```
16
```

```
17 supply[i] = Sum(j, x[i, j]) <= a[i]
```

```
18 demand[i] = Sum(i, x[i, j]) >= b[j] #wrong equation domain!
```

```
19
```

```
ValidationError: 'Given set `i` is not a valid domain for declared domain `j`'
```

GAMS Philosophy

Tight syntax leads to
better modeling

GAMSPy Features

Interoperability (.toLatex)

```
transport.toLatex("latex_out_path")
```

```
-----  
  
[CONVERTER - INFO] LaTeX (.tex) file has been generated  
under latex_out_path\transport.tex
```

Symbols

Sets

Name	Domains	Description
i	*	
j	*	

Parameters

Name	Domains	Description
a	i	
b	j	
c	i,j	

Variables

Name	Domains	Description
x	i,j	

Equations

Name	Domains	Description
supply	i	
demand	j	

Model Definition

min $\sum_{i,j} c_{i,j} \cdot x_{i,j}$
s.t.

supply
 $\sum_j x_{i,j} \leq a_i \quad \forall i$

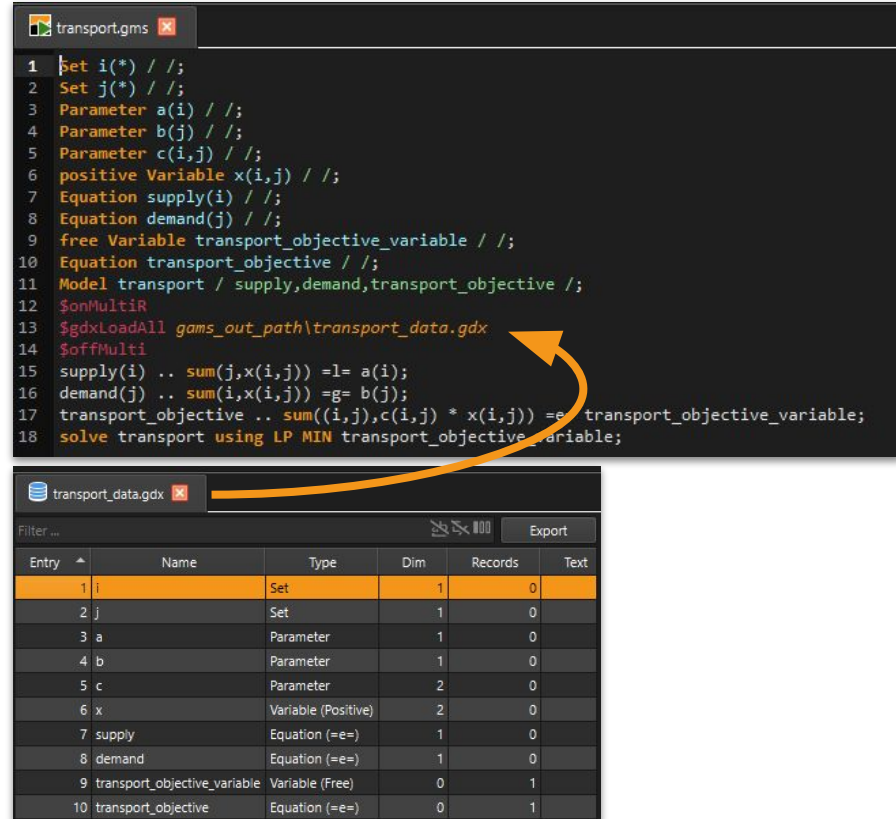
demand
 $\sum_i x_{i,j} \geq b_j \quad \forall j$

$x \geq 0 \quad \forall i, j$

Interoperability (.toGams)

```
transport.toGams("gams_out_path")
```

```
-----  
[CONVERTER - INFO] GAMS (.gms) file has been generated  
under gams_out_path\transport.gms
```



