

MINLP Solvers – version to version

This is an updated version of the MINLP solvers benchmark from my talk at ISMP 2015.

Stefan Vigerske

11th December 2017

Which instances to run?

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 - ▶ 60 small investor portfolio optimization instances
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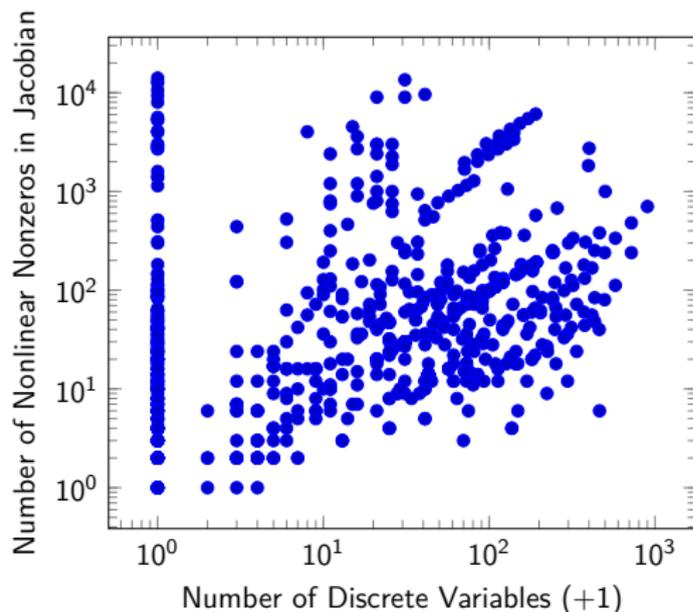
Thus, need to select a reasonable subset of (e.g., 87) instances.

Apply the P.I.T.T. heuristic.

Prune Instances by Tractability and Triviality Heuristic

1. Remove intractable instances

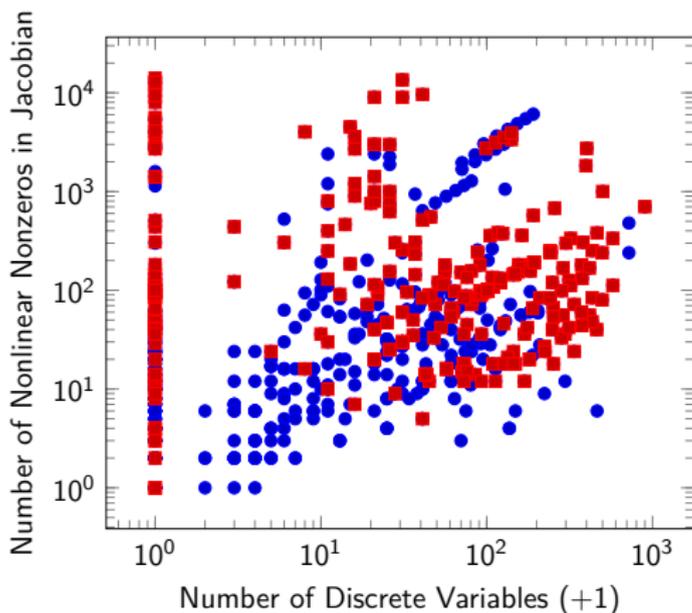
- ▶ consider only the 881 instances that are marked as solved in MINLPLib 2



Prune Instances by Tractability and Triviality Heuristic

2. For each solver separately:

- ▶ Remove instances that are solved within 60 seconds by the oldest solver version (e.g., as in GAMS 23.7).
- ▶ Remove instances that the solver cannot handle (due to trigonometric functions, SOS, ...).



In case of SCIP:

Prune Instances by Tractability and Triviality Heuristic

For SCIP, this leaves 312 instances:

alkylation	clay0304h	ex6_1_1	fo9_ar5_1	house
arki0003	clay0305h	ex6_1_3	gasnet	jbearing25
arki0005	crudeoil_lee2_10	ex6_2_12	genpooling_meyer04	jbearing75
arki0006	crudeoil_lee3_07	ex6_2_14	ghg_1veh	johnall
arki0019	crudeoil_lee3_08	ex6_2_8	ghg_3veh	kall_circles_c6a
arki0024	crudeoil_lee3_09	ex6_2_9	glider100	kall_circles_c6b
autocorr_bern20-10	crudeoil_lee3_10	ex7_2_4	graphpart_2g-0066-0066	kall_circles_c7a
autocorr_bern20-15	crudeoil_li06	ex8_1_7	graphpart_2g-0077-0077	kall_circles_c8a
autocorr_bern25-06	csched1a	ex8_2_1b	graphpart_2g-0088-0088	kall_circlespolygons_c1p
autocorr_bern25-13	edgecross10-060	ex8_2_4b	graphpart_2g-0099-9211	kall_circlespolygons_c1p
autocorr_bern30-04	edgecross10-070	ex8_4_1	graphpart_2pm-0066-0066	kall_circlesrectangles_c
autocorr_bern35-04	edgecross10-080	ex8_4_3	graphpart_2pm-0077-0777	kall_circlesrectangles_c
batch0812_nc	edgecross14-039	ex8_4_4	graphpart_2pm-0088-0888	kall_congruentcircles_c7
batches201210m	edgecross14-058	ex8_4_5	graphpart_2pm-0099-0999	kall_diffcircles_10
bayes2_50	edgecross14-078	ex8_4_8_bnd	graphpart_3g-0334-0334	kall_diffcircles_5b
blend480	edgecross14-176	filter	graphpart_3g-0344-0344	kall_diffcircles_7
blend531	edgecross20-040	fin2bb	graphpart_3g-0444-0444	kall_diffcircles_8
blend718	edgecross22-048	flay05h	graphpart_3pm-0244-0244	kall_diffcircles_9
blend852	emfl1050_5_5	fo7	graphpart_3pm-0333-0333	launch
carton7	emfl100_5_5	fo8	graphpart_3pm-0334-0334	lop97icx
casctanks	ethanolh	fo8_ar25_1	graphpart_3pm-0344-0344	mathopt5_7
cecil_13	ethanolm	fo8_ar2_1	graphpart_3pm-0444-0444	mathopt5_8
chem	ex1252a	fo9	graphpart_clique-30	mhw4d
clay0203h	ex14_1_1	fo9_ar25_1	graphpart_clique-40	milinfract
clay0204h	ex14_1_7	fo9_ar2_1	gsg_0001	minlphix
clay0205h	ex4_1_5	fo9_ar3_1	hda	minsurf100
clay0303h	ex4_1_6	fo9_ar4_1	heatexch_trigen	...

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arki0003	clay0305h	ex6_1_3	gasnet	jbearing25
arki0005	crudeoil_lee2_10	ex6_2_12	genpooling_meyer04	jbearing75
arki0006	crudeoil_lee3_07	ex6_2_14	ghg_1veh	johnall
arki0019	crudeoil_lee3_08	ex6_2_8	ghg_3veh	kall_circles_c6a
arki0024	crudeoil_lee3_09	ex6_2_9	glider100	kall_circles_c6b
autocorr_bern20-10	crudeoil_lee3_10	ex7_2_4	graphpart_2g-0066-0066	kall_circles_c7a
autocorr_bern20-15	crudeoil_li06	ex8_1_7	graphpart_2g-0077-0077	kall_circles_c8a
autocorr_bern25-06	csched1a	ex8_2_1b	graphpart_2g-0088-0088	kall_circlespolygons_c1p
autocorr_bern25-13	edgecross10-060	ex8_2_4b	graphpart_2g-0099-9211	kall_circlespolygons_c1p
autocorr_bern30-04	edgecross10-070	ex8_4_1	graphpart_2pm-0066-0066	kall_circlesrectangles_c
autocorr_bern35-04	edgecross10-080	ex8_4_3	graphpart_2pm-0077-0777	kall_circlesrectangles_c
batch0812_nc	edgecross14-039	ex8_4_4	graphpart_2pm-0088-0888	kall_congruentcircles_c7
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bayes2_50	edgecross14-078	ex8_4_8_bnd	graphpart_3g-0334-0334	kall_diffcircles_5b
blend480	edgecross14-176	filter	graphpart_3g-0344-0344	kall_diffcircles_7
blend531	edgecross20-040	fin2bb	graphpart_3g-0444-0444	kall_diffcircles_8
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P.I.T.T.E.D. Heuristic: P.I.T.T. with Eased Dominance

3. Ensure uniqueness of 6-characters-prefix of instances names.

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autocorr_bern20-15	crudeoil_li06	ex8_1_7	graphpart_2g-0077-0077	kall_circles_c8a
autocorr_bern25-06	csched1a	ex8_2_1b	graphpart_2g-0088-0088	kall_circlespolygons_c1p
autocorr_bern25-13	edgexcross10-060	ex8_2_4b	graphpart_2g-0099-9211	kall_circlespolygons_c1p
autocorr_bern30-04	edgexcross10-070	ex8_4_1	graphpart_2pm-0066-0066	kall_circlesrectangles_c
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clay0303h	ex4_1_6	fo9_ar4_1	heatexch_trigen	...

P.I.T.T.E.D. SCIP testset

In summary:

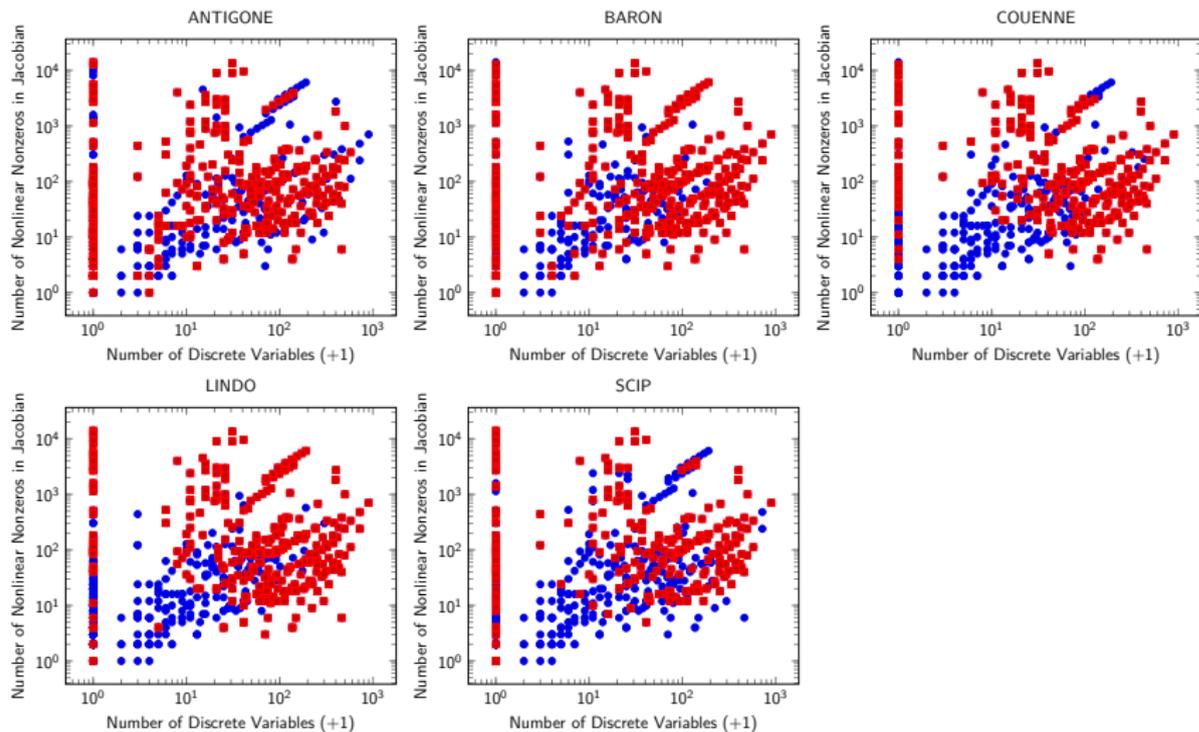
1. Keep only instances that are marked as **solved** in MINLPLib 2.
2. Keep only instances that take ≥ 60 s with **oldest version** of solver and that can be **handled** by solver.
3. Reduce instances with **similar names**.

For SCIP, this reduces from 1363 to 881 to 123 instances:

alkylation	emf1050_5_5	fo9_ar25_1	milinfract	pinene50	
arki0003	emf1100_5_5	gasnet	minlphix	pointpack08	
autocorr_bern20-10	ethanolh	genpooling_meyer04	minsurf100	pooling_epa1	sssd12-05
batch0812_nc	ex1252a	ghg_1veh	multiplants_mtg1a	prob07	sssd15-04
batches201210m	ex14_1_1	ghg_3veh	no7_ar3_1	process	sssd16-07
bayes2_50	ex4_1_5	glider100	nous1	procsyn	sssd18-06
blend480	ex6_1_1	graphpart_2g-0066-006809	nvs22	prolog	sssd20-04
blend531	ex6_2_12	gsg_0001	o7	qp3	sssd25-04
blend718	ex7_2_4	hda	o7_2	routingdelay_bigm	st_e35
blend852	ex8_1_7	heatexch_trigen	o7_ar25_1	rsyn0805m02h	stockcycle
carton7	ex8_2_1b	house	o7_ar3_1	sepasequ_convent	supplycha
casctanks	ex8_4_1	jbearing25	o7_ar4_1	sfacloc2_2_80	syn10m03h
cecil_13	filter	johnall	o7_ar5_1	slay07h	syn15m02h
chem	fin2bb	kall_circles_c6a	o8_ar4_1	slay09h	syn20m02h
clay0203h	flay05h	kall_diffcircles_10	o9_ar4_1	slay10h	syn30h
clay0303h	fo7	launch	oil	smallinvDAXr1b020-022	syn30m02h
crudeoil_lee2_10	fo8	lop97icx	oil2	sporttournament14	syn40h
csched1a	fo8_ar25_1	mathopt5_7	parallel	sqfl1010-025	syn40m02h
edgexcross10-060	fo9	mhw4d		sssd08-04	

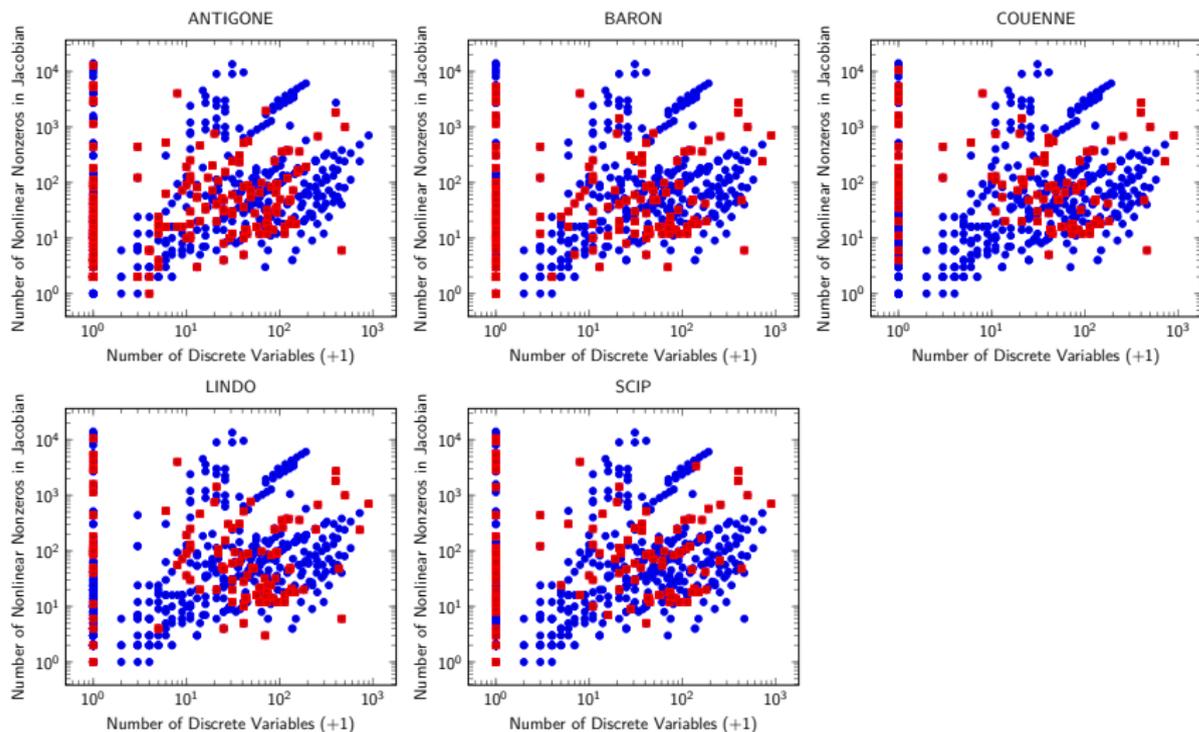
PITT test set for each solver

Removed easy and unsolvable instances:



PITTED test set for each solver

Removed easy and unsolvable instances, then filter by name:



Run jobs

date	GAMS	ANTIGONE	BARON	COUENNE	LINDO	SCIP
08/11	23.7.3	–	9.3.1	0.3	6.1.1.588	–
04/12	23.8.2	–	10.2.0	0.4	7.0.1.421	2.1.1
11/12	23.9.5	–	11.5.2	0.4	7.0.1.497	2.1.2
02/13	24.0.2	–	11.9.1	0.4	7.0.1.497	3.0
07/13	24.1.3	1.1	12.3.3	0.4	8.0.1283.385	3.0
05/14	24.2.3	1.1	12.7.7	0.4	8.0.1694.498	3.0
09/14	24.3.3	1.1	14.0.3	0.4	8.0.1694.550	3.1
06/15	24.4.6	1.1	14.4.0	0.4	9.0.1983.157	3.1
11/15	24.5.6	1.1	15.9.22	0.5	9.0.2120.225	3.2
01/16	24.6.1	1.1	15.9.22	0.5	9.0.2120.225	3.2
09/16	24.7.4	1.1	16.8.24	0.5	9.0.2217.293	3.2
05/17	24.8.5	1.1	17.4.1	0.5	10.0.2539.182	3.2
11/17	24.9.2	1.1	17.10.16	0.5	11.0.3802.300	4.0

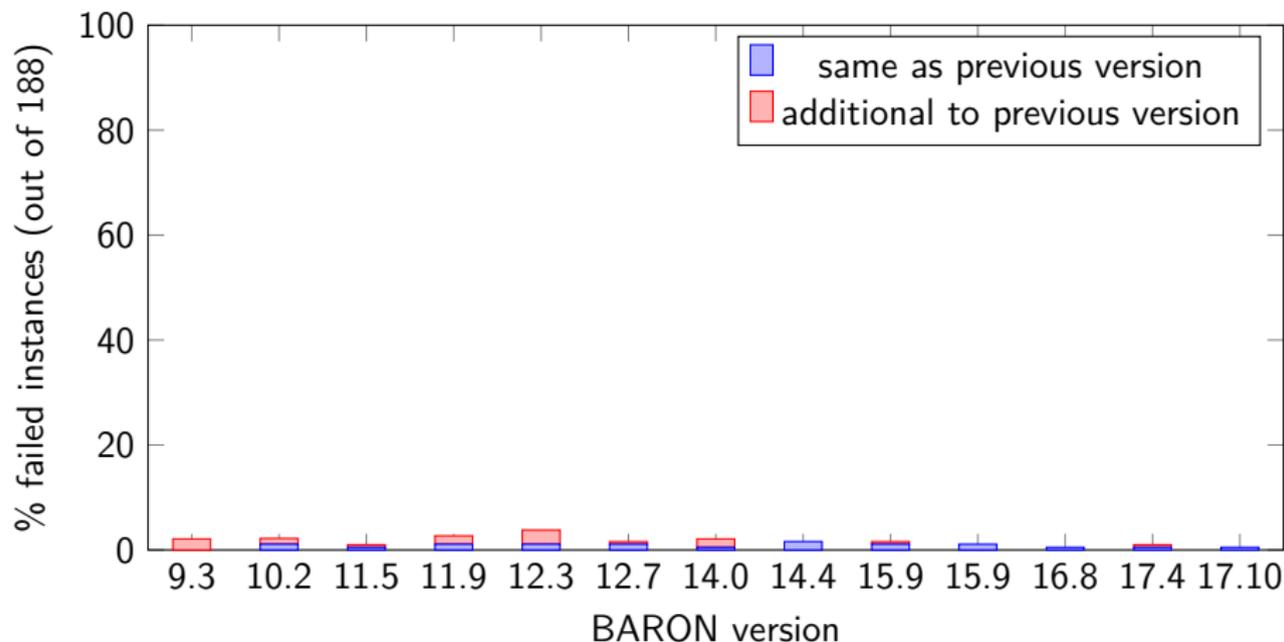
```
for GAMS in $GAMSS ; do
  for SOLVER in $SOLVERS($GAMS) ; do
    for INSTANCE in $TESTSET($SOLVER) ; do
      sbatch --exclusive --time=0:1800 $GAMS $INSTANCE SOLVER=$SOLVER
    done
  done
done
```

Hardware: Dell PowerEdge M1000e, 48GB RAM, Intel Xeon X5672@3.2GHz

BARON: Fails

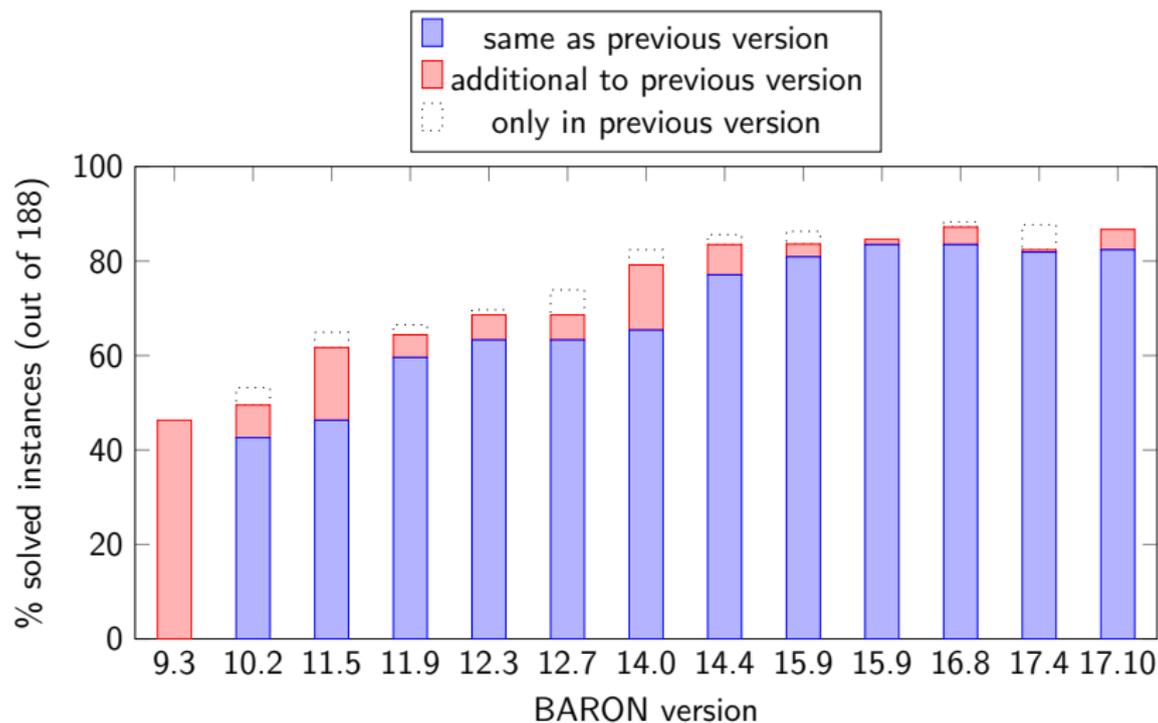
A solver **failed**, if it

- ▶ crashed, or
- ▶ reported an infeasible point as feasible (tolerance: 10^{-4}), or
- ▶ reported a suboptimal solution as optimal (tolerance: 10^{-4})

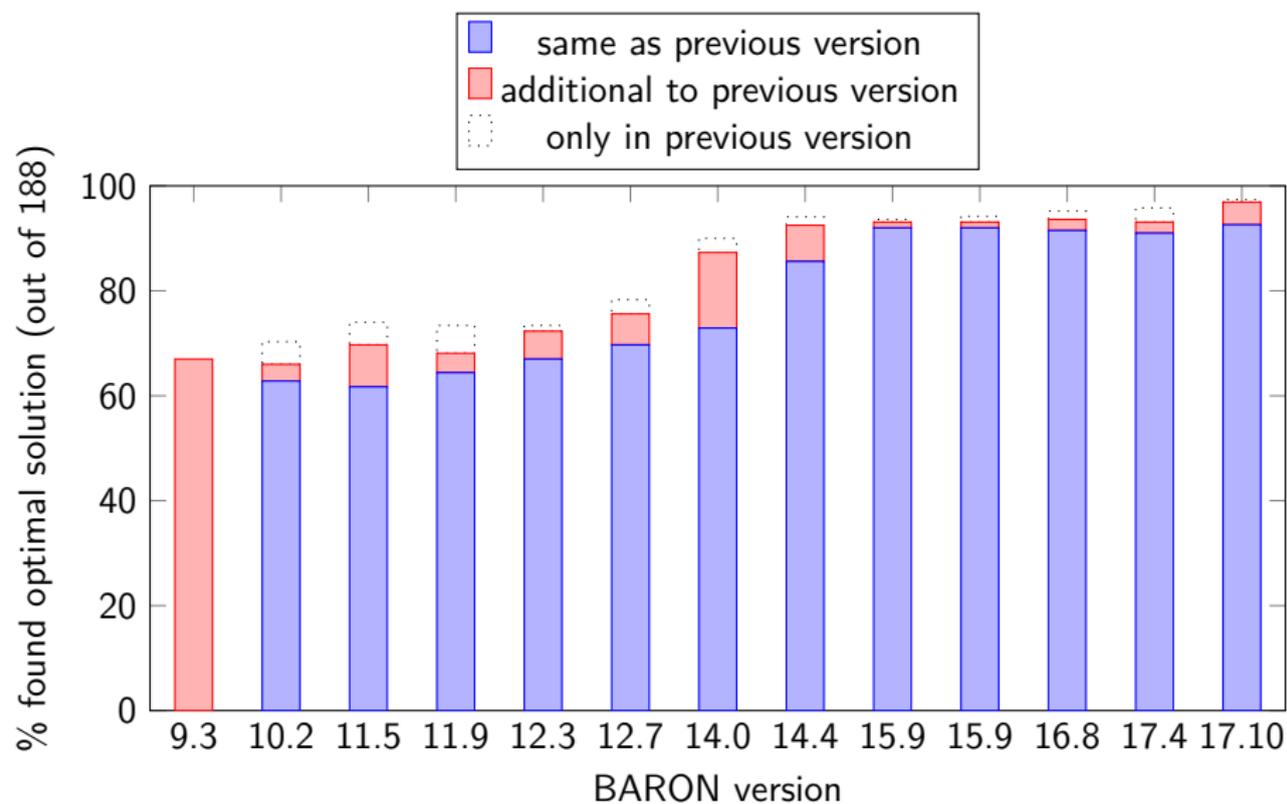


BARON: Solved

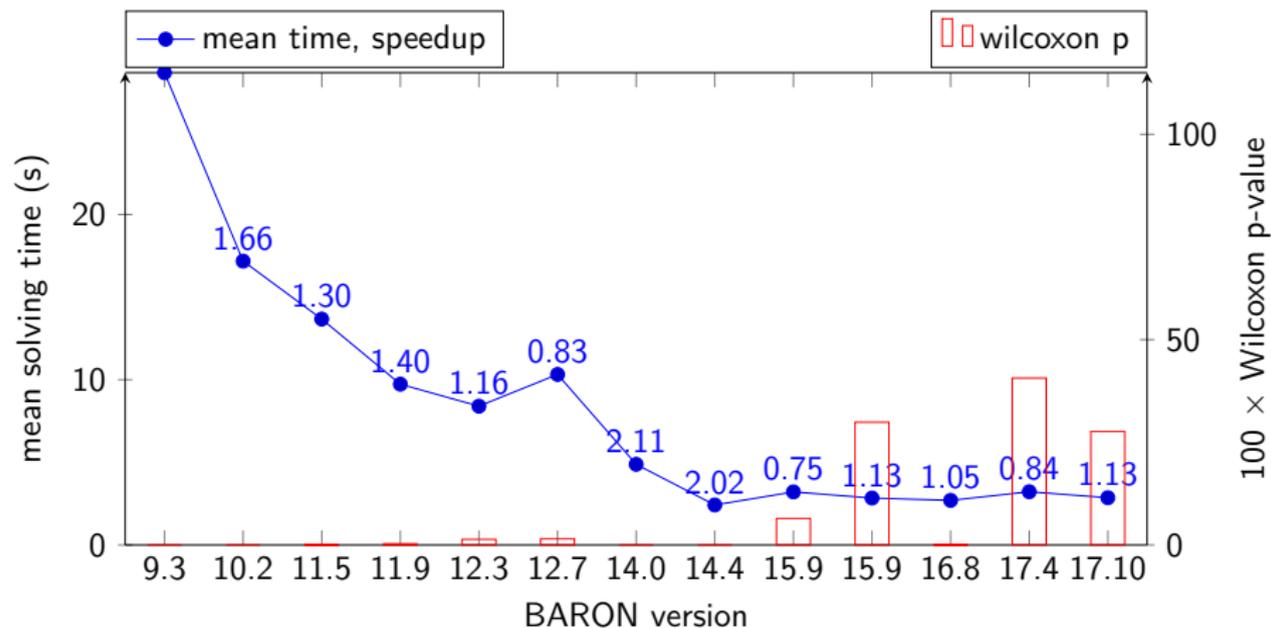
Solved: solver did **not fail** and reports a relative optimality gap $\leq 10^{-4}$