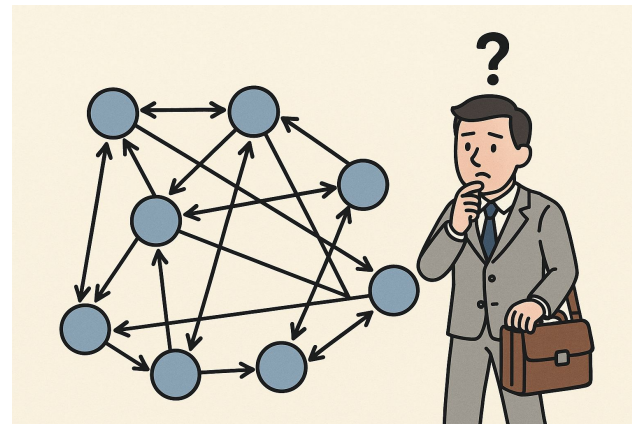
```
1 Set i(*) //;  
2 Set j(*) //;  
3 Parameter a(i) //;  
4 Parameter b(j) //;  
5 Parameter c(i,j) //;  
6 positive Variable x(i,j) //;  
7 Equation supply(i) //;  
8 Equation demand(j) //;  
9 free Variable transport_objective_variable //;  
10 Equation transport_objective //;  
11 Model transport / supply,demand,transport_objective /;  
12 $onMultiR  
13 $gdxLoadAll gams_out_path\transport_data.gdx  
14 $offMulti  
15 supply(i) .. sum(j,x(i,j)) =l= a(i);  
16 demand(j) .. sum(i,x(i,j)) =g= b(j);  
17 transport_objective .. sum((i,j),c(i,j) * x(i,j)) =e= transport_objective_variable;  
18 solve transport using LP MIN transport_objective_variable;
```

Entry	Name	Type	Dim	Records	Text
1	i	Set	1	0	
2	j	Set	1	0	
3	a	Parameter	1	0	
4	b	Parameter	1	0	
5	c	Parameter	2	0	
6	x	Variable (Positive)	2	0	
7	supply	Equation (=e=)	1	0	
8	demand	Equation (=e=)	1	0	
9	transport_objective_variable	Variable (Free)	0	1	
10	transport_objective	Equation (=e=)	0	1	

Interoperability (advanced)

Travelling Salesperson Problem

- Visit all cities
- Visit each city only once
- Minimize cost



→ Modelling

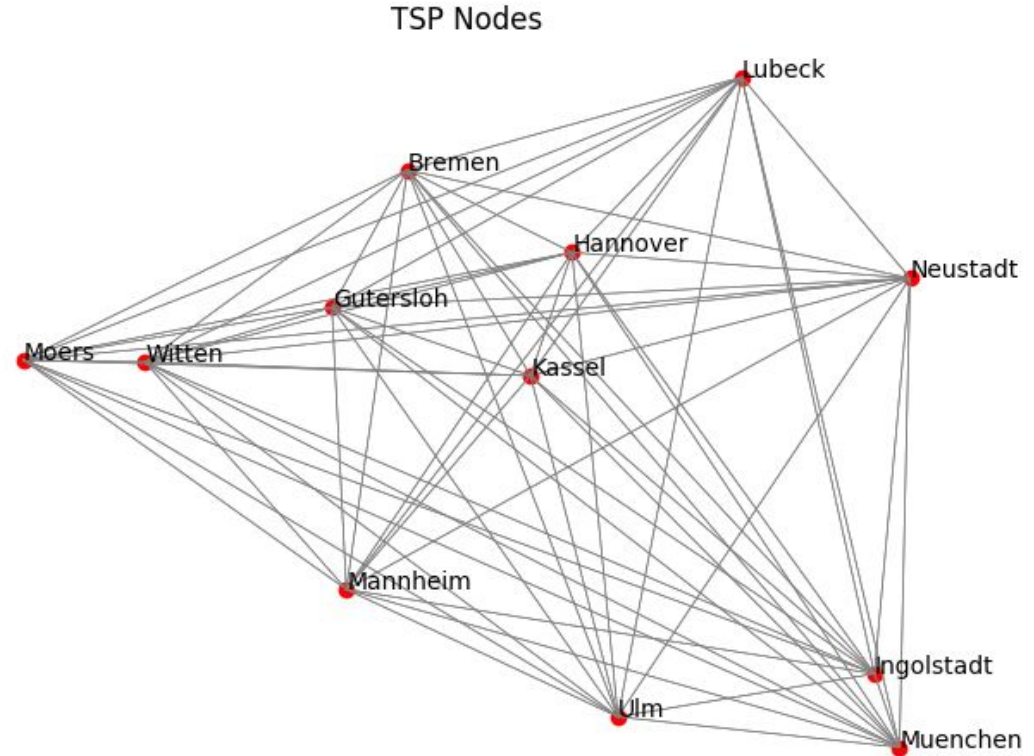


→ Subtour Detection & Plotting

Traveling Salesman Problem

Data Input:

- Nodes
- Edges
- Edge weights



Traveling Salesman Problem

```
[...]
rowsum = Equation(m, name="rowsum", domain=ii, description="leave each city only once")
colsum = Equation(m, name="colsum", domain=jj, description="arrive at each city only once")

# the assignment problem is a relaxation of the TSP
rowsum[i] = Sum(j, x[i, j]) == 1
colsum[j] = Sum(i, x[i, j]) == 1

# Objective Function
objective = Sum([i, j], c[i, j] * x[i, j])

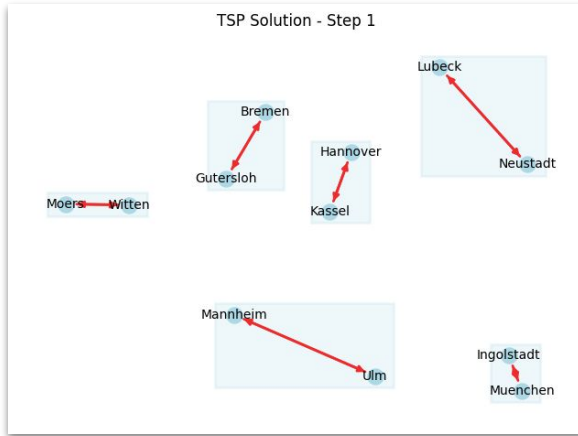
# exclude diagonal
x.fx[ii, ii] = 0
[...]

# Cuts to be added dynamically
cut = Equation(m, name="cut", domain=cut_ids, description="dynamic cuts")
cut[cut_active] = (Sum([i, j], cutcoeff[cut_active, i, j] * x[i, j]) >= 1)
[...]
```

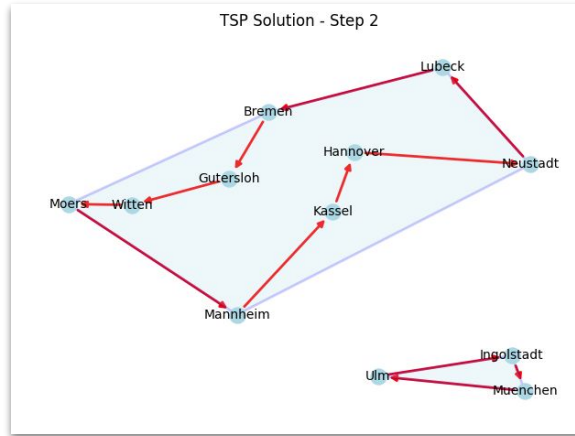
Cuts will be added
iteratively for
subtours detected via
`nx.strongly_connected_components`

Traveling Salesman Problem

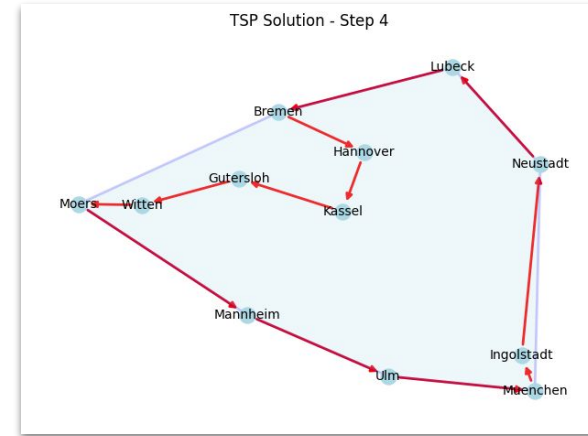
TSP Solution - Step 1



TSP Solution - Step 2



TSP Solution - Step 4



Corresponding example available at

<https://github.com/GAMS-dev/gamspy-examples/blob/master/models/tsp/tsp.py>

MIRO (from GAMS Py model to Web App)