BARON: Found optimal solution



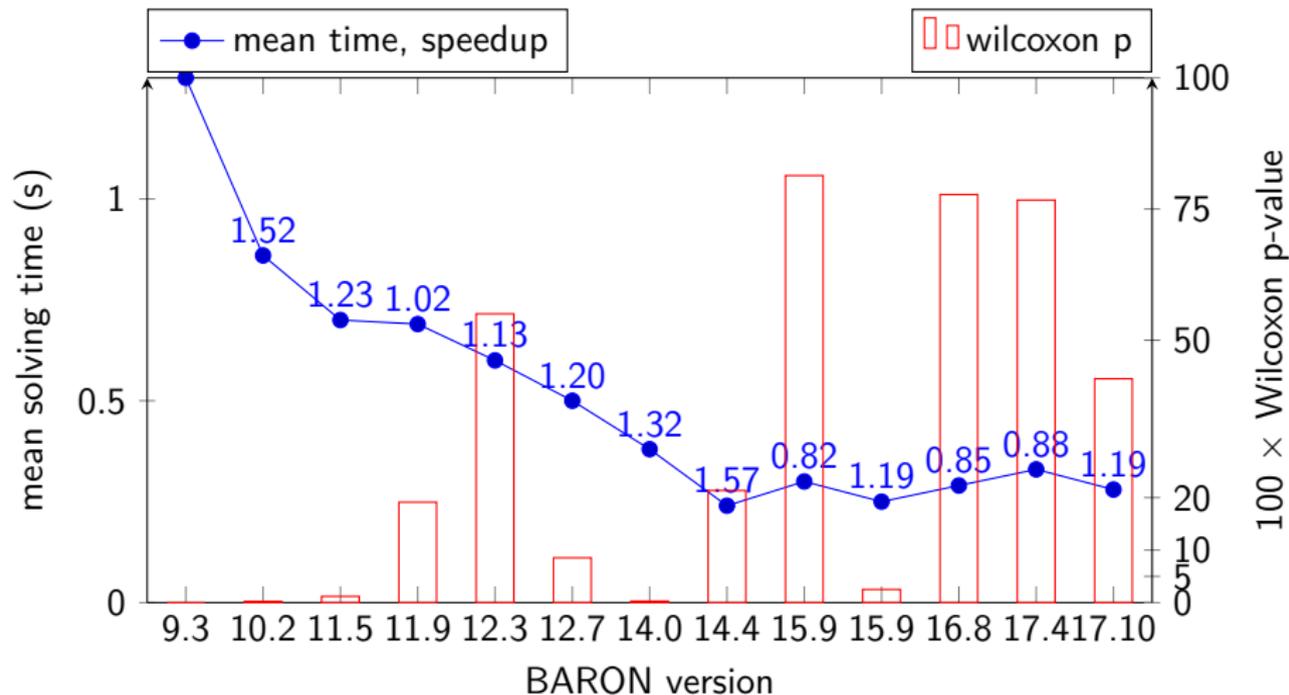
BARON: Solving time on instances that never failed (169)



Overall speedup: 10.1

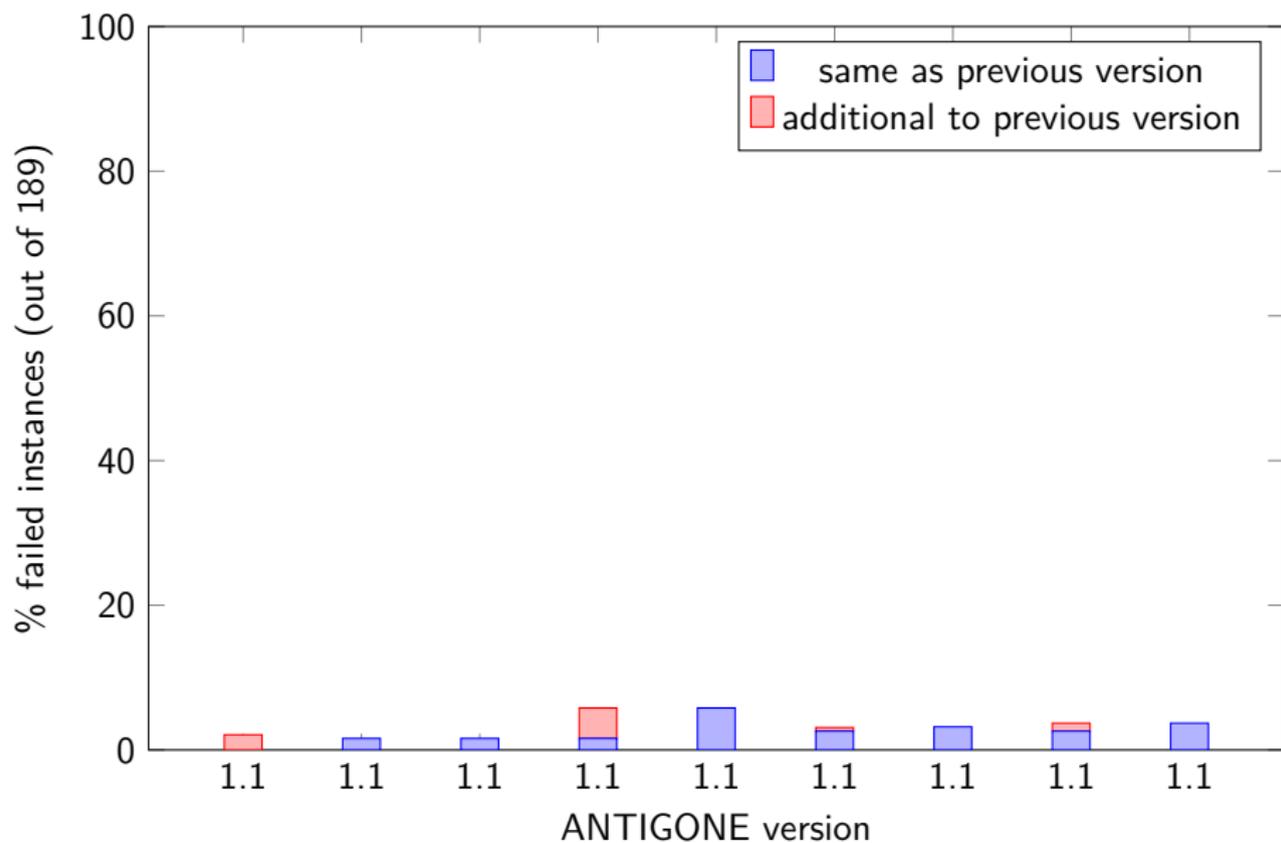
12.7: "Automatic setting of many options based on problem characteristics and learning algorithms."

BARON: Solving time on instances solved by all vers. (71)