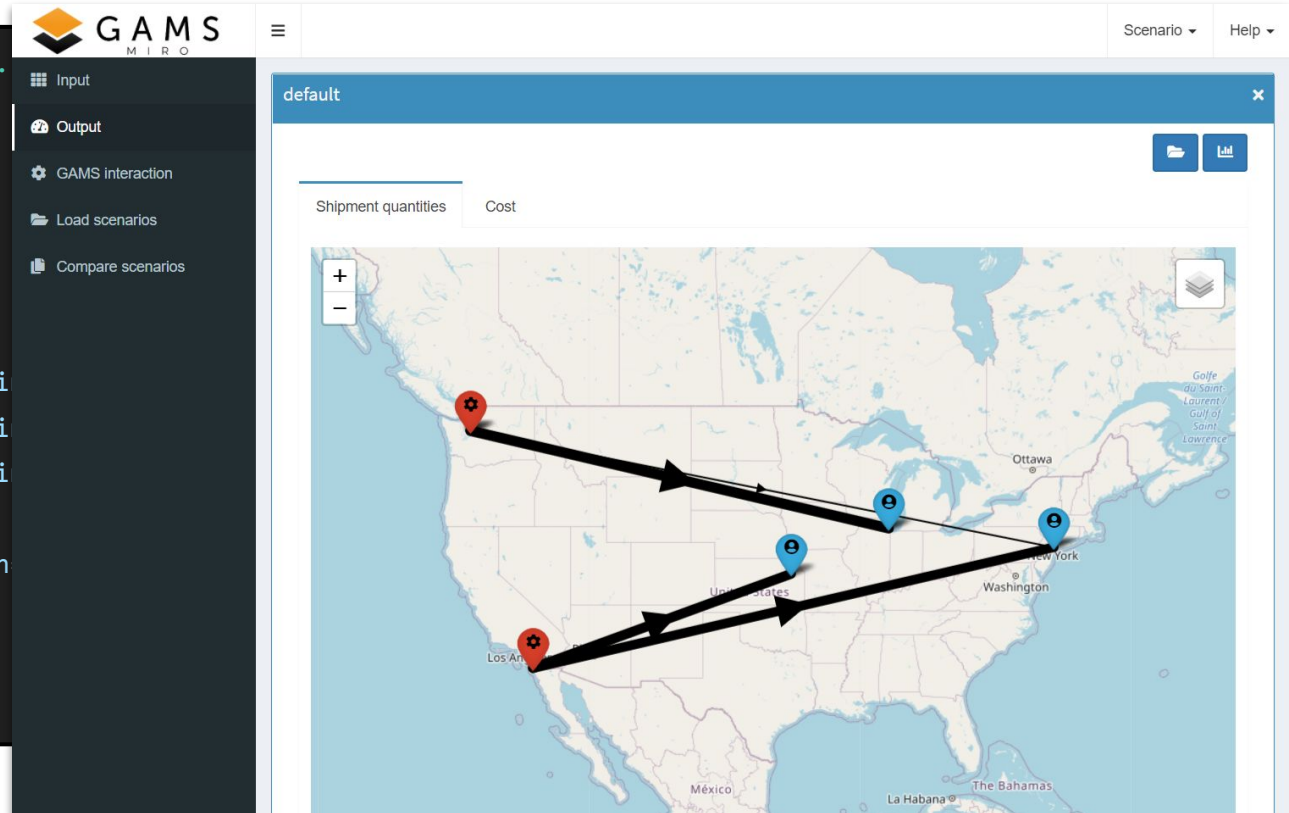
```
from gamspy import Container, ...  
...  
...  
data preparation  
...  
...  
  
a = Parameter(m, name="a", domain=[i], records=capacities)  
b = Parameter(m, name="b", domain=[j], records=demands)  
d = Parameter(m, name="d", domain=[i, j], records=distances, is_miro_input=True)  
  
x = Variable(m, name="x", domain=[i, j], type="Positive", is_miro_output=True)  
...  
...  
model.solve()
```

MIRO (from GAMSPy model to Web App)



MODEL – SOLVE – DEPLOY

```
from gamspy import Container, ...  
...  
...  
data preparation  
...  
...  
  
a = Parameter(m, name="a", domain=  
b = Parameter(m, name="b", domain=  
d = Parameter(m, name="d", domain=  
  
x = Variable(m, name="x", domain=  
...  
...  
model.solve()
```



Remote Solve (NEOS)



MODEL – SOLVE – DEPLOY

```
from gamspy import Container, Equation, Model, NeosClient, Parameter, Sense, Set,
Sum, Variable
import sys
import os

m = Container()
[...]
client = NeosClient(
    email=os.environ["NEOS_EMAIL"],
    username=os.environ["NEOS_USER"],
    password=os.environ["NEOS_PASSWORD"],
)

transport.solve(solver="highs", output=sys.stdout, backend="neos", client=client)
```

Remote Solve (NEOS)

```
from gamspy import Container, Equation, Model, NeosClient, Parameter, Sense, Set,  
Sum, Variable  
import sys  
import os  
  
m = Container()  
[...]  
client = NeosClient(  
    email=os.environ["NEOS_EMAIL"],  
    username=os.environ["NEOS_USER"],  
    password=os.environ["NEOS_PASSWORD"],  
)  
  
transport.solve(solver="highs", output=sys.stdout, ba
```

```
[NEOS - INFO] Job Number: 17342076, Job Password: hYgsnIRH  
--- Job MODEL.gms Start 08/25/25 04:48:47 49.6.1 55d34574 LEX-LEG x86 64bit/Linux  
[...]  
--- Executing HIGHS (SolveLink=2): elapsed 0:00:00.002[LST:22]  
  
HIGHS          49.6.1 55d34574 May 28, 2025          LEG x86 64bit/Linux  
[...]  
Model status      : Optimal  
Objective value    : 1.5367500000e+02  
Relative P-D gap   : 0.0000000000e+00  
HiGHS run time    :          0.00  
[...]  
*** Status: Normal completion[LST:73]  
--- Job MODEL.gms Stop 08/25/25 04:48:47 elapsed 0:00:00.012
```