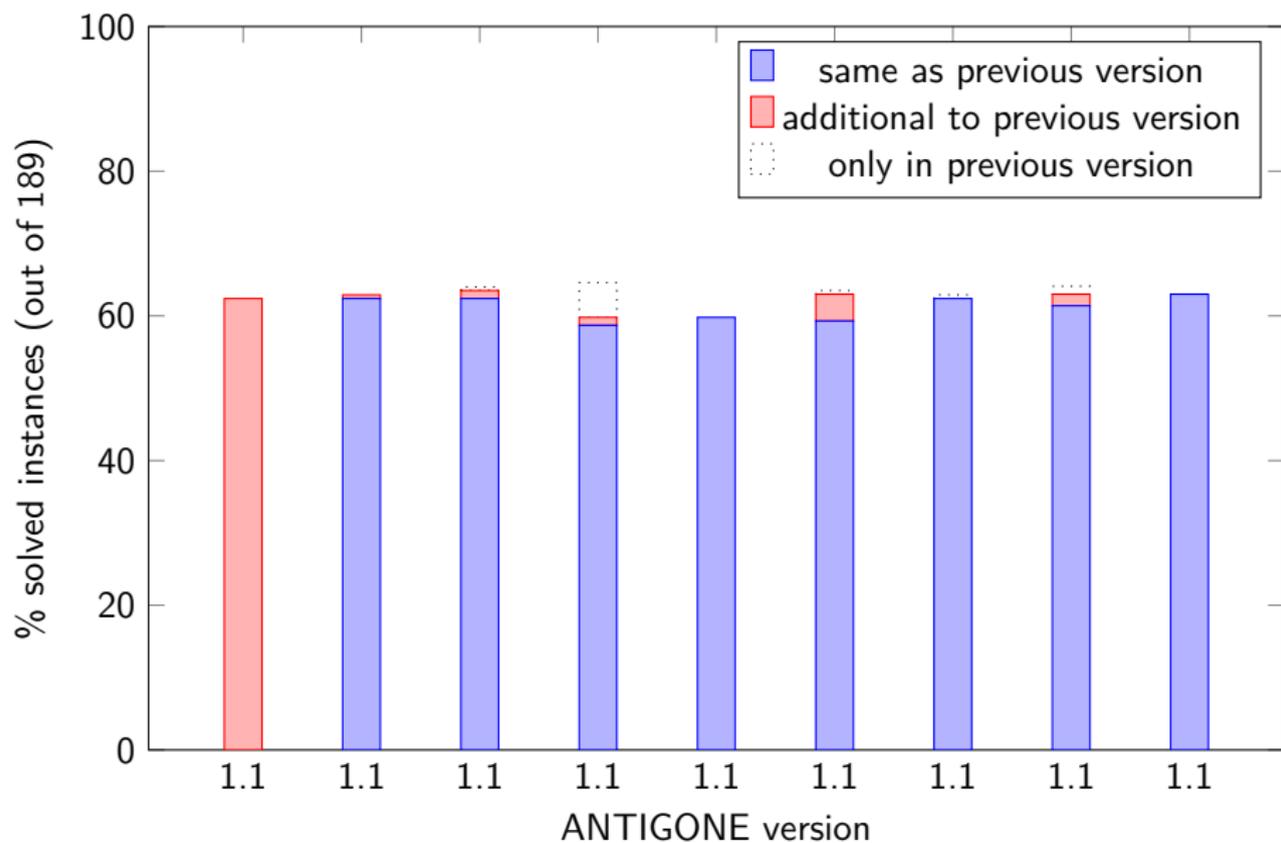


Overall speedup: 4.7

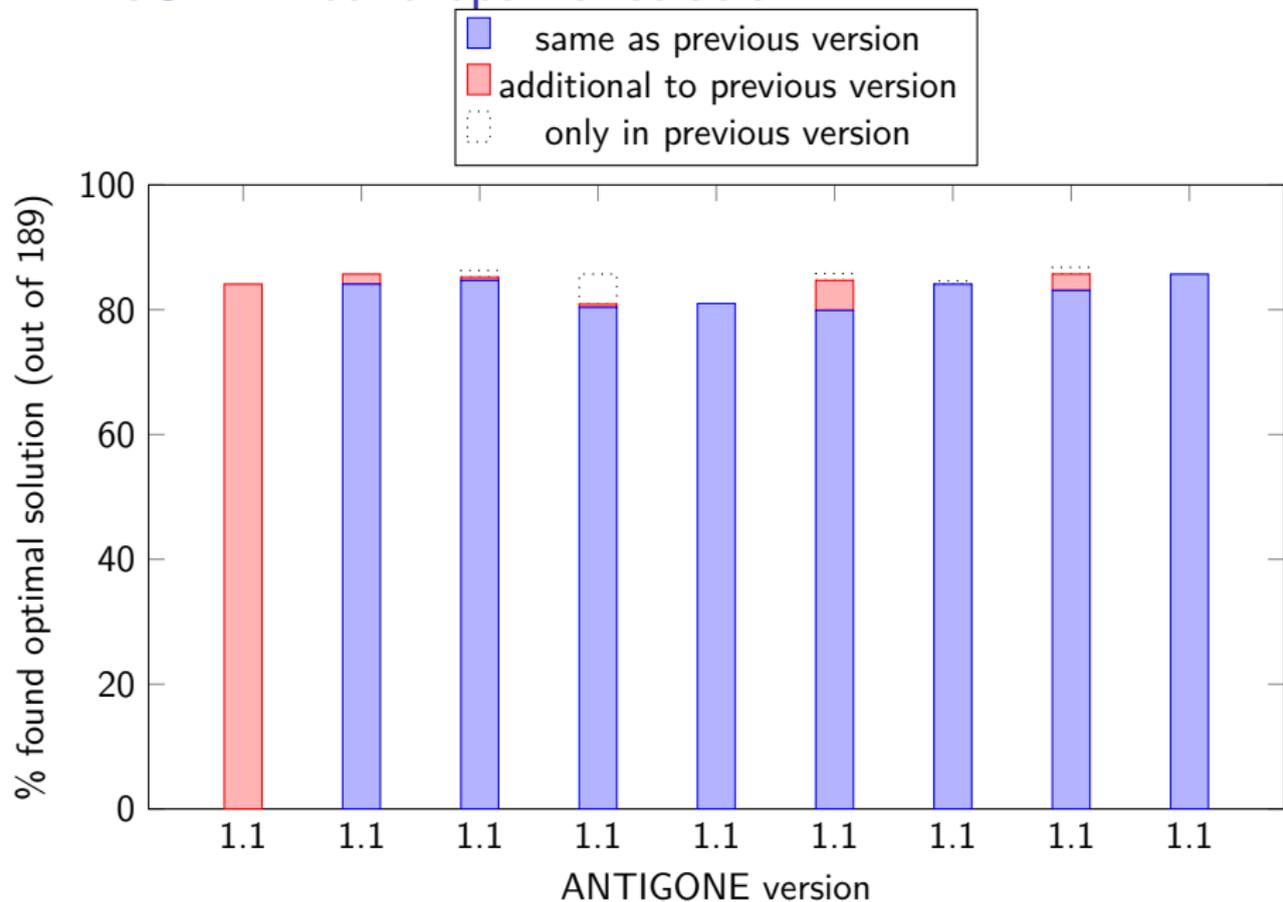
ANTIGONE: Fails



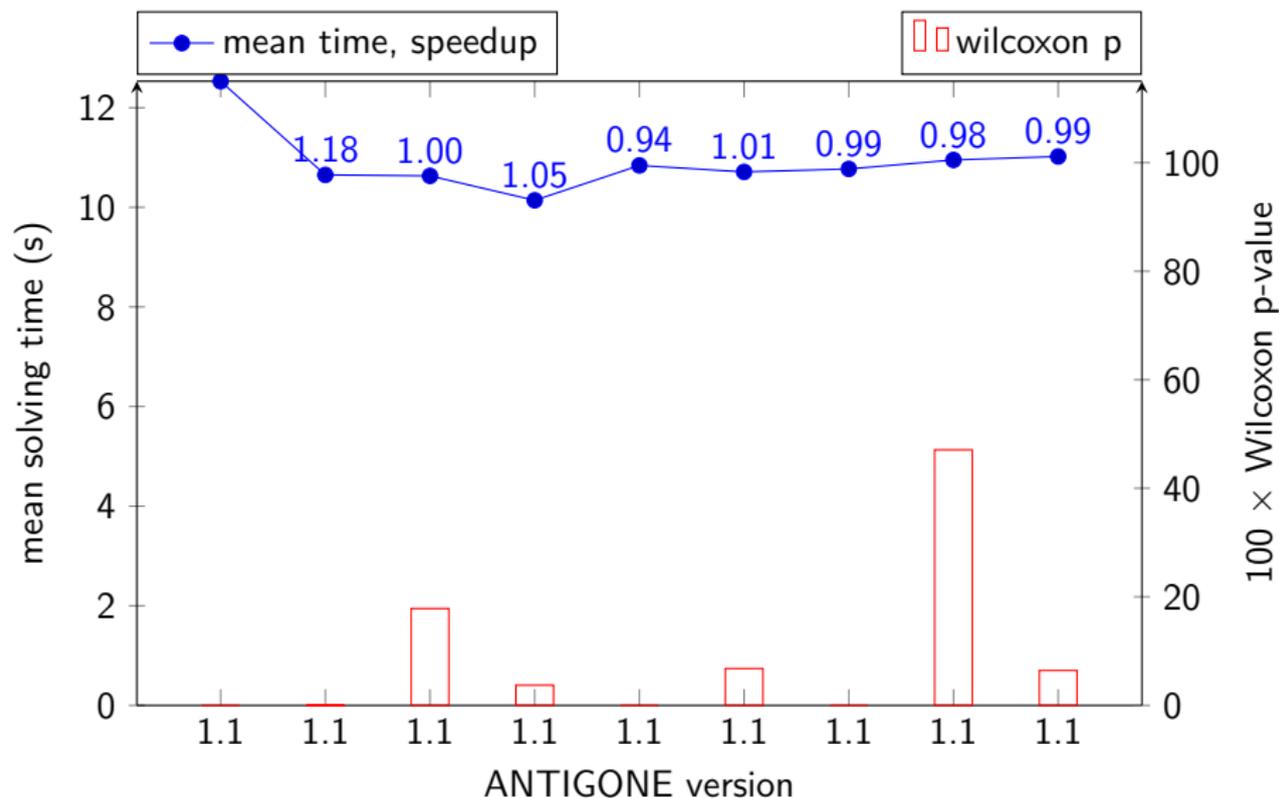
ANTIGONE: Solved



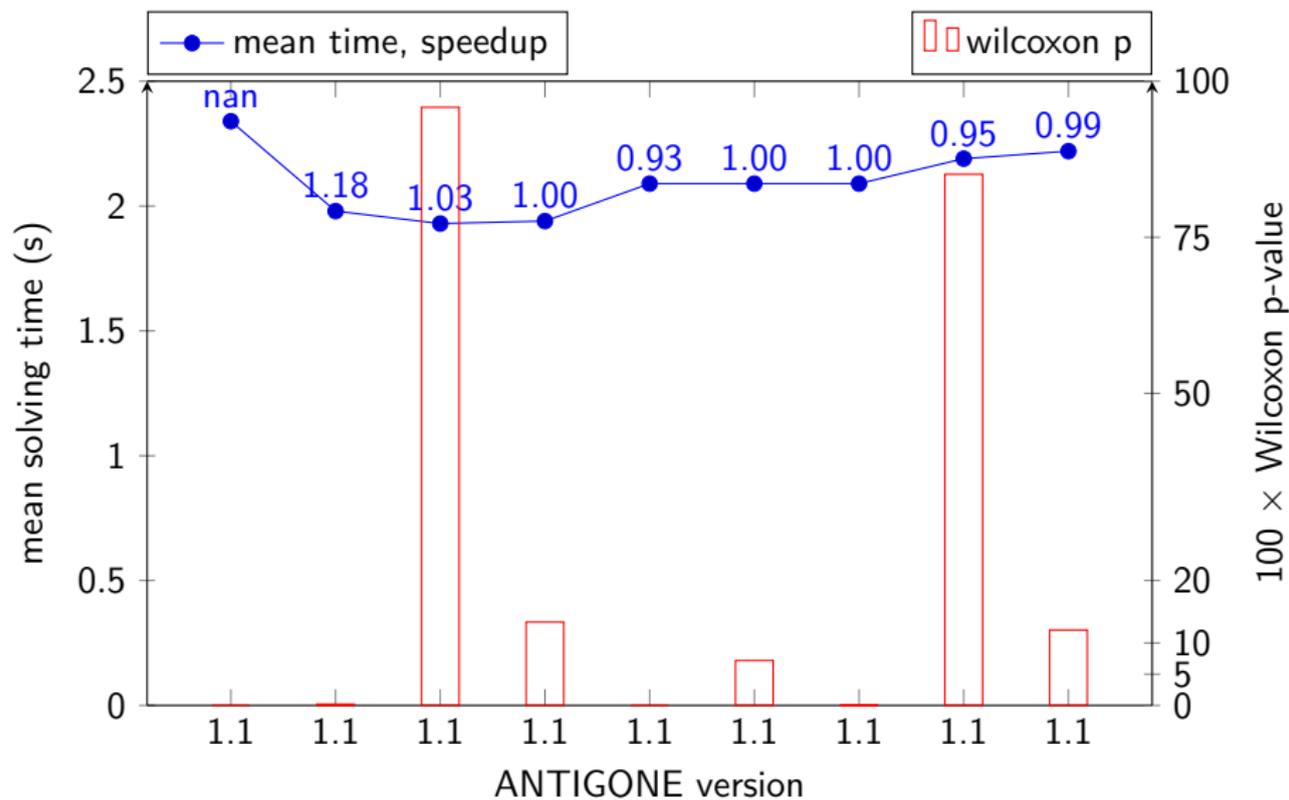
ANTIGONE: Found optimal solution



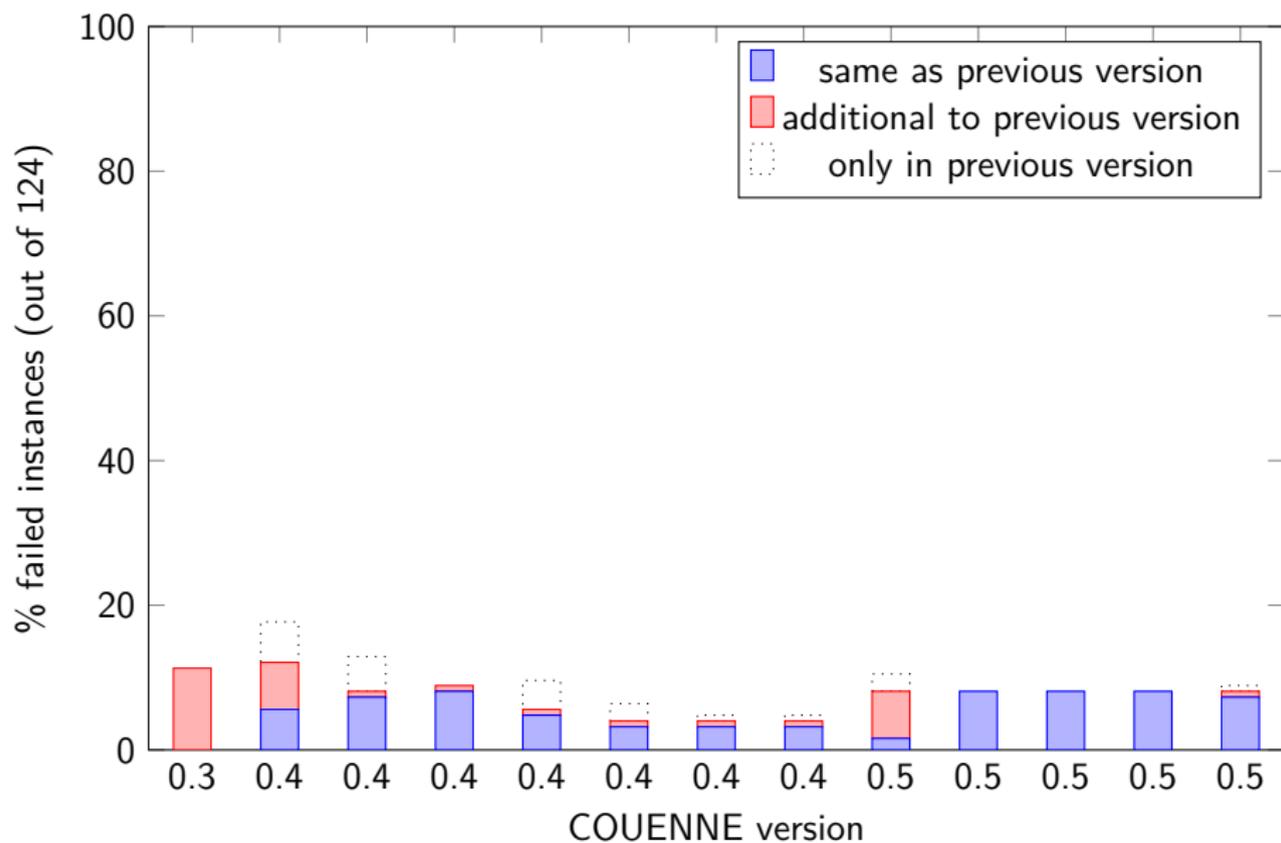
ANTIGONE: Solving time, instances that never failed (175)



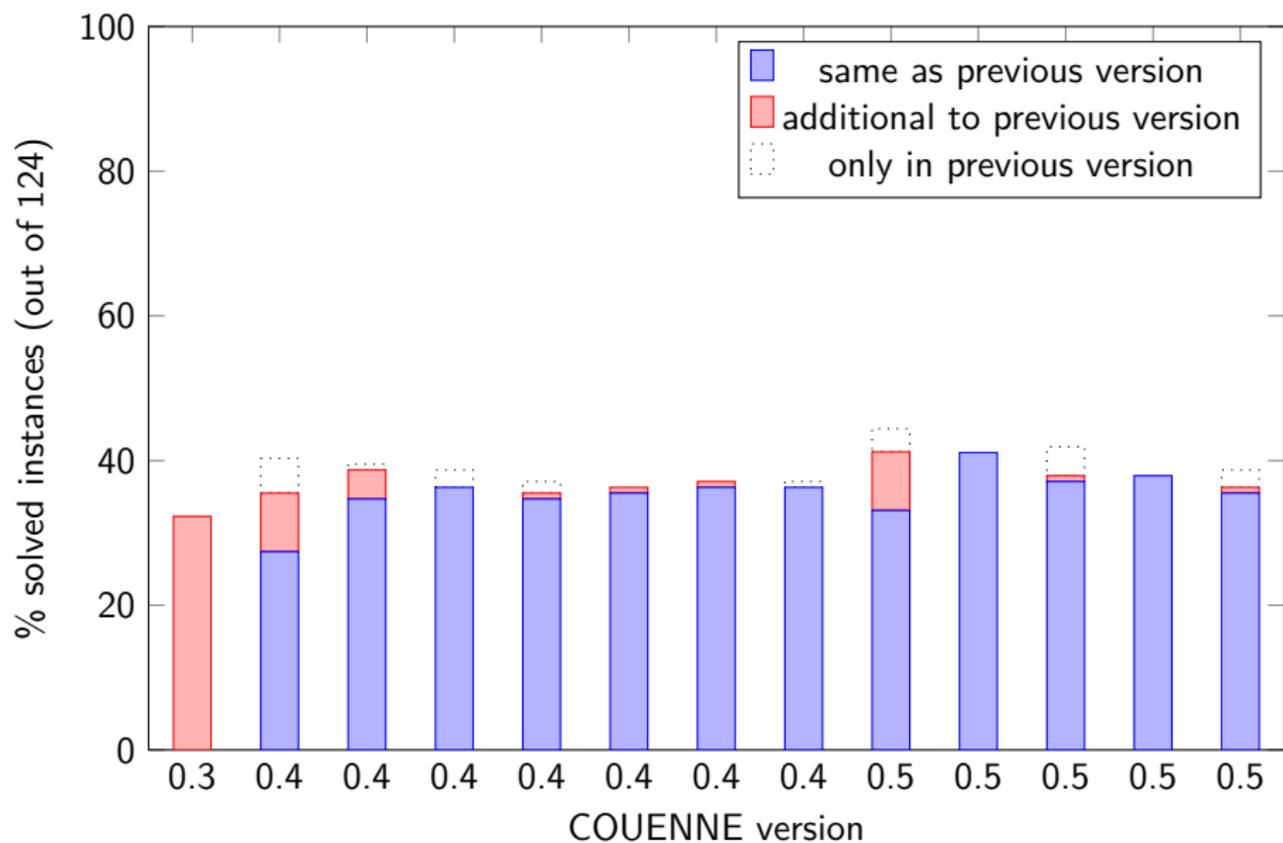
ANTIGONE: Solving time on instances solved by all (109)



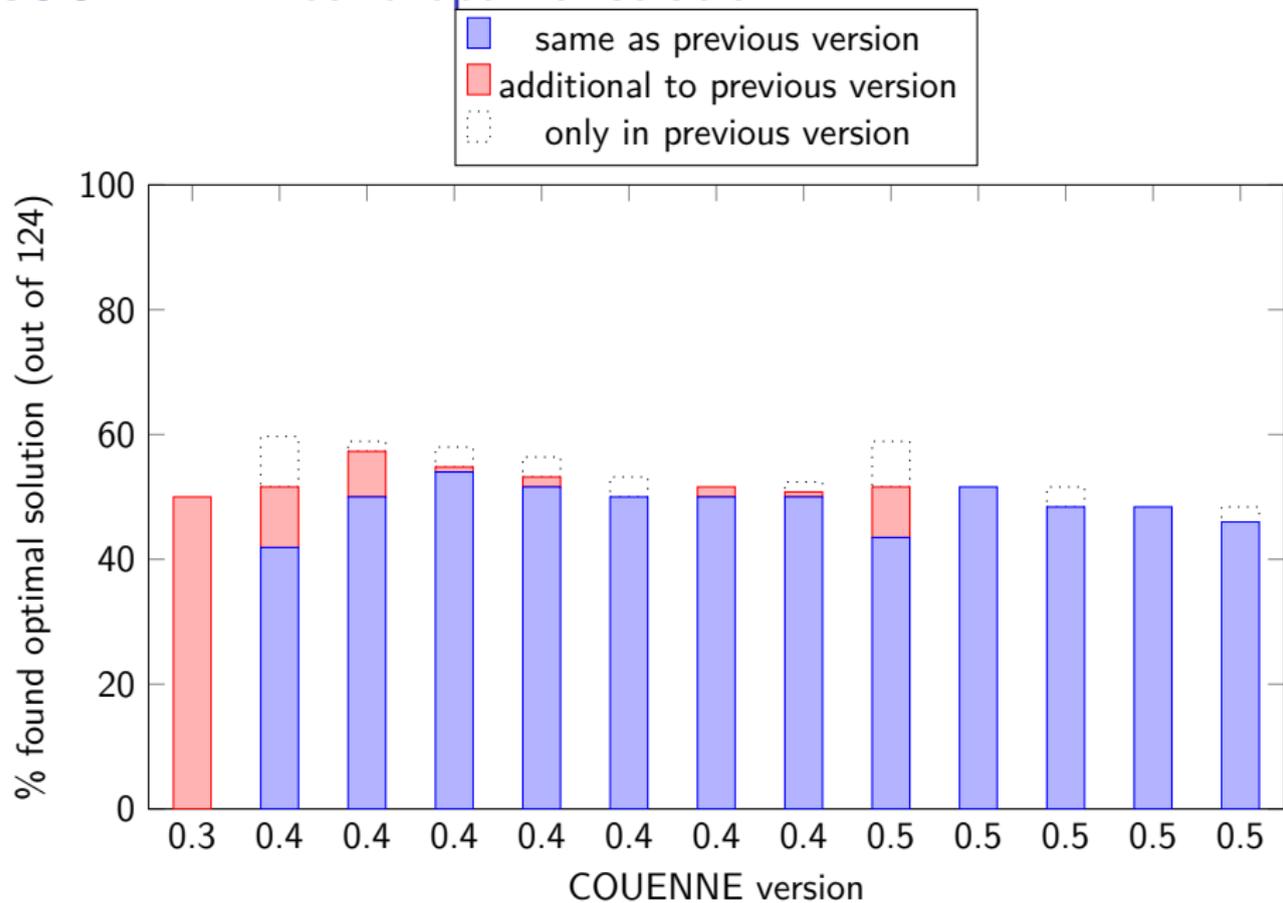
COUENNE: Fails



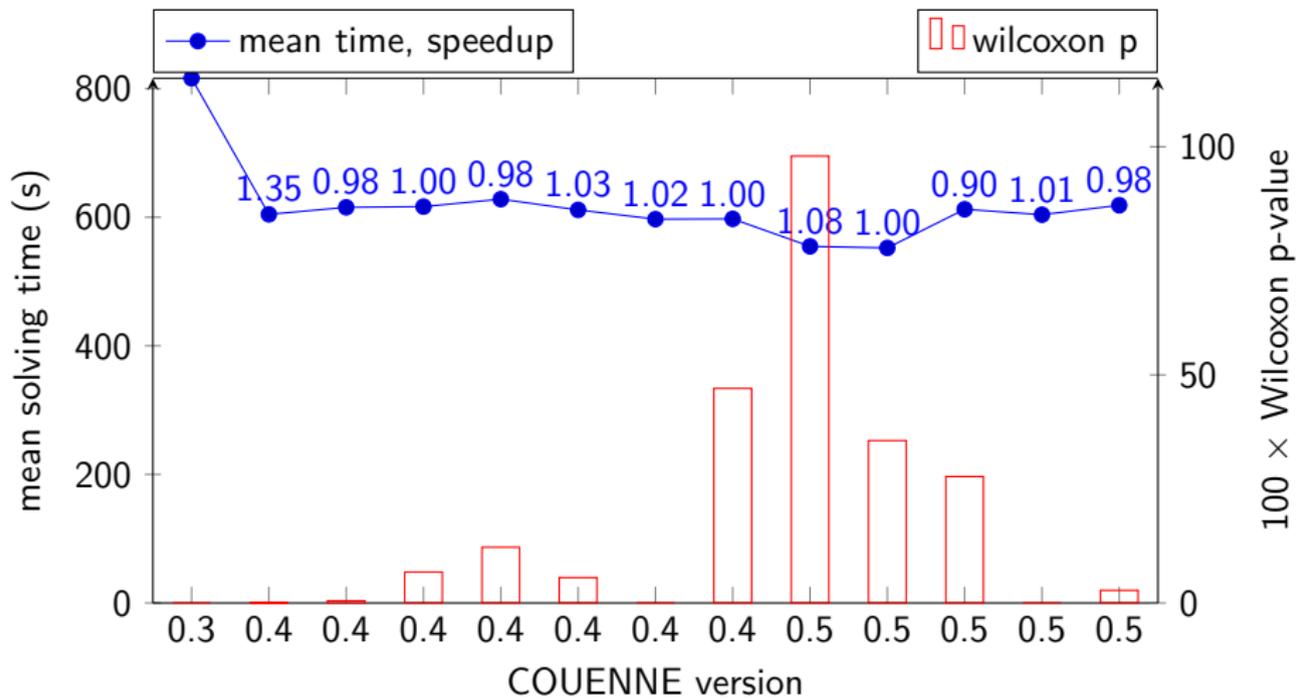
COUENNE: Solved



COUENNE: Found optimal solution

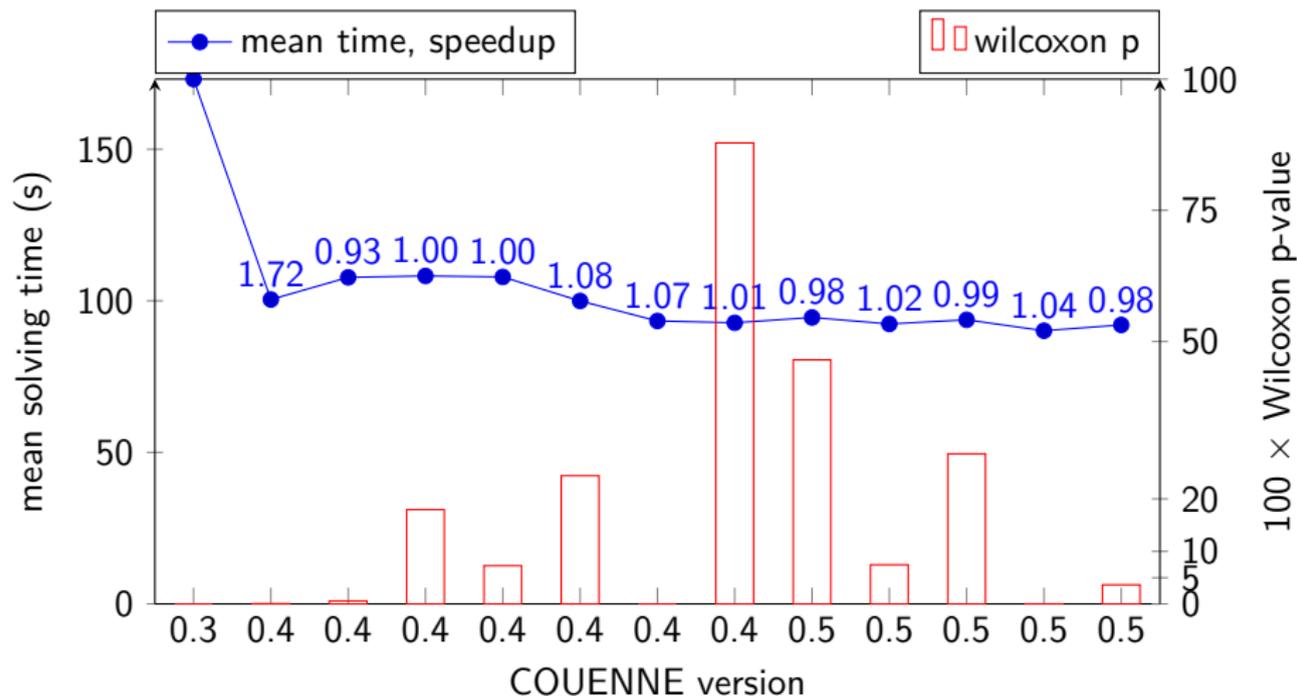


COUENNE: Solving time, instances that never failed (96)



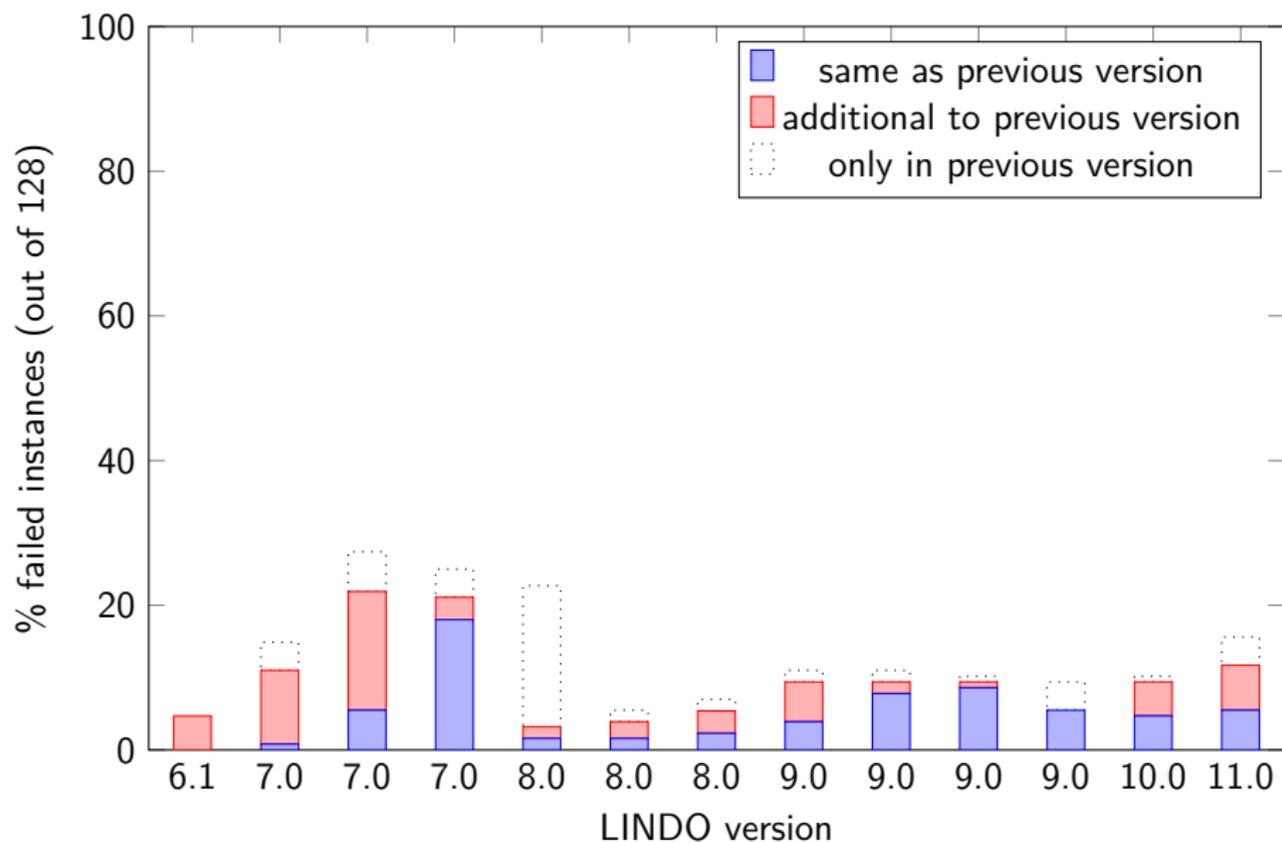
Overall speedup: 1.3

COUENNE: Solving time on instances solved by all (27)