Remote Solve (NEOS)

```
from gamspy import Container, Equation, Model, NeosClient, Parameter, Sense, Set,  
Sum, Variable  
import sys  
import os
```

```
m = Container()
```

```
[...]
```

```
client = NeosClient(  
    email=os.environ["NEOS_EMAIL"],  
    username=os.environ["NEOS_USER"],  
    password=os.environ["NEOS_PASSWORD"],  
)
```

} optional

```
transport.solve(solver="highs", output=sys.stdout, ba
```

```
[NEOS - INFO] Job Number: 17342076, Job Password: hYgsnIRH  
--- Job MODEL.gms Start 08/25/25 04:48:47 49.6.1 55d34574 LEX-LEG x86 64bit/Linux  
[...]  
--- Executing HIGHS (SolveLink=2): elapsed 0:00:00.002[LST:22]
```

```
HIGHS          49.6.1 55d34574 May 28, 2025          LEG x86 64bit/Linux
```

```
[...]
```

```
Model status      : Optimal  
Objective value    : 1.5367500000e+02  
Relative P-D gap   : 0.0000000000e+00  
HiGHS run time     : 0.00
```

```
[...]
```

```
*** Status: Normal completion[LST:73]
```

```
--- Job MODEL.gms Stop 08/25/25 04:48:47 elapsed 0:00:00.012
```

Remote Solve (GAMS Engine)

```
from gamspy import Container, EngineClient, Equation, Model, Parameter, Sense, Set,
Sum, Variable, Options
import sys
import os

m = Container()
[...]
client = EngineClient(
    host=os.environ["ENGINE_URL"],
    username=os.environ["ENGINE_USER"],
    password=os.environ["ENGINE_PASSWORD"],
    namespace=os.environ["ENGINE_NAMESPACE"],
)

transport.solve(solver=" highs", output=sys.stdout, backend="engine", client=client)
```

Remote Solve (GAMS Engine)

```
from gamspy import Container, EngineClient, Equation, Model, Parameter, Sense, Set,
Sum, Variable, Options
import sys
import os

m = Container()
[...]
client = EngineClient(
    host=os.environ["ENGINE_URL"],
    username=os.environ["ENGINE_USER"],
    password=os.environ["ENGINE_PASSWORD"],
    namespace=os.environ["ENGINE_NAMESPACE"],
)

transport.solve(solver="highs", output=sys.stdout, backend="engine", client=client)
```

```
(gamspy) PS C:\... \transport> & ... python.exe 8_transport_engine.py
[ENGINE - INFO] Job status is queued...
[ENGINE - INFO] Job status is queued...
--- Job _h90DwTG8QxW_gCq7UTbZXw.gms Start 08/30/25 05:01:55 50.4.1 84b10359
LEX-LEG x86 64bit/Linux
[...]
--- Executing HIGHS (SolveLink=2): elapsed 0:00:00.003
[...]
Model status      : Optimal
Objective value    : 1.5367500000e+02
Relative P-D gap   : 0.0000000000e+00
HIGHS run time    : 0.00
[...]
*** Status: Normal completion
--- Job _X48ZOZpwSQuuKxEW7iBNTA.gms Stop 08/31/25 19:22:45 elapsed 0:00:00.496
[ENGINE - INFO] Results have been extracted to your working directory:
C:\Users\ffian\AppData\Local\Temp\tmpt18c6oa4.
```