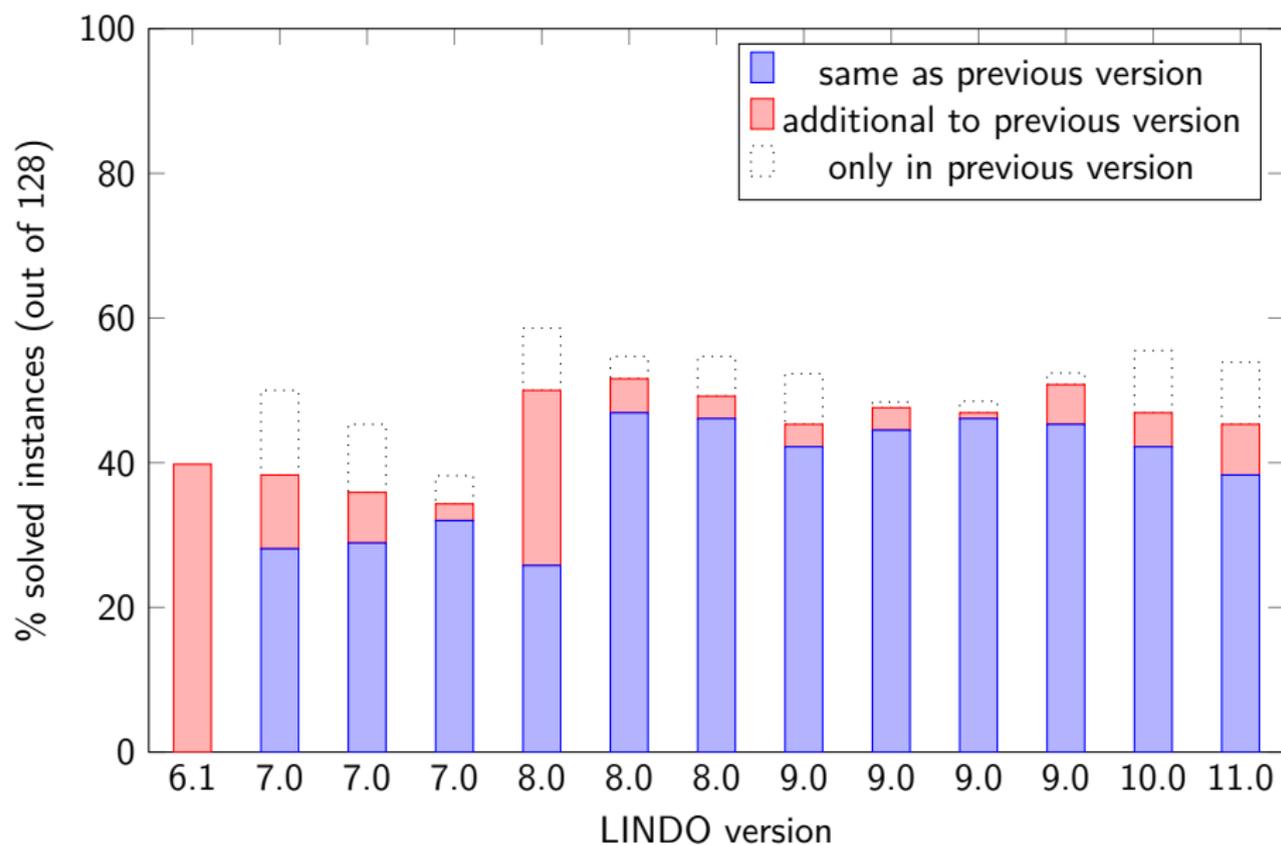


Overall speedup: 1.9

LINDO: Fails

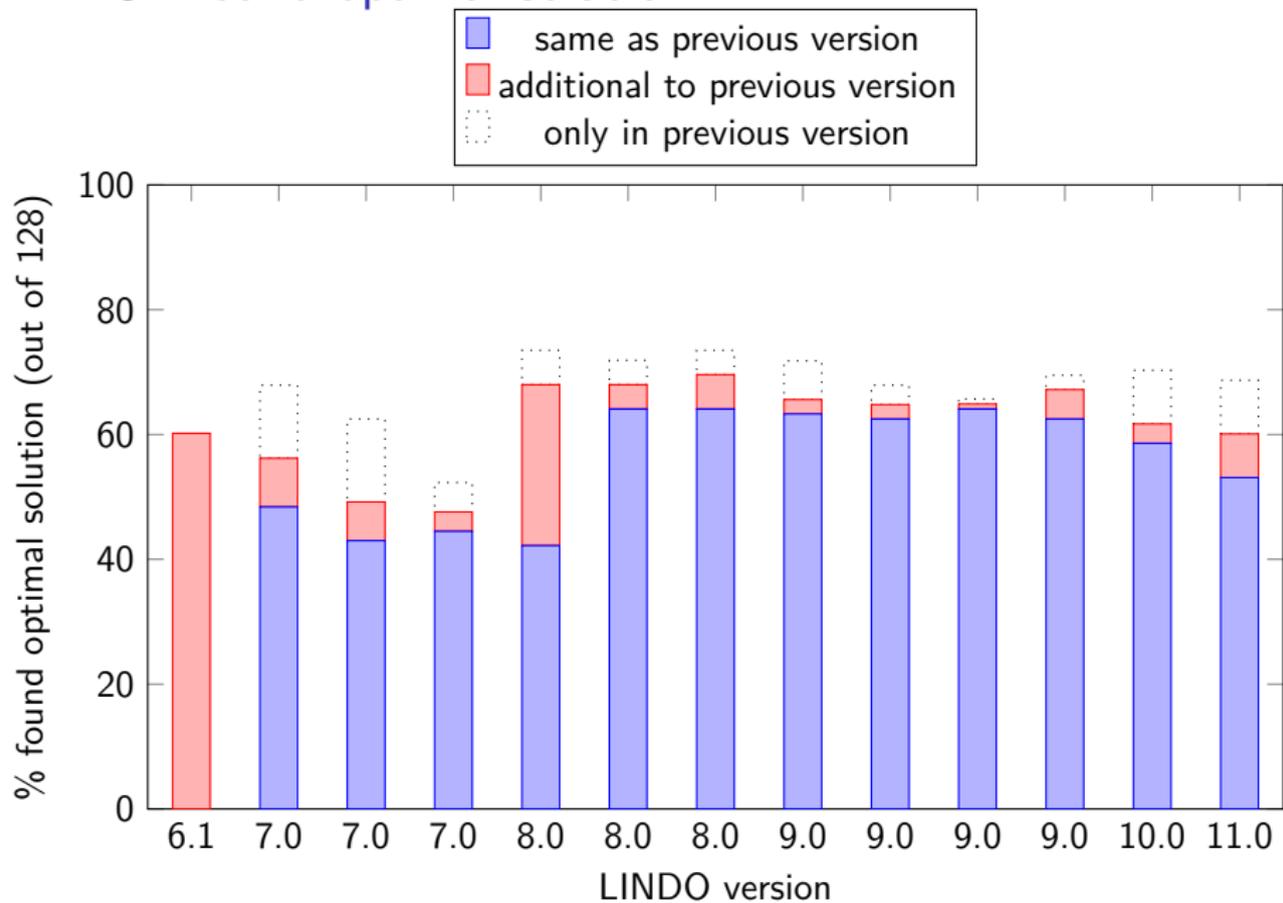


LINDO: Solved

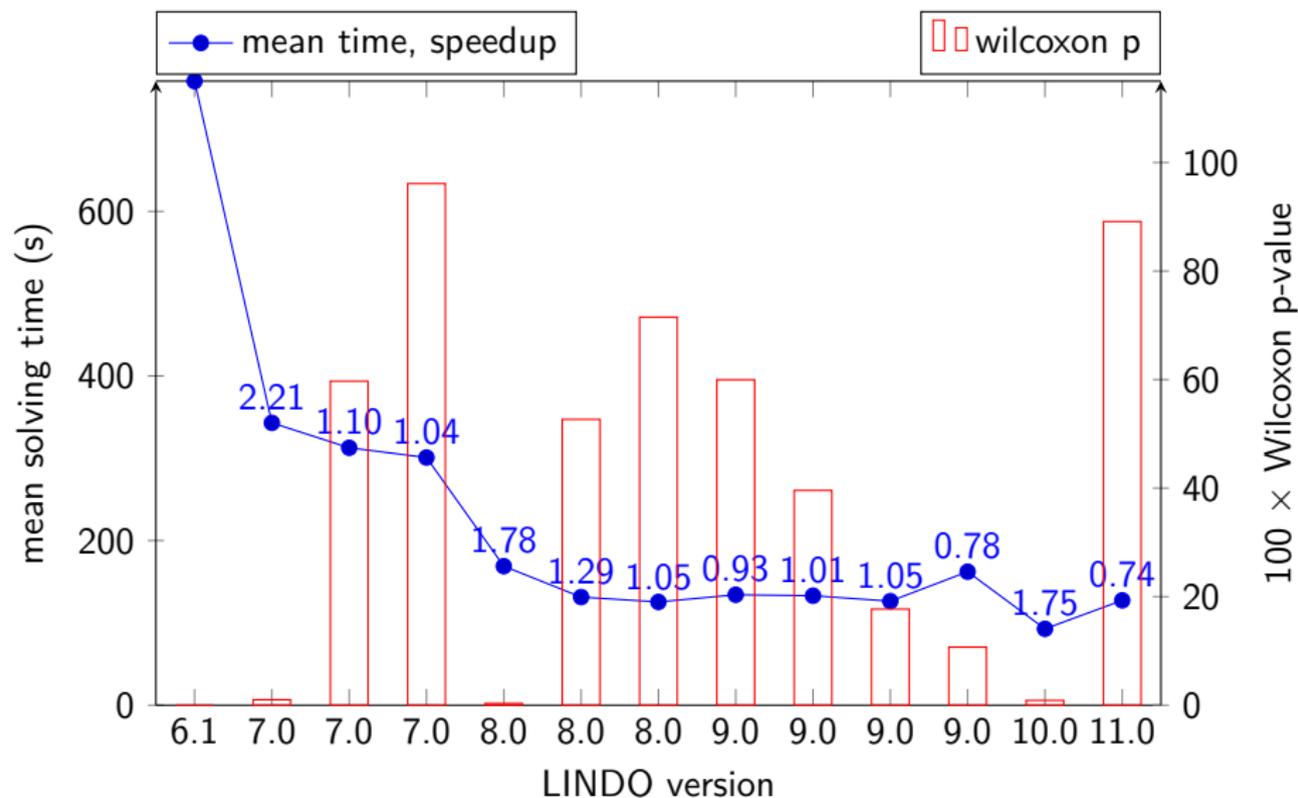


LINDO 8.0: improvements in primal heuristics for MIP (feas. pump) and

LINDO: Found optimal solution

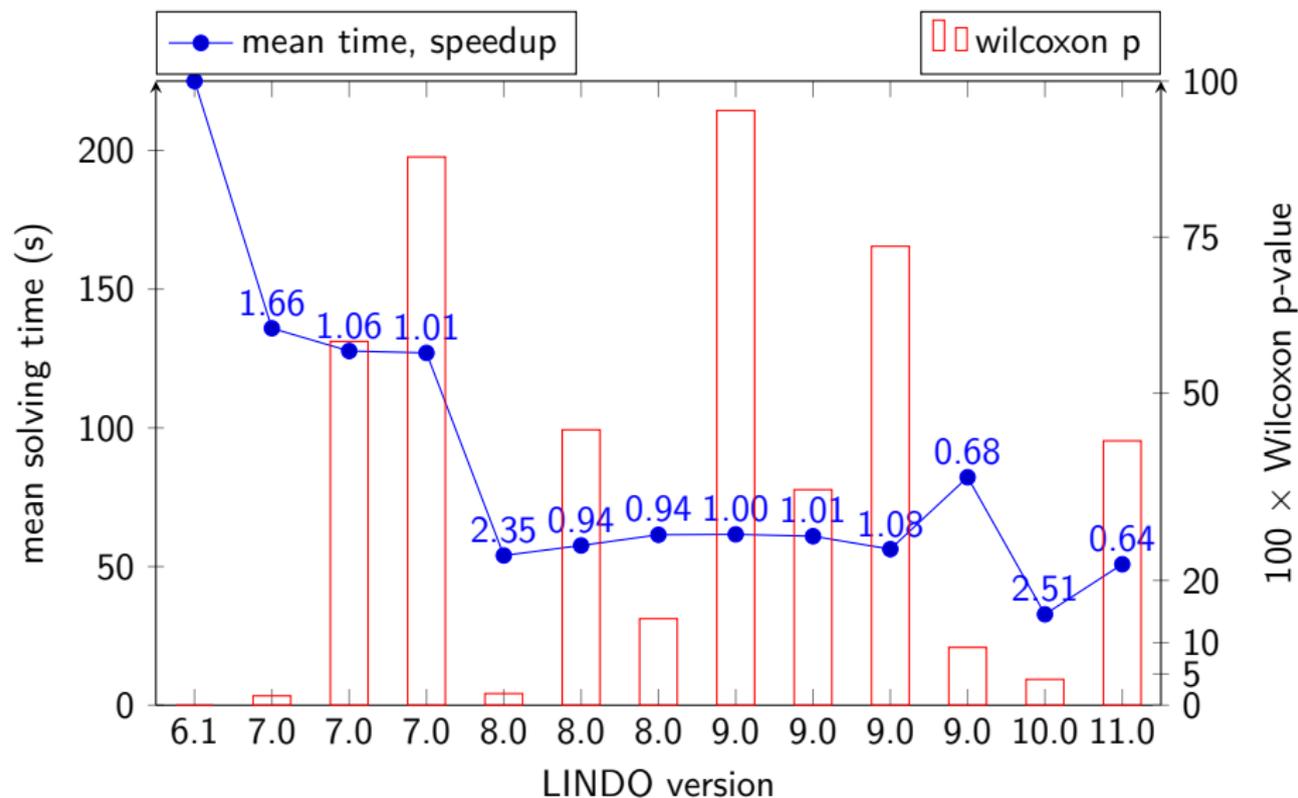


LINDO: Solving time on instances that never failed (76)



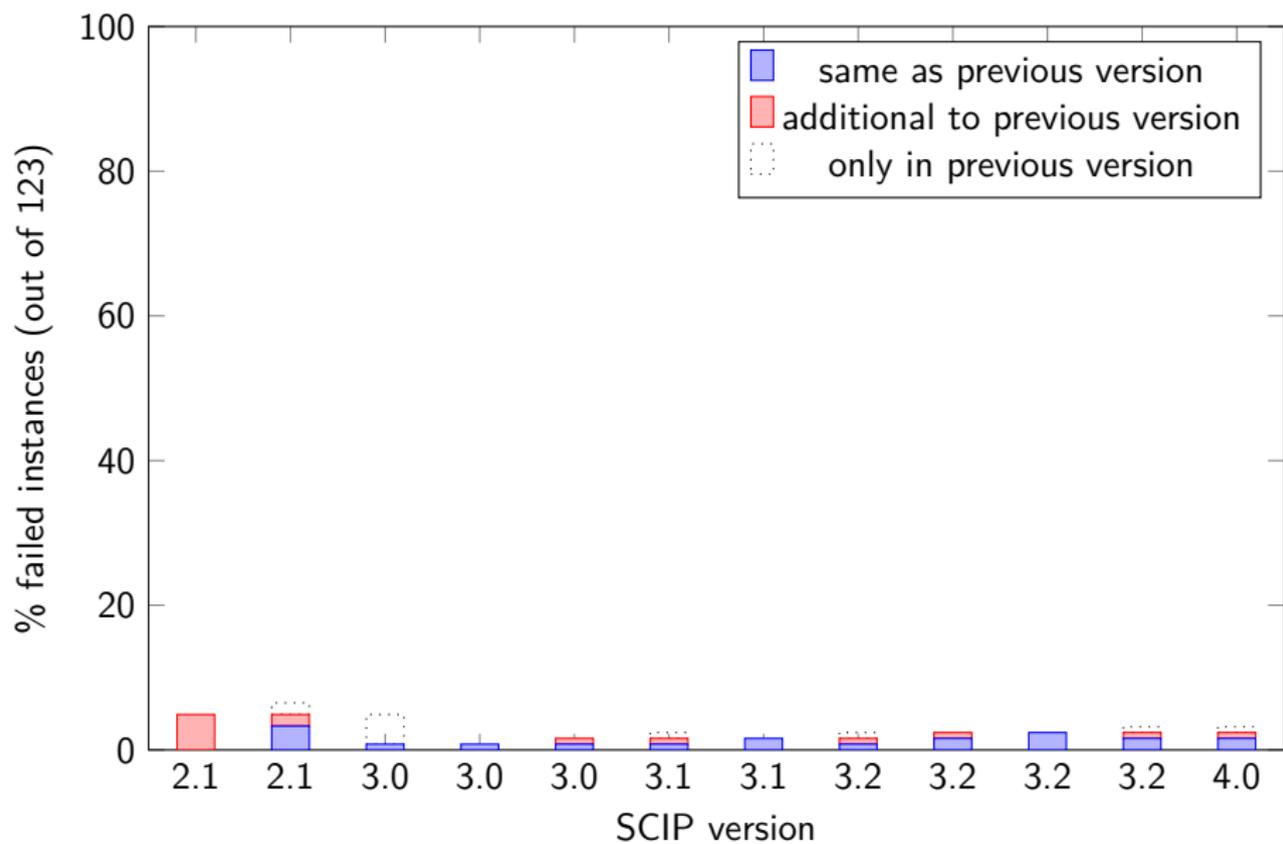
Overall speedup: 6.0

LINDO: Solving time on instances solved by all vers. (12)

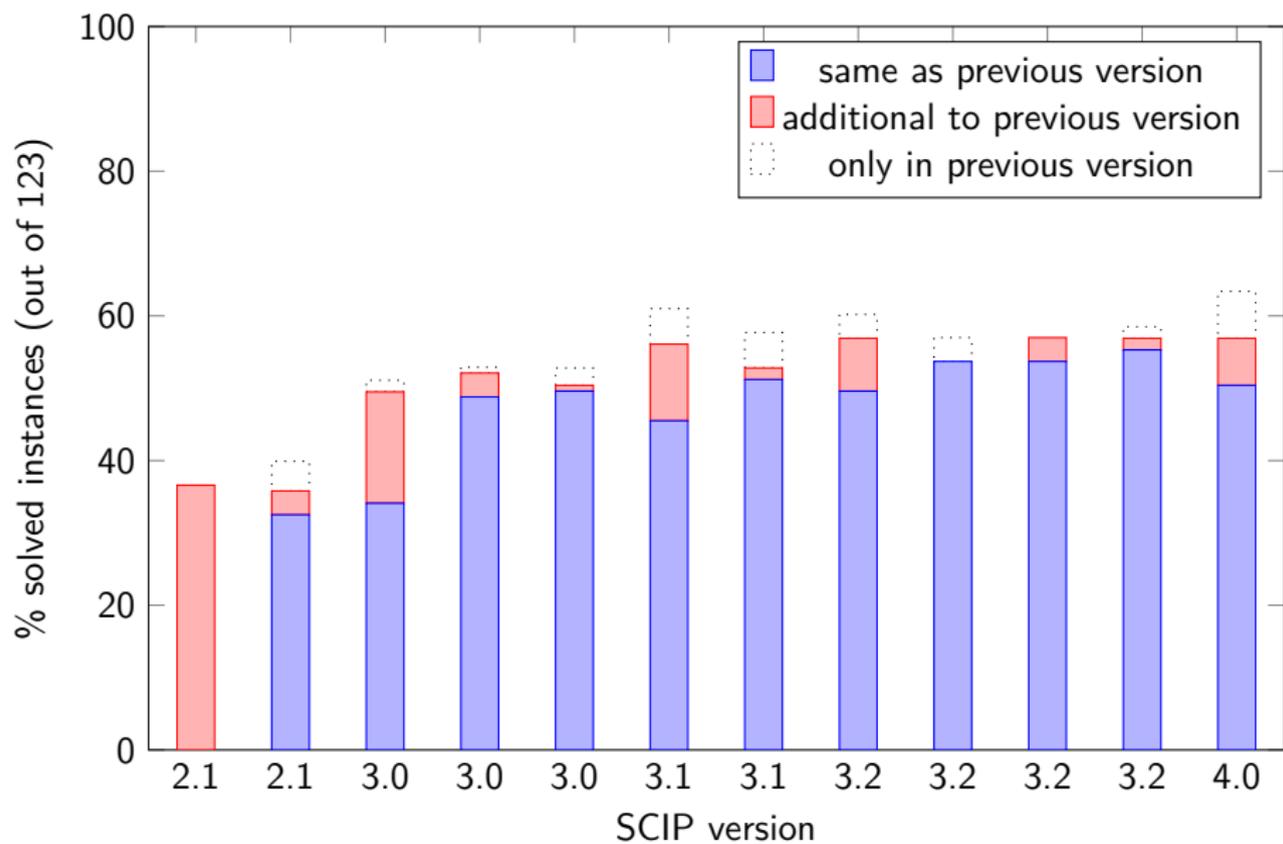


Overall speedup: 4.4

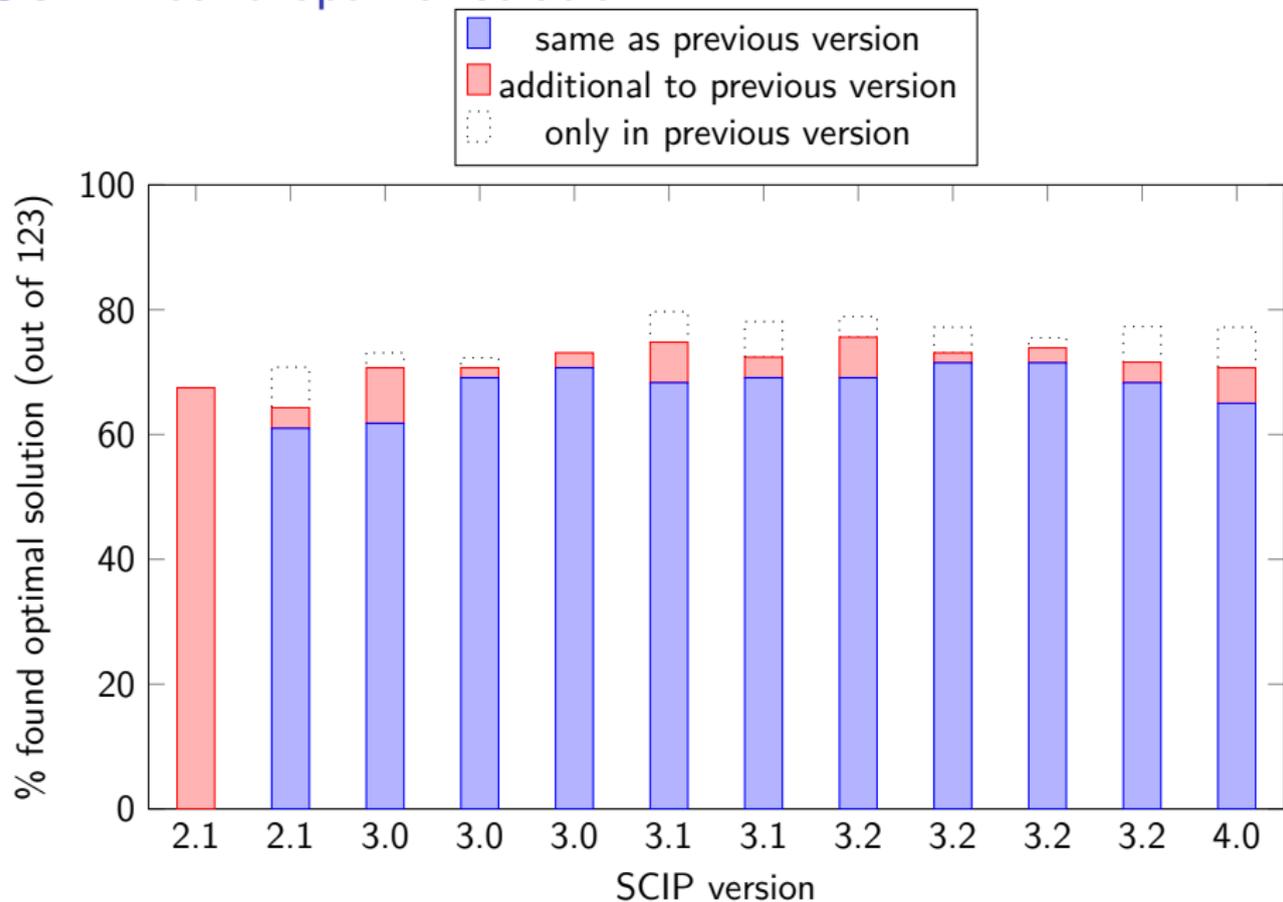
SCIP: Fails



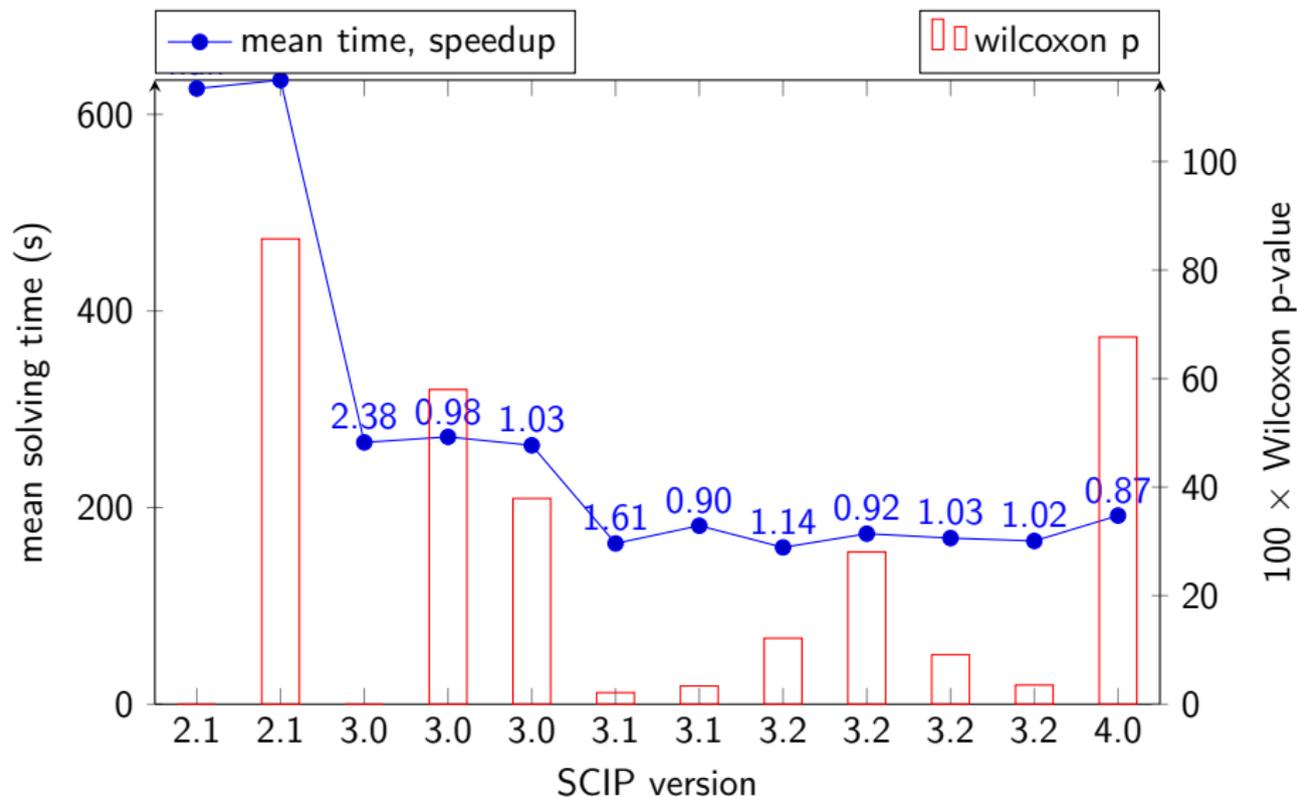
SCIP: Solved



SCIP: Found optimal solution

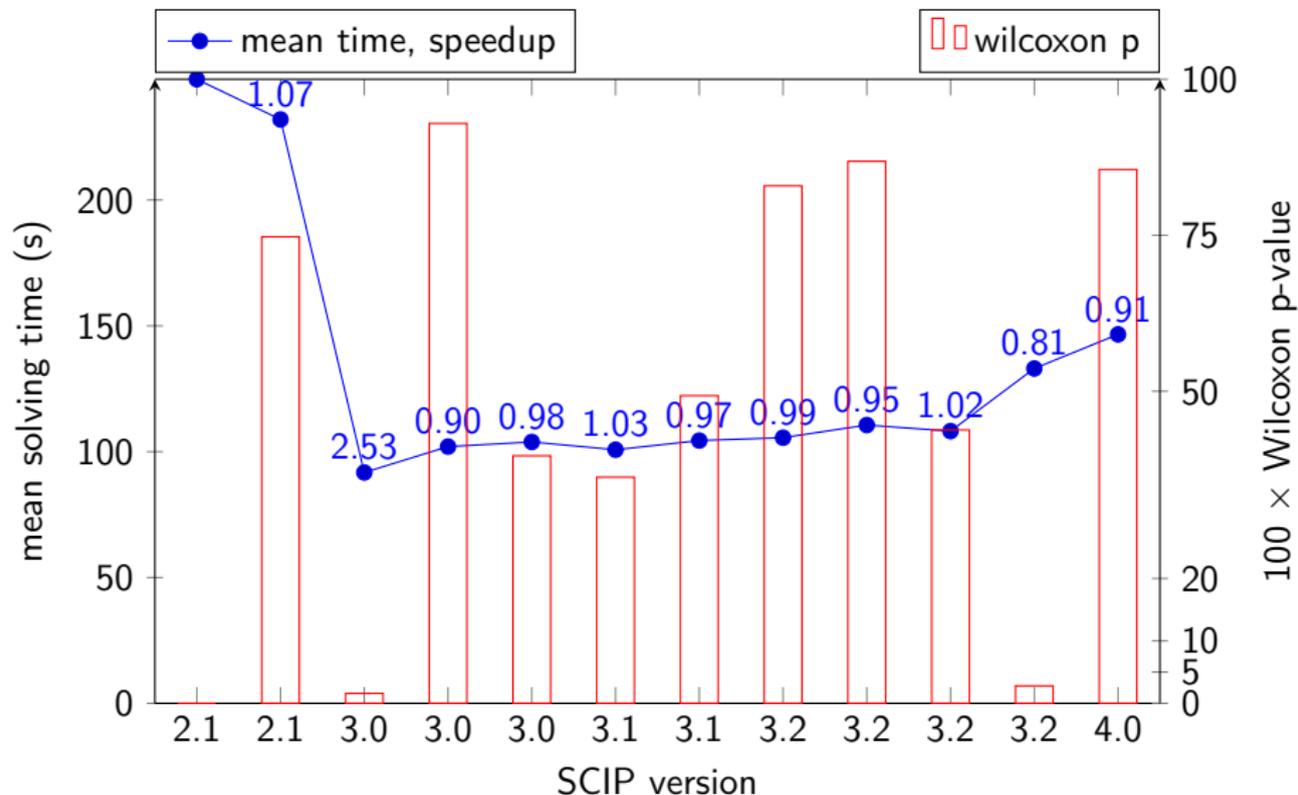


SCIP: Solving time on instances that never failed (111)



Overall speedup: 3.3

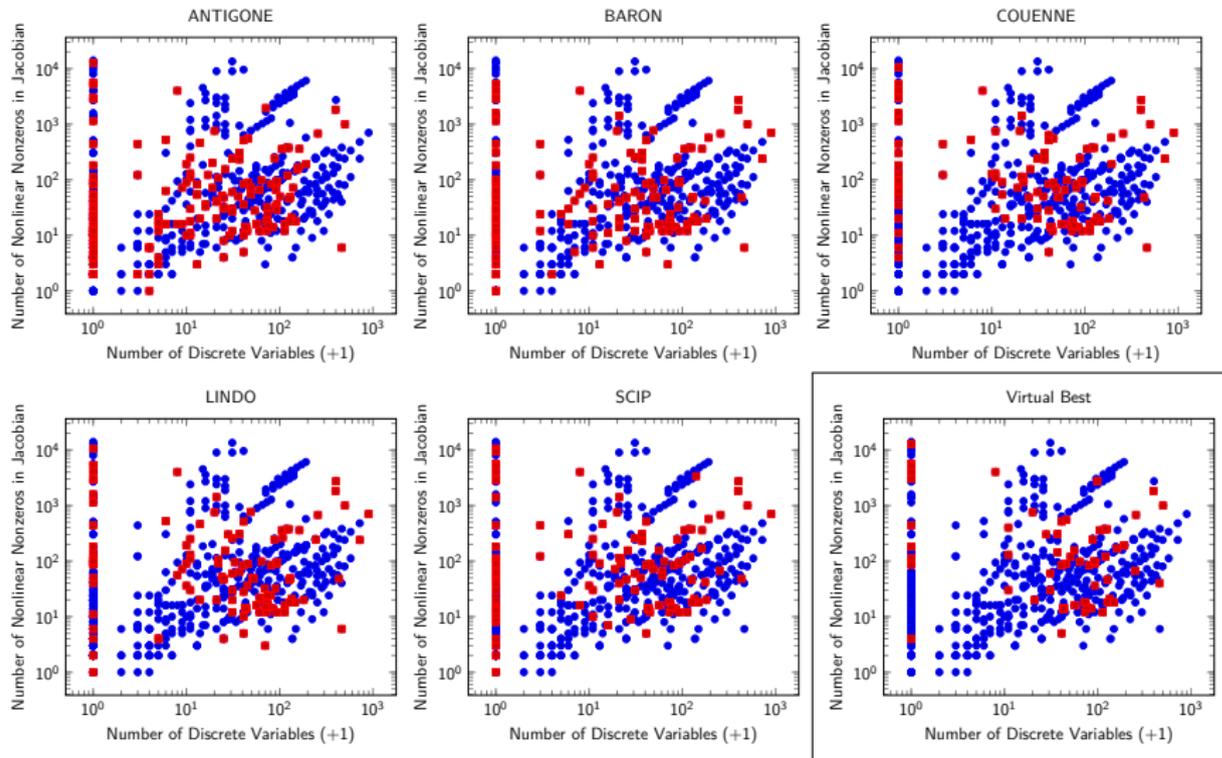
SCIP: Solving time on instances solved by all vers. (32)