Frozen Solve

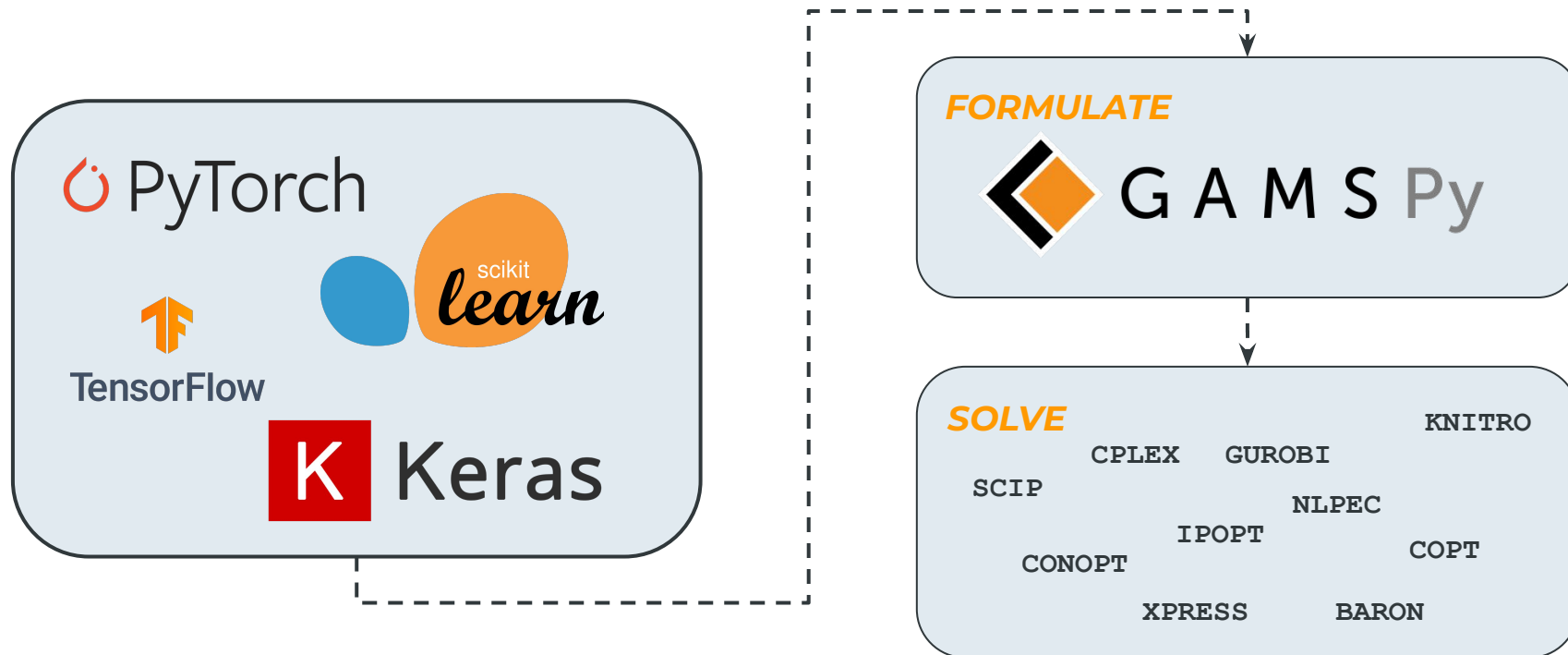
```
# define the model
...
# parameter definition
bmult = Parameter(m, name="bmult", records=1)
demand[j] = Sum(i, x[i, j]) >= bmult * b[j]
# parameter values
bmult_list = [0.6, 0.7, 0.8, 0.9, 1.0, 1.1, 1.2, 1.3]

transport.freeze(modifiabiles=[bmult])
for b_value in bmult_list:
    bmult.setRecords(b_value)
    transport.solve(solver="conopt")
transport.unfreeze()
```

Frozen
solve

New Opportunities

Python is THE ML Language



New Opportunities

Python is THE ML Language

Learn more at session

WE-09

Wednesday, 16:30-18:00 - Room: H15
Modelling and APIs

Talk 2

Embedding Neural Networks into Optimization Models with GAMSPy

Frederik Fiand, Michael Bussieck, Hamdi Burak Usul

PyTorch



TensorFlow



K

A M S Py

KNITRO

GUROBI

NLPEC

IPOPT

COPT

CONOPT

XPRESS

BARON

Summary

- GAMSPy leverages GAMS backend to generate and solve models
- State-of-the-art optimization solvers
- Unique and streamlined way to complete pre/post-processing and visualization – all in a single environment
- Seamless integration with [GAMS MIRO](#), [GAMS Engine](#), and [NEOS](#) (local machines vs. cloud/AWS machines)
- Installed with one line:

```
pip install gamspy
```

From GAMS to GAMSPy

Basics

Translating Symbols

```
Set      i      / i1, i2 /;
Alias    (i, a);
Parameter p(i) / i1 1, i2 2 /;
Variable v(i), z;
Equation e(i);
e(i) .. v(i) + p(i) =l= z;
Model my_model / e /;
solve my_model using LP min z;
```

```
import gamspy as gp
gp.set_options({"USE_PY_VAR_NAME": "yes"})

m = gp.Container()

i = gp.Set(m, records=['i1','i2'])
a = gp.Alias(m, alias_with=i)
p = gp.Parameter(m, domain=i, records=[['i1','1'], ['i2','2']])
v = gp.Variable(m, domain=i)
z = gp.Variable(m)
e = gp.Equation(m, domain=i)
e[i] = v[i] + p[i] <= z
my_model = gp.Model(m, equations=[e], problem="lp", sense="min",
objective=z)
my_model.solve()
```

Translating Operations: Sum, Prod , ...

Ellipsis Literal
→ Scalar Equation

```
Set      i      / i1,  i2 /;  
Parameter a(i) / i1 1, i2 2 /;  
Variable z;  
Equation eq;  
eq .. sum(i, a(i)) =l= z;
```

```
import gamspy as gp  
from gamspy import Sum, Product, Smin, Smax  
gp.set_options({"USE_PY_VAR_NAME": "yes"})  
  
m = gp.Container()  
i = gp.Set(m, records=['i1','i2'])  
a = gp.Parameter(m, domain=i, records=[['i1','1'], ['i2','2']])  
z = gp.Variable(m)  
  
eq = gp.Equation(m)  
eq[...] = Sum(i, a[i]) <= z
```

```
Set i / i0*i180 /;  
Parameter step;  
step = pi / 180;  
Parameter omega(i);  
omega(i) = (ord(i) - 1) * step;
```

```
import gamspy as gp  
import math  
gp.set_options({"USE_PY_VAR_NAME": "yes"})  
  
m = gp.Container()  
i = gp.Set(m, records=[f'i{i}' for i in range(181)])  
step = gp.Parameter(m, records=math.pi / 180)  
omega = gp.Parameter(m, domain=i)  
omega[i] = (gp.Ordinal(i) - 1) * step
```

Condition

```
Set i / i1*i5 /;  
Alias (i, j);  
Set adjacent(i, j);  
adjacent(i, j) = ord(i)=ord(j)-1;  
  
Parameter p(i,j);  
p(i,j)$adjacent(i, j) = 42;
```

```
import gamspy as gp  
gp.set_options({"USE_PY_VAR_NAME": "yes"})  
  
m = gp.Container()  
i = gp.Set(m, records=[f"i{b}" for b in range(1, 6)])  
j = gp.Alias(m, alias_with=i)  
adjacent = gp.Set(m, domain=[i, j])  
adjacent[i, j] = gp.Ord(i)==gp.Ord(j)-1  
  
p = gp.Parameter(m, "cntAdj", [i, j])  
p[i, j].where[adjacent[i, j]] = 42
```

Condition - Domain

```
Set i / i1*i5 /;  
Alias (i, j);  
Set adjacent(i, j);  
adjacent(i, j) = ord(i)=ord(j)-1;  
  
Parameter cntAdj;  
cntAdj = sum((i,j)$adjacent(i, j), 1);
```

```
import gamspy as gp  
gp.set_options({"USE_PY_VAR_NAME": "yes"})  
  
m = gp.Container()  
i = gp.Set(m, records=[f"i{b}" for b in range(1, 6)])  
j = gp.Alias(m, alias_with=i)  
adjacent = gp.Set(m, domain=[i, j])  
adjacent[i, j] = gp.Ord(i)==gp.Ord(j)-1  
  
cntAdj = gp.Parameter(m)  
cntAdj[...] = gp.Sum(gp.Domain(i, j).where[adjacent[i, j]], 1 )
```

Condition - Number

```
Set k / "1964-i", "1964-ii",  
        "1964-iii", "1964-iv"/,  
    ki(k) "initial period";  
ki(k) = ord(k) = 1;
```

```
import gamspy as gp  
gp.set_options({"USE_PY_VAR_NAME": "yes"})  
  
m = gp.Container()  
k = gp.Set(m,  
records=["1964-i","1964-ii","1964-iii","1964-iv"])  
ki = gp.Set(m, domain=k, description="initial period")  
ki[k] = gp.Number(1).where[gp.Ordinal(k) == 1]
```

Math package

```
Set i / i1, i2 /;  
Set k / k1, k2 /;  
Parameter sigma(i,k);  
sigma(i,k) = uniform(0.1, 1);  
display sigma;
```

```
import gamspy as gp  
import gamspy.math as gams_math  
import random  
gp.set_options({"USE_PY_VAR_NAME": "yes"})  
  
m = gp.Container()  
i = gp.Set(m, records=['i1', 'i2'])  
k = gp.Set(m, records=['k1', 'k2'])  
sigma = gp.Parameter(m, domain=[i, k])  
sigma[i, k] = gams_math.uniform(0.1, 1) # Generates a different  
value from uniform distribution for each element of the domain.  
sigma[i, k] = random.uniform(0.1, 1) # This is not equivalent  
to the statement above. This generates only one value for the  
whole domain.
```

Logical Operations

Since it is not possible in Python to overload keywords such as **and**, **or**, and **not**, one needs to use bitwise operators **&**, **|**, and **~**.

Mapping:

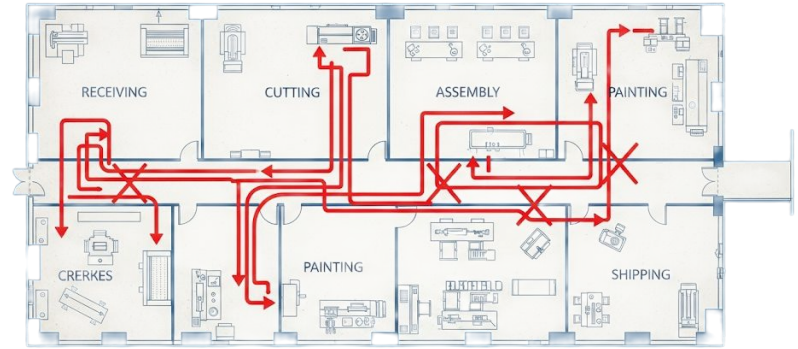
- **and** → **&**
- **or** → **|**
- **not** → **~**

```
error01(s1,s2) = rt(s1,s2) and not lfr(s1,s2) or not rt(s1,s2) and lfr(s1,s2);
```

```
error01[s1, s2] = rt[s1, s2] & (~lfr[s1, s2]) | ((~rt[s1, s2]) & lfr[s1, s2])
```

Example: Layout planning

- **Goal:** Figure out the best way to place a number of objects into available locations to make things run as smoothly as possible
- **Input:**
 - List of locations with given space capacity
 - List of objects to be placed, each with space requirement
 - Number of trips between every pair of objects
 - Distance between every pair of locations
 - Placement requirements



Example: Layout planning

- **Objective**

- Minimize Transportation Cost: Sum up the flow between every pair of objects multiplied by the distance between their final locations

- **Decision Variables**

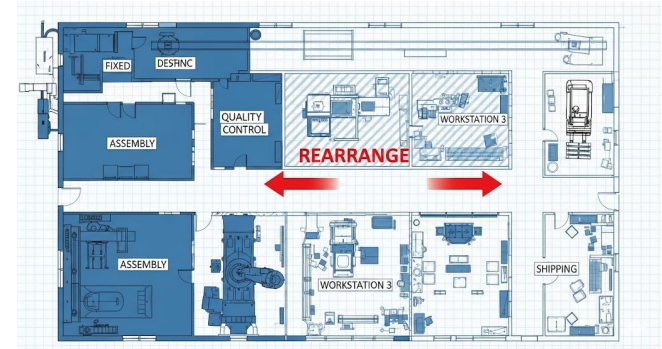
- Decide if a specific object will be placed in a specific location for every possible pairing of object and location

- **Constraints**

- The total space of all objects placed in a single location cannot be more than that location's available space
- Each object must be assigned to exactly one location
- Respects placement requirements

Solution Approach: Fix and Optimize

- Iterative process that repeatedly solves a series of smaller sub-problems of the original problem
- **Start:** A feasible solution
- **The "Fix":** Fixes most of the decision variables to their current values
- **The "Optimize":** Optimizes a small, unfixed subset of the variables to find a better solution
- **Iteration:** If the optimization step improves the overall solution, that new solution becomes the starting point for the next round
- **End:** No further improvements can be found.



From GAMS to GAMSPy

Example from:
<https://www.operations-management-online.de/>



Author:
Prof. Dr. Stefan Helber
Leibniz Universität
Hannover

4 + 1 Modules to achieve:

- Tailor software engineering best practises to optimization software
- Implement models like in LaTeX
- Maintainable optimization software

Course Instructor: **Tim Varelmann**



- GAMS user since 2018
- RWTH, UQ Brisbane, UT Austin & MIT
- Independent optimization consultant

Registration opens 10th of September



Sign up to stay in the loop!

- Don't miss out on additional information
- Get exclusive bonuses
- Sweet discounts

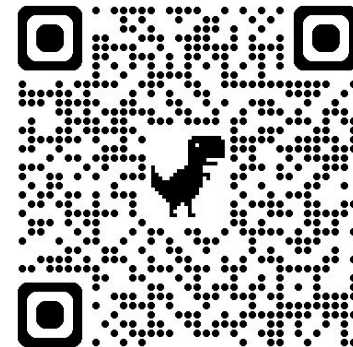
Try before you buy

- 30-minute course intro when you ride home again
- Required prerequisites & instructor introduction
- Goals, content & structure of the course
- **Leave your comment!**



Academic Program

- Free GAMS and GAMS^{Py} licenses
 - No model size limit on GAMS^{Py}
 - Access to all open-source solvers + commercial solvers such as CPLEX, CONOPT, COPT, MOSEK, XPRESS, and GUROBI-link
 - Sign up at <https://academic.gams.com/>
- Other resources
 -  Community FORUM  at <https://forum.gams.com/>
 -  YouTube channel  at <https://www.youtube.com/@GAMSLessons>
 - Ready-to-run notebooks, case studies, blog posts, and more!





MODEL – SOLVE – DEPLOY