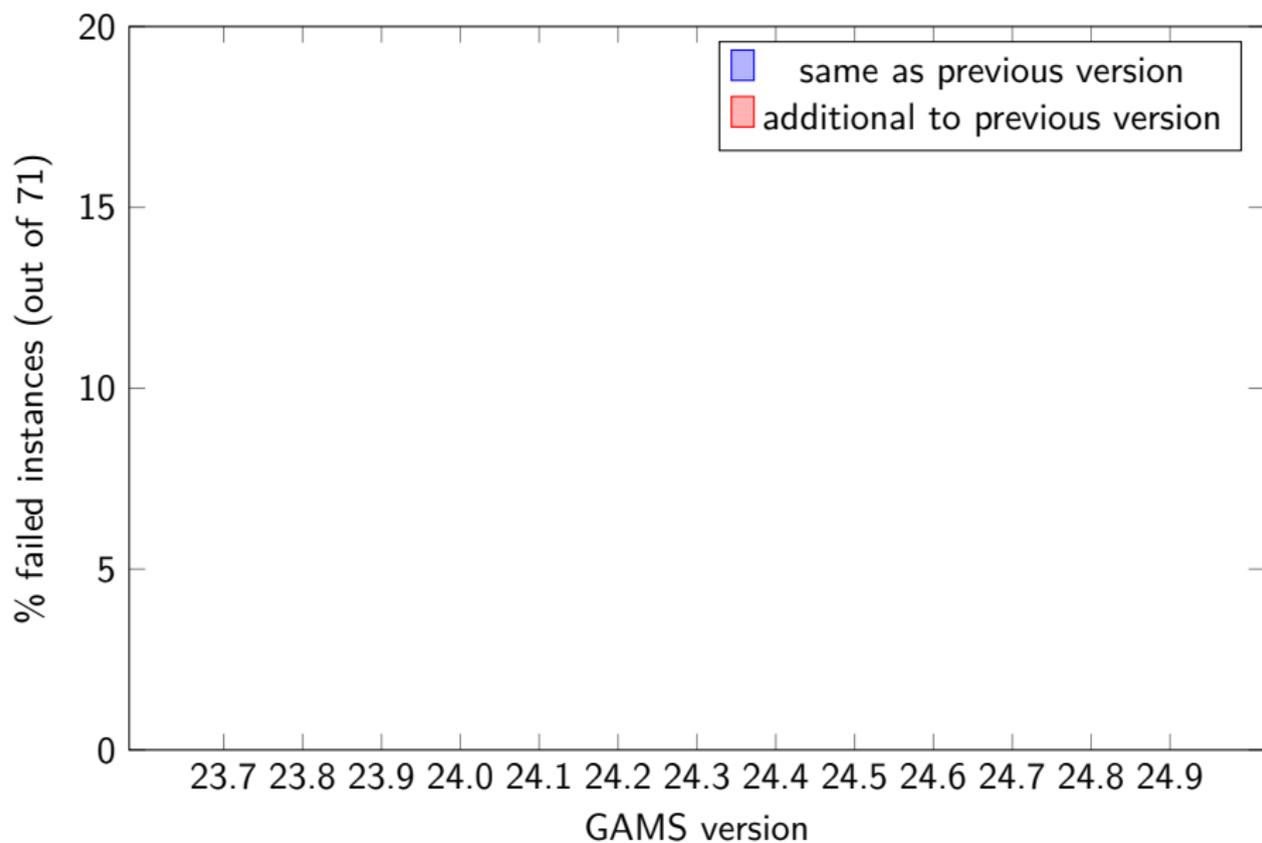
Overall speedup: 1.7

“Virtual Best” Solver

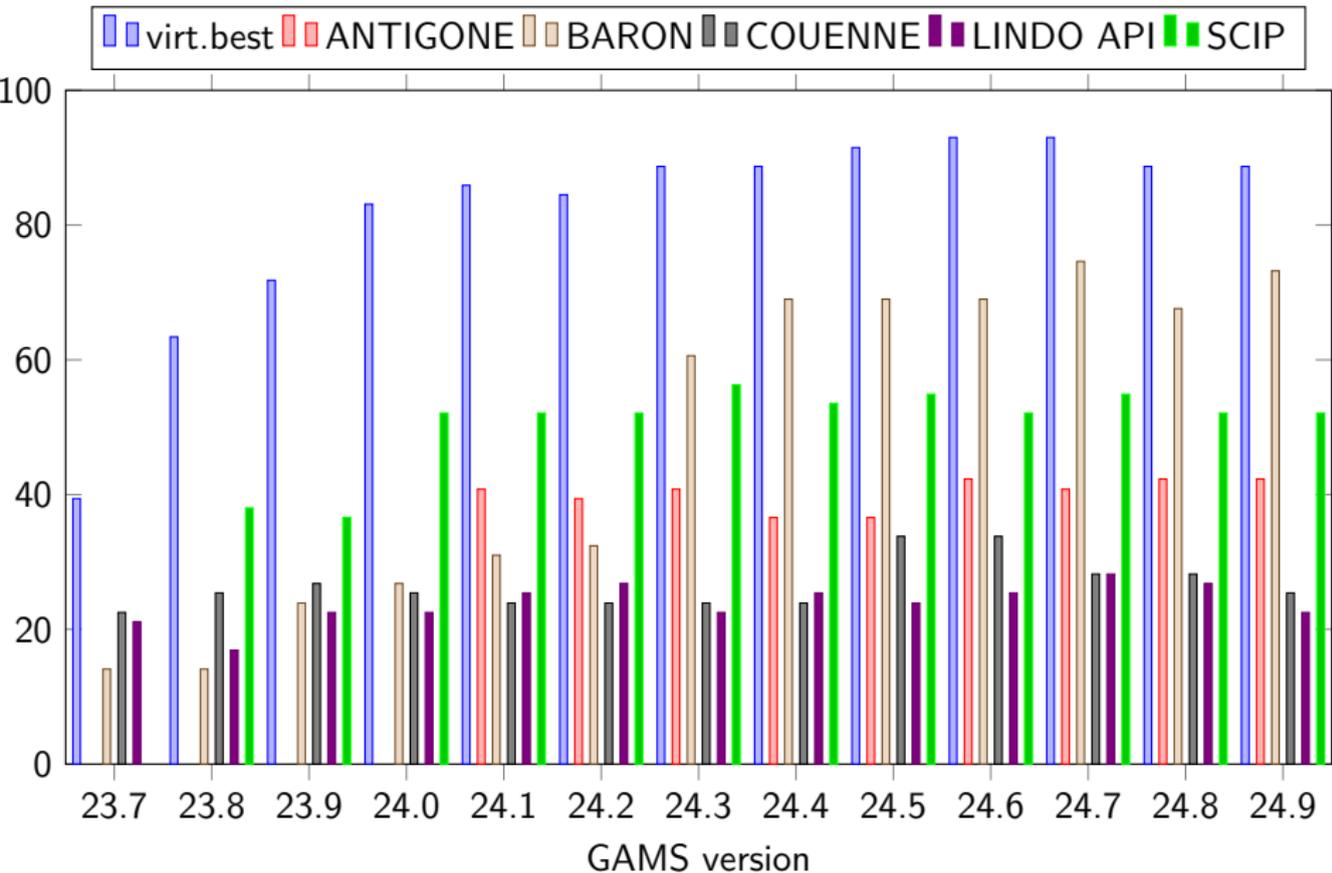
- ▶ common subset of instances
- ▶ for each instance and GAMS version, pick best results among all solvers



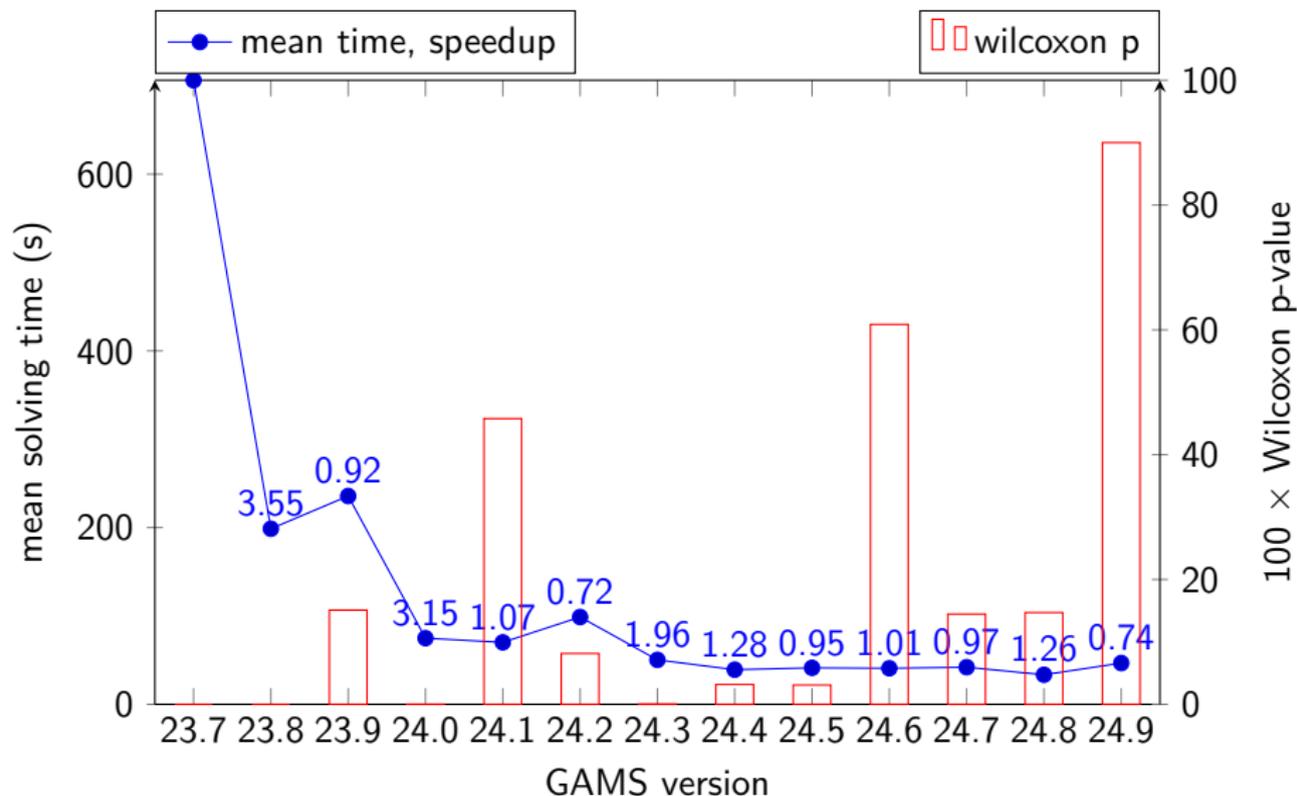
Virtual Best: Fails



Virtual Best: Solved (in %, out of 71)

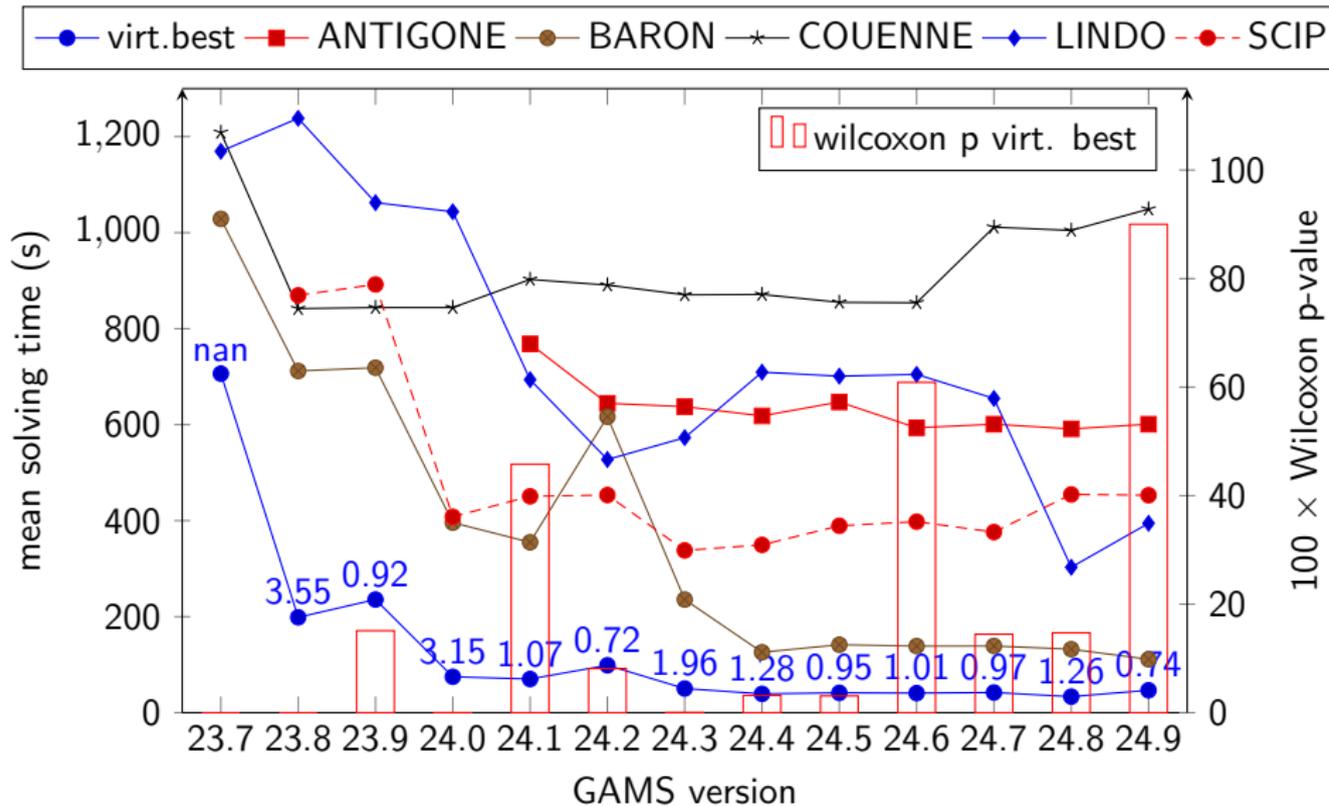


Virtual Best: Solving time, instances that never failed (71)



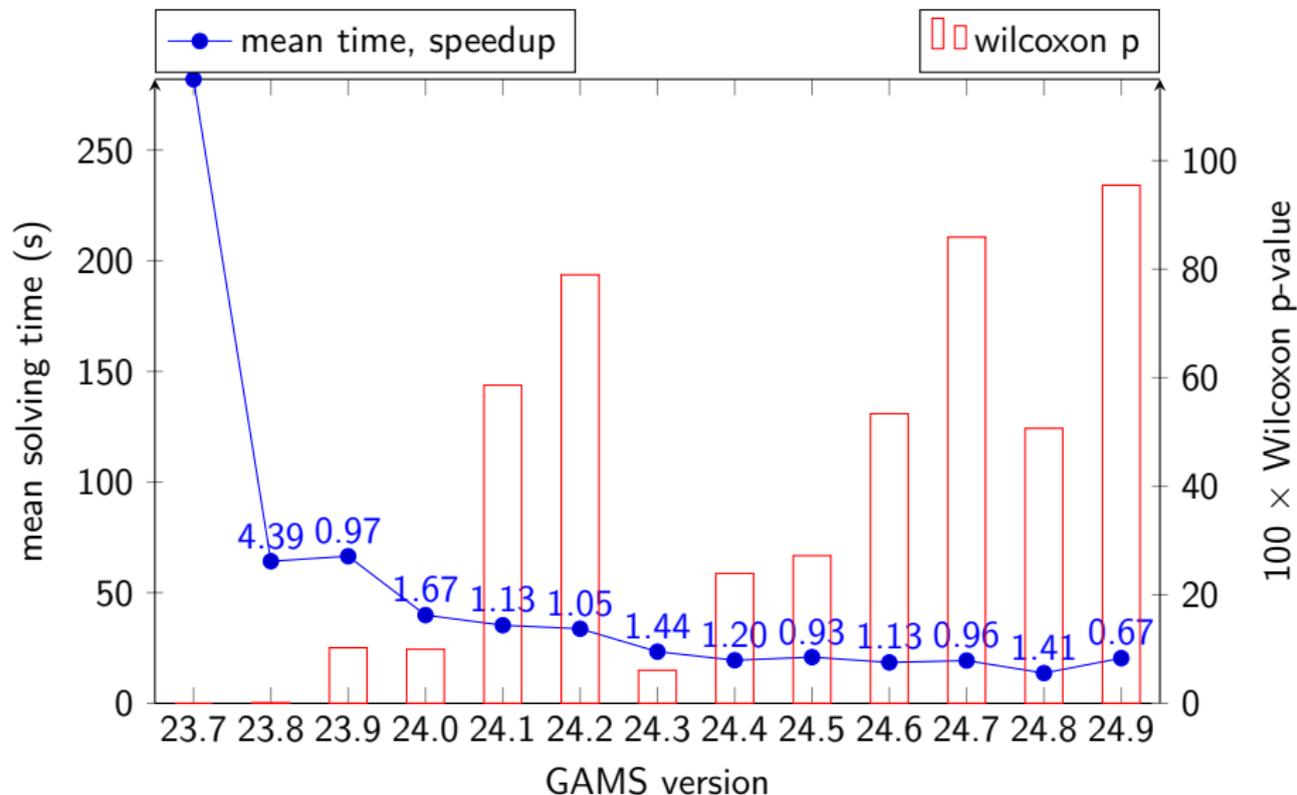
Overall speedup: 15.1

Virtual Best: Solving time, instances that never failed (71)



Overall speedup: 15.1

Virtual Best: Solving time on instances solved by all (20)



Overall speedup: 13.